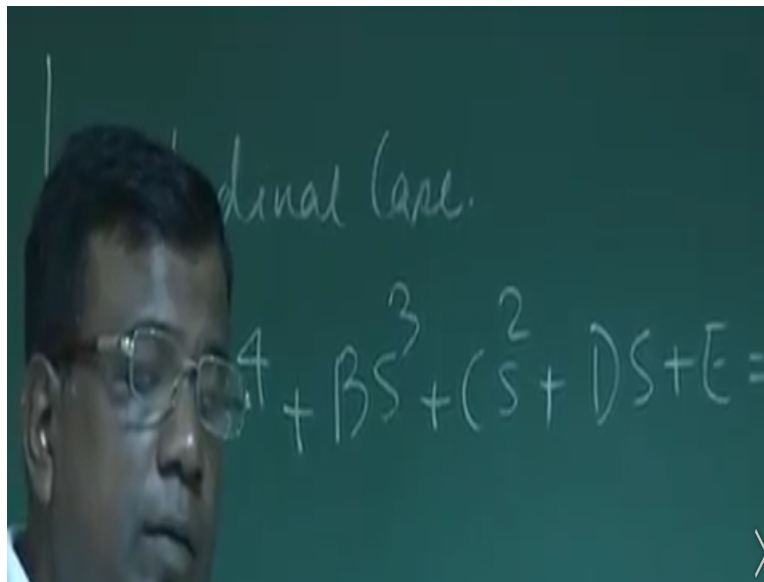


Aircraft Stability and Control
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Lecture – 54
Stability Augmentation System

Good morning, friends.

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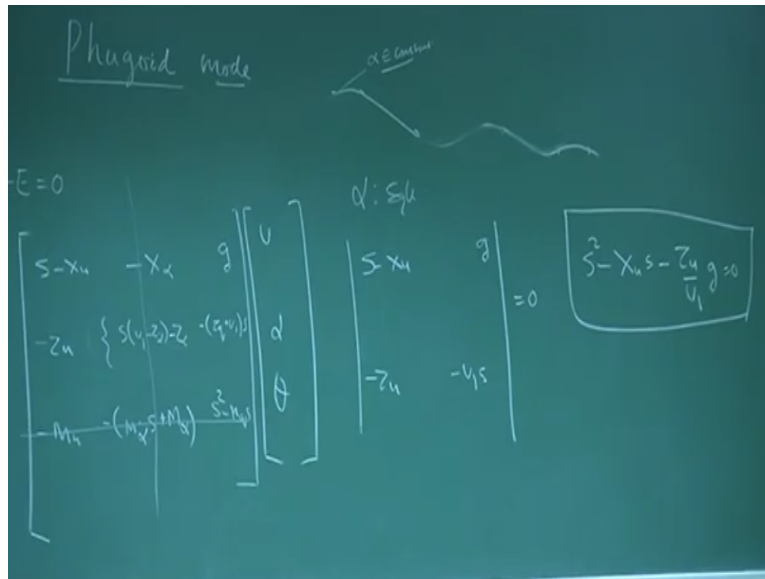


We will be revisiting phugoid mode little bit for enhancing of our understanding we will recall for a longitudinal case we got equation characteristic equation we form $A s^4$ plus $B s^3$ plus $C s^2$ plus $D s$ plus E equal to zero right and this coefficients of A, B, C, D, E can be expressed in terms of algebraic derivatives and probability etc and what we found from the example numerical example.

Once we find this root we get two complex value here and what we attribute to short period mode that is this disturbance compared to equilibrium very short time and during that time it's fair enough to assume the q perturbation is zero or speed remaining constant. Second root problem that we solve as coming pretty less or lesser really getting valued that is a long period mode unlike short period mode where the real root was large negative around minus 1 for this sample case.

The second case which is long period mode, we realize that this is phugoid mode that is after disturbance the airplane get excited like this ok and what is the assumption here that if you see this, the airplane.

