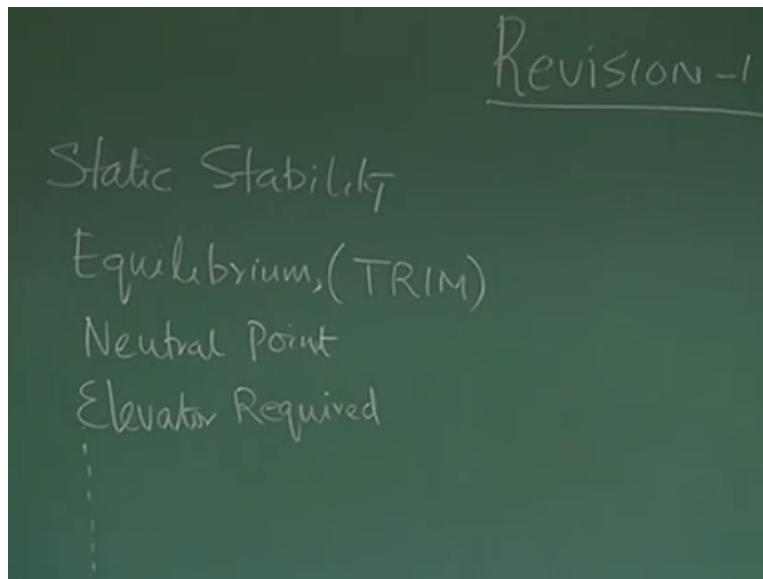


Aircraft Stability & Control
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Lecture -56
Tutorial - 1

Good morning friends what do have to be decided by reviewing all the fore arm questions, that potions that we need to have one or two succession words. I can revisit whatever discussed in this course and try to touch the salient points this you can treat as tutorial you can treat as a mann ki baat but this week completely. I try to revisit whatever we have to discussed and underline the salient point if you see we started with let me give a name for this revision-1.

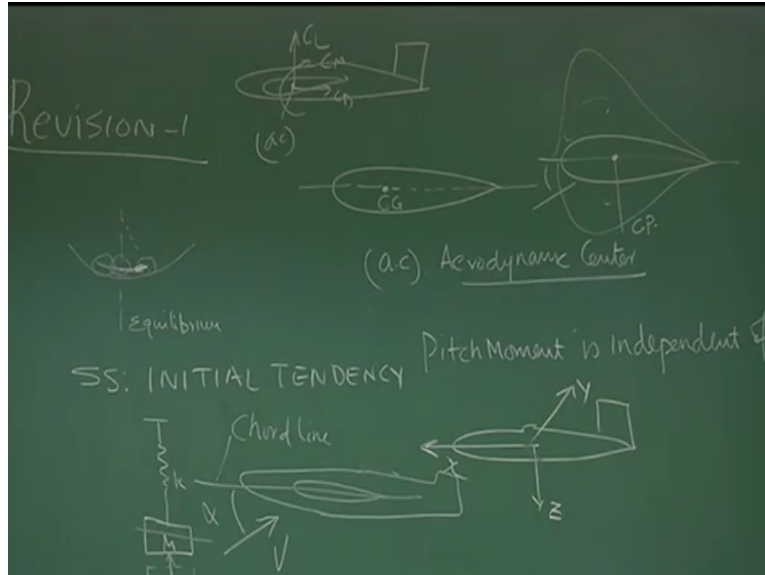
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If you see that, when we started this course we use one term at statics stability we use term like equilibrium also we use specific one trim, and then we also talk neutral point. We also talked about Elevator required for trim then as we progresses we glance throw lateral directional case and finally came down to dynamic stability ok. They will start with static stability. What understood?

What our understanding is as for as static stability is concerned it said if body in the equilibrium is disturbed and if you observe it has initial tendency to come back to equilibrium it said the body is having static stability ok.