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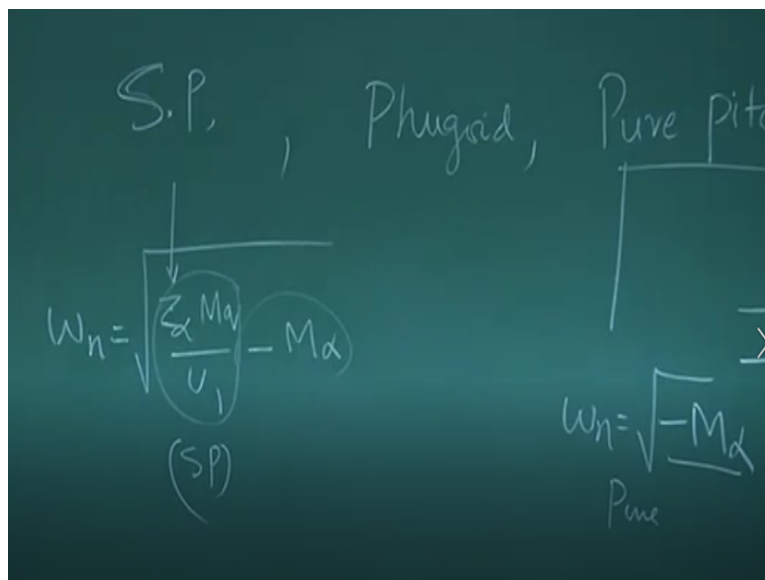
So alpha the angle of attack alpha almost remain constant which is at which is fairly put the approximation, I will not say a good, very good approximation but ok approximation. So we assume that the alpha equation is superfluous that is you need not consider that alpha equation at all right. We are not considering oscillating the moment this will about axis. If you do that then we get we can do the trick let me try s minus x u minus x alpha g minus z z u 1 minus z alpha dot minus z alpha minus z q plus u 1 into s minus m u m alpha s that is m alpha dot plus m alpha and s square minus n q s.

This is the equation characteristic equation I may know we are trying to approximate to get it characteristic equation for phugoid mode and want to check alpha to be superfluous that you do not consider alpha at all. And then you could see here that u alpha and theta so what we do. You drop this and drop this, that's takes care of this approximation we are assuming that alpha becoming constant and that how we get determinant. S minus X u g and then here minus z u and this is minus u 1 s right, this equal to zero ok.

This is equal to zero so then you get the characteristic equation $s^2 - X_u s - Z_u$ by U_1 into g equal to zero. So what I want to stretch is please understand that from this equation we get the approximation we assume that α is superfluous so we have dropped this and this and says there is no pitching moment be considered about y axis because it is going like this. This is the approximation ok right so.

Then convenient results last term will have obtained no other point want to find but I am going to tell you is answer. Let us see what we have done we have done the short period phugoid mode of approximation.

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Short period then phugoid and we have also done pure pitch ok. What was pure pitch, pure pitch was as simple as let I am going like this the airplane is at equilibrium and give a disturbance all the motion is happening pitch but you can understand airplane in free space if this lot of thing is happening so that's why the angle of attack will change.

So it will have this short of motion also right. When in pure pitch we are neglecting that. That is essentially what we are telling if we are picking similar to model wing -- here and oscillation is like this and the velocity vector will be constant here. So there is no question of very vertical motion of the airplane. So all in this $\dot{\theta}$ which is equal to q right. I will make an airplane

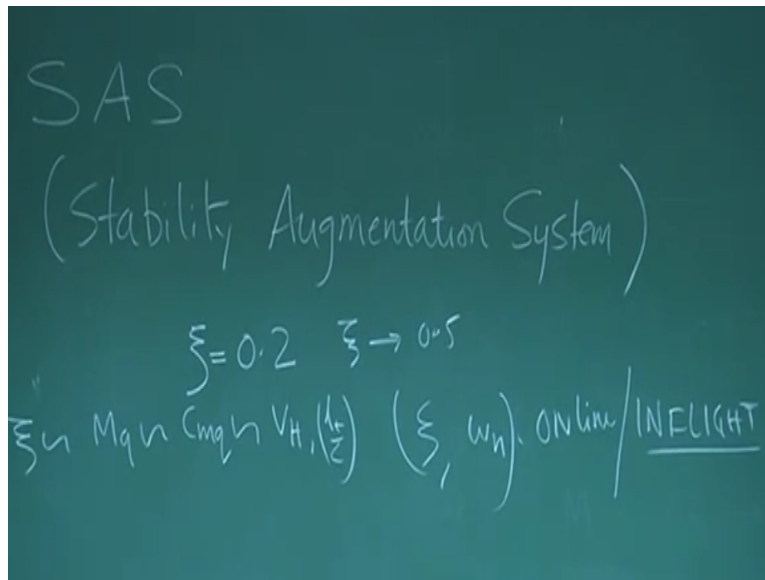
where you take the theta either alpha force in this direction there will be motion in this direction also right. This answer comes to the combined motion.

There was pure pitch and there we found ω_n angle root minus $m\alpha$. For short period what we got ω_n is I write under root minus, $z\alpha$ $m q$ by u $1 - m\alpha$. If you see this short period approximation and if I go by pure pitch here root of minus $m\alpha$ this term here additionally comes down which has $z\alpha$ that you understand the $z\alpha$ will come either restriction on the airplane to go up and down ok.

At the designer for the designer air craft I start with this I got with the so many numbers I know what we have got. $M\alpha$ means what. $M\alpha$ is related to $cm\alpha$ right. So I design an airplane what is the stability margin? Static stability margin that is we know that $cm\alpha$ can be related to d_{cm} by d_{c1} ok.

So I can start for consuming the airplane d_{cm} by d_{c1} by 10 percent and then I found natural frequency and then I go for designing the airplane so this way I did. Then I go for modify when come to short period and if my airplane will shows configuration by and then I come to dynamic stability is $A s^4 + b s^3 + c s^2 + d s + e = 0$. I solve that whole equation so this is the simpler root go from here to here then go to that big equation ok.

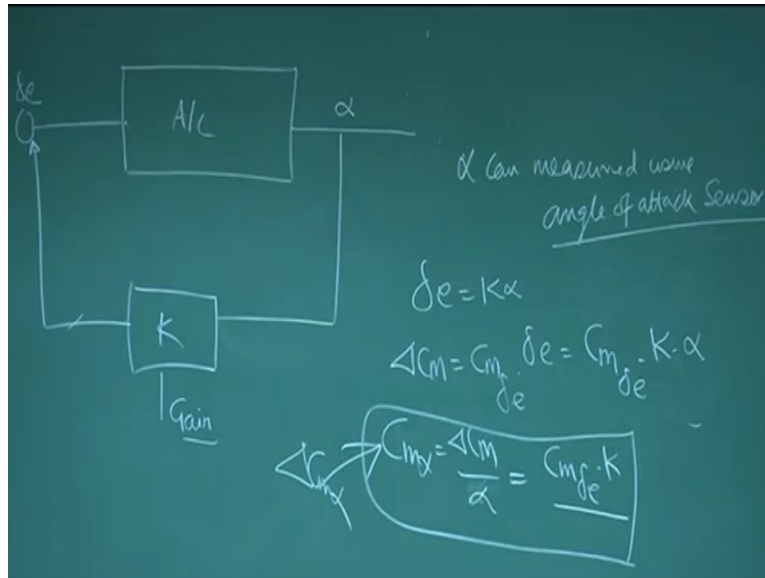
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Today I thought I will share with you something called stability of augmentation system. This is SAS what is the meaning of this SAS that how can I augment stability of airplane that is suppose the airplane has some zeta is 0.2 since this is longitudinal mode. Now we want to increase zeta to 0.5. what are the ways we know that zeta is proportional to $m q$ is proportional to cmq as cmq are in the ratio l by c . so I can change the terminal ratio I can change l by c I change $m q$ and in turn theta change.