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And we try to explain through the diagram where this is the equilibrium, and by equilibrium we all understand at this condition lift force and net moment is zero ok. And how we explain we said it is disturbed from the equilibrium and once the disturbance is withdrawn it has initial tendency to come back to equilibrium. We say it is static stable and if we see that such a diagram. There is force component of gravity and this ball will roll here like this but we talk about static stability it has initial tendency that's more important.

We are not talking about the dynamic at all, we are talking about the transient at all only the initial derivative tendency. If it is having an initial tendency we said it is static stability so what was the keyword for static stability it is the initial tendency to come back to the equilibrium ok. We try to explain this through mass spring systems this is spring this is mass and you know if I stretch it somewhere here and release it.

It also has initial tendency to come back to equilibrium it will oscillate that is not the point of concern for the static stability concern it is only the initial tendency that matters ok you are from these two examples, these two illustrations when we are talking in terms of aircraft. What we said we see this is aircraft this is only a wing aircraft and flying wing type concept and said this is the center of gravity and define term for a c is an aerodynamic center.

What was that aerodynamic center? Aerodynamic center is that 56 point at which the pitching movement is independent of angle of the attack. What is the pitching movement pitching movement you know it is a movement about aircraft y axis. What is air craft y axis. We have following this convention if this is x this is y and this z in right hand side and what is pitching movement about the y axis ok. What is the aerodynamic center that 56 point about pitching movement.

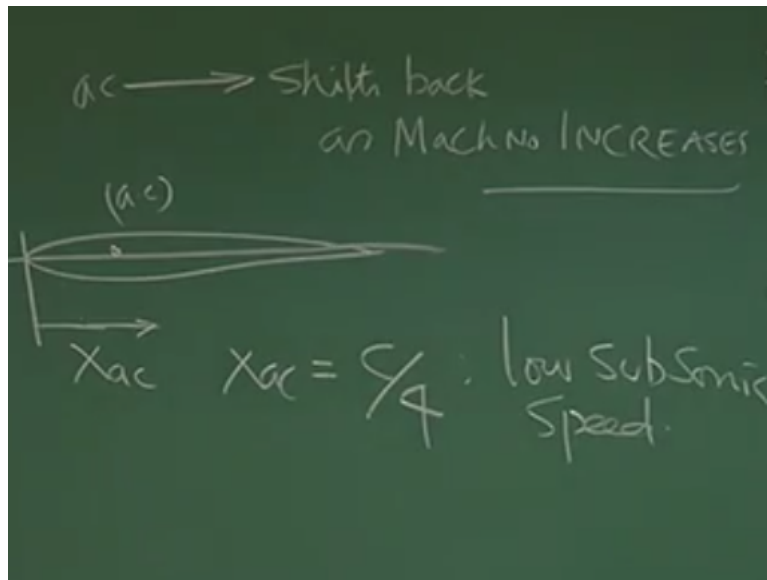
Pitching moment is independent of angle of attack and what is angle of attack as we also understand. If this is the airplane this a wing and this is the chord line and this is the velocity vector the angle between the chord line and the velocity vector in the vertical plane is defined as angle of attack ok. So we know understood are reconfirmed of understanding.

And the Aerodynamic center is that 56 point about the pitching movement is independent of an angle of the attack, pitching movement is independent of angle of attack. Now we also understand and this is the body and any angle of attack that will be perturbed distribution and net force. We can be represented at the center of pressure and you know what is the center of pressure the center pressure is at that point of this resultant force is what about acting here and there in fact the pressure distribution top and bottom surface.

When we integrate the pressure of area top and bottom we get result in force and depending on the perturbed distribution depending up on the quality we can define find out the center pressure of like you have center of gravity ok but what about doing will here we have the represent the forces moment acting at the center of pressure. What we will do forces and moment we represented at aerodynamic center.

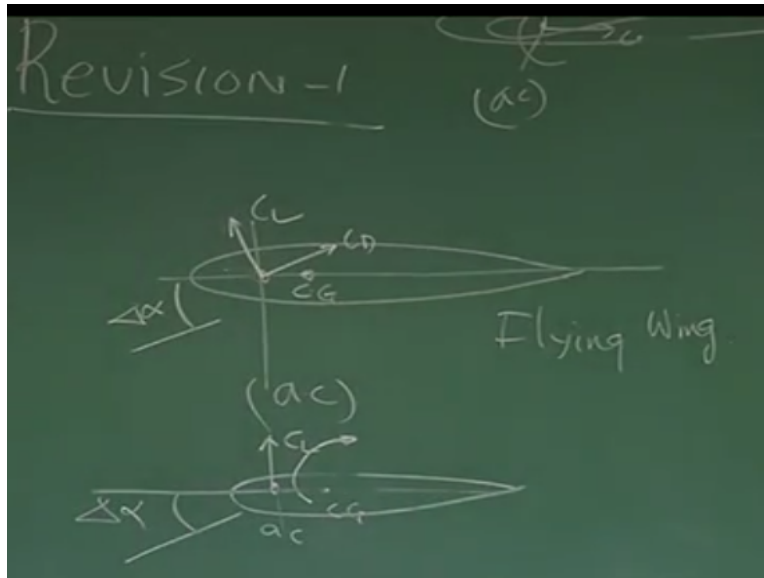
I put to the c_l and c_d , c_m it set putting at center of pressure. We will transfer and the represent the acting at the aerodynamic center because have additional advantage at above the aerodynamic center pitching movement is independent and the angle of attack is that helps and typically we also know for a low subsonic wing.

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This aerodynamic center location is if I measure from here if I write it x_{ac} . The x_{ac} is typically $c/4$ low subsonic speed for conventional air ok. But as I increase the speed as it goes to higher, higher speed. Then it is convincing to subsonic to high subsonic supersonic, this aerodynamic center shifts the backward as mac number increases. This is the understanding of the aerodynamic center ok. Once we understand this aerodynamic center now we will try to see for the aircraft. What is our understanding about static stability?

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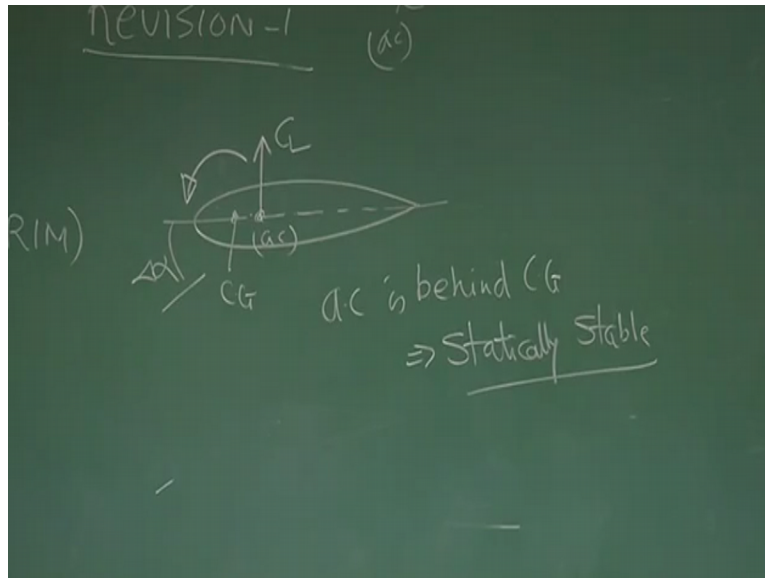


I will draw in here let's look at the flying wing configuration and if this is and center of gravity is flying wing. So this flying wing let's see the aerodynamic center is ahead of center of gravity ok. One this compound is possible now see. We going to see ask a question.