But if you want this zeta to be changed without changing further the geometric of an airplane is configured. How online we can change zeta or how online we can change ω_n online in a sense it can be in flight ok. So what we can do we can reserve that I will be discussing, our discussion will be there. Let us understand how to do that.

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Let's us everyone see $C_m \alpha$ if we have $C_m \alpha$ basic and that give $C_m \alpha$ new so designed well. What is the mechanism we have seen we have seen this is the airplane equal to SAS this is the aircraft and you know this is the δe and this will be the α and that in α . What does these diagrams tells you it is telling that in flight you tab α . How can I tab α . α can be tabbed using α can be measured or paired using angle of attack sensor.

So I tab α and then I deflect this elevator δe proportional to α k α k is gain ok . Now giving δe equal to $k \alpha$.

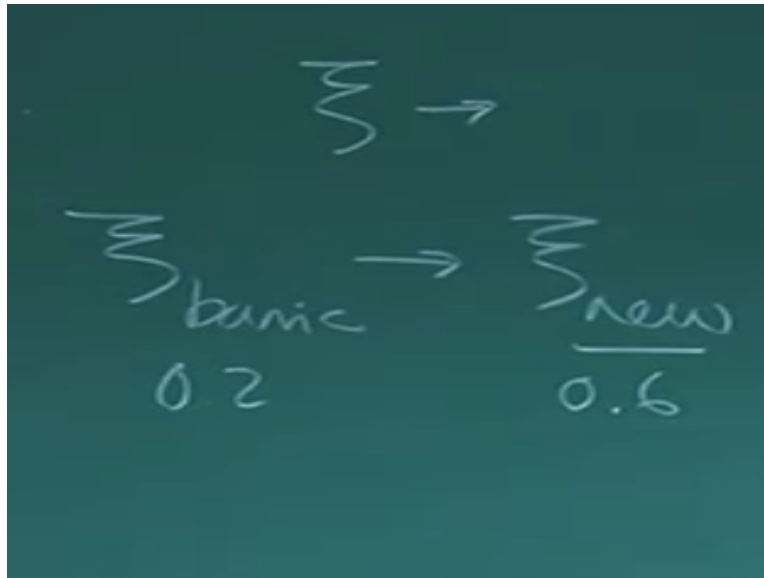
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The image shows a handwritten derivation on a chalkboard. At the top, it says $C_{m\alpha_{back}} \rightarrow C_{m\alpha_{new}}$. Below this, the equation $Wn = \sqrt{-M\alpha} = \sqrt{\frac{-1}{\sum \rho v^2 S} C_{m\alpha}}$ is written. To the right, $\delta e = k\alpha$ is written. In the middle, a box contains the equation $C_{m\alpha} = C_{m_{\delta e}} \cdot k$. At the bottom, a larger box contains the equation $C_{m\alpha_{New}} = C_{m\alpha_{basic}} + k C_{m_{\delta e}}$. Arrows indicate the flow of information: from $\delta e = k\alpha$ to $C_{m\alpha} = C_{m_{\delta e}} \cdot k$, and from $C_{m\alpha} = C_{m_{\delta e}} \cdot k$ to $C_{m\alpha_{New}} = C_{m\alpha_{basic}} + k C_{m_{\delta e}}$. There are also arrows pointing from the top equation towards the middle and bottom equations.

I have delta cm equal to cm delta e into delta e that is cm delta e into k into alpha that is delta cm. Now what is delta cm alpha now that is delta cm by delta alpha or alpha it is the cm delta e into k. You could see that this cm was additional cm alpha ok. So by giving an equation proportional to k where predict additional cm alpha into am delta e k what is the value of k. k has the value of 1.001 and I can go on filling alpha ND deflect the elevator proportional to k alpha and then I give delta cm alpha which is equal to cm delta e into k.

So cm alpha new whatever you want which is equal to cm alpha basic available plus k into cm delta e we have to choose the value of k so that we will get cm alpha new whatever we have.