What that this is statically stable are not? How to I do that I introduce the disturbance the angle of attack. The movement I do this I know by now there will be C_L there will be C_D know this force is the ahead of cg the small angle is make not a simpler. I can write this is ac and this is cg for small angle and this is C_L and what is happen. As I introduce the angle of attack because the C_L will be there because the angle of attack and it will give a movement about the cg nose up.

If we see that force is here is it nose up moment it doesn't have a restoring the tendency of and it doesn't have initiate tendency to make a $\alpha = 0$ because this is α actually. It statically stable you should do like this let α become a zero α become whatever original it was right. So this ac is the ahead of cg of the flying of the explain wing. Then we say the aircraft is statically unstable and what will also same configurations.

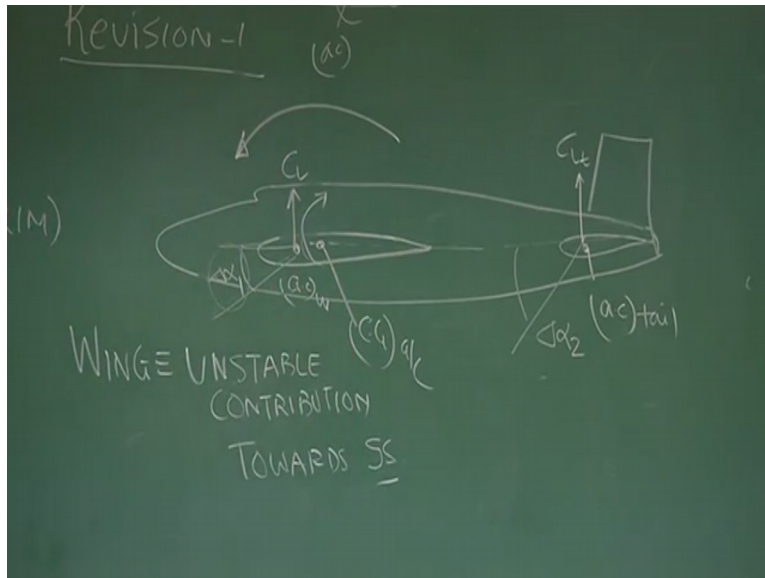
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If CG is here the AC is here you could see that if there is the alpha disturbance that is. When I say the alpha disturbance is what the suppose the airplane is closing at alpha 2 degree because the angle of attack becomes 2.5 degree so this is 2.5 minus 2 degree is 0.5 degree is the disruption. So you know that the disrupt is there AC is begin CG and I can draw the CL and this give a nose down movements nose down pitching movement.

So it will try to do come back to that whatever all given alpha was there it will discourage any increasing angle are if have initial tendency to come back to the equilibrium. So this configuration. AC is behind CG is aircraft is statically stable this find for the flying wing but we talk about aircraft. When it is the aircraft when drawing the aircraft.

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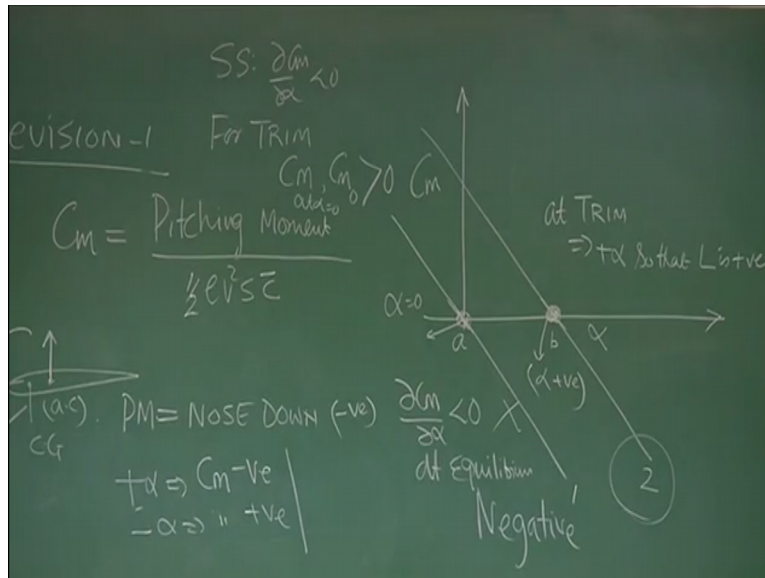
So suppose this the aircraft right as wings now let's see the ac of the wing is of cg of the aircraft if this is combination. Then if I you ask a question as the wing is concerned the wing is static stability to aero plane in constant of here is see is ac of the wing is ahead of cg of the aircraft this will give unstable contribution towards static stability right you can understand very well there is the alpha disturbance the C_L is here the C_L will give nose movement it will further increase the angle of attack.