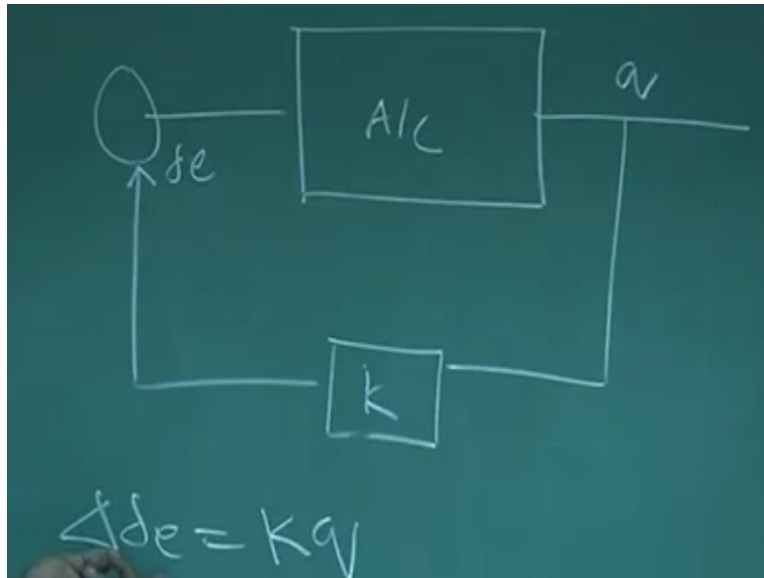
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This is one way we are augmenting ζ above the ζ sets. ζ sets primarily matter of frequency between under root of minus m alpha equal to under root of minus half $\rho v^2 s c \bar{c}$ α by $I y y$ if you are changing this ζ and ω_n will be changing right. So you have problem is you need to change the natural frequency from this value to that value I can tune sheath to get that ζ new value or ω_n value right.

Suppose if second question want to change ζ . Suppose we want to change ζ that id the requirement that is the ζ basic in the airplane and we want ζ new. This side was 0.2 and this side was 0.6 to flight. How do I do that? Again I will come back here.

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This is aircraft and this is again delta e and this is q this is k and what I am doing now and giving that additional deflection proportional to q right. I sense q through q and through master dimension plane and ensure that the delta e is proportional to k q. Once I do that what is happening what is delta cm.

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$$C_{mq_{\text{new}}} - C_{mq_{\text{basic}}} = \frac{2U}{c} C_{m_{\delta e}} \cdot k$$

$$\Delta C_m = C_{m_{\delta e}} k q$$

$$C_{mq} = \frac{\Delta C_m}{\frac{q c}{2U}} = \frac{C_{m_{\delta e}} k q}{\frac{q c}{2U}} = \frac{2U C_{m_{\delta e}} k}{c}$$

$\Sigma \rightarrow C_{mq}$
 $0.2 \text{ to } 0.6$

Delta cm is cm delta e into k q is the additional velocity. So what I can do cmq equal to delta cm by q c by 2 u or 2 u cm delta e into k q by q c bar 2 u. q q get canceled which is equal to 2 u cm delta e into k by c. Now that's you could see that suppose zeta has but I know zeta is proportional to cmq another addition for zeta we have already done that. So now I need to increase the zeta

from 0.2 to 0.6 so that it corresponds to some cmq_{new} that is the value we required to enhance ζ from 0.2 to 0.6.

So what I will do I will write that cmq_{new} minus cmq_{basic} and that is additional cmq required that will be $2u$ by c $cm_{\Delta e}$ into k so I can go on plugging in number in k and then c that I get appropriate cmq_{new} at the speed that all be given that able to control power. All your guided system when you are using this mechanism in the inner loop ok. So I thought I will also end this course and I will give initial brief description on the SAS which is the stability augmentation system also measure.

Please understand that also I change cmq or cm_{α} it will affect the other derivatives $c_{l\alpha}$ will change $c_{l\Delta}$ will change that you could see by plugging them into the equations right. Thank you very much this is the end of SAS part.