So wing will proved unstable contribution for the static stability but now want to make it statically stable. What can I do? The question is this and that is where the concept comes. We put horizontal tail. Now what is happening actually you see if there is alpha contribution and disturbance. The $\Delta\alpha$ activate wings and let's assume that same $\Delta\alpha$ and little $\Delta\alpha$ alpha 2 and I call it $\Delta\alpha_1$ and the I am in little bit concise that is I know that angle of attack and wings difference which you know because downwards buying that please understand.

If there is a $\Delta\alpha$ at the wing to give C_V and the nose up movement so it is the tendency to increase angle of attack but what is happening at the tail the tail aerodynamic center of tail which is behind center of the gravity of the aircraft. So it will give contribution physically what will happen because of this C_L tail and this moment of the large info a nose down movement.

It will try to decrease tail to comeback original angle at the depending of on which contribution is more is dividing on is contribution stability, contribution of because a wing and, the stability contribution of the tail, and the stability tail then more. Then to vision then the airplane will provide the stability got it that is the basic understanding ok now from here we talking in terms of cm vs cl graph remember cm pitching movement coefficient.

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We defined as pitching movement $1/2 \rho V^2 S \bar{c}$. The \bar{c} was what do have notice the static ability this is the aircraft center. And this is the center of gravity. So if there the disruptions in terms of this combination no downs movement pitching movement is nose down. The nose down is as per of conversion is negative. What we you like for static ability is there is positive angle then the pitching movement C_m should be negative right for negative alpha should be positive.

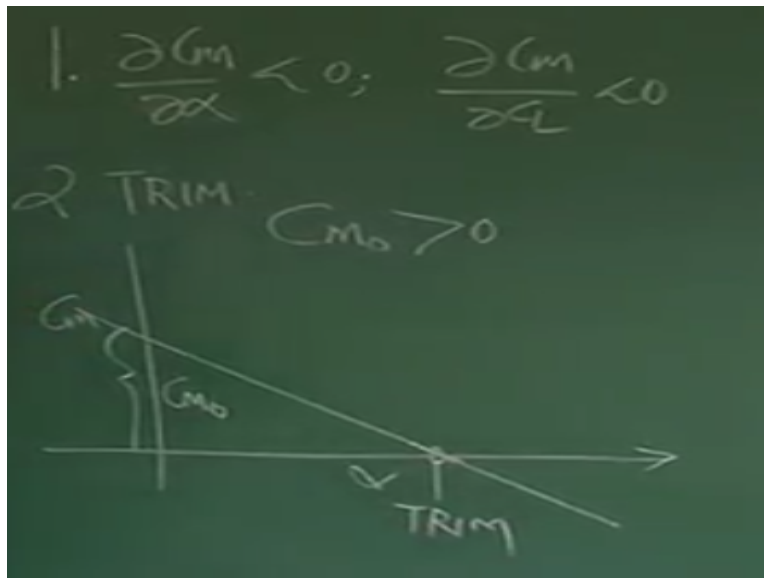
So this understanding is develop C_m and the alpha graph this is these are possibility if \bar{c} between 1 and 2 first identify what are quality of points the equality point. Where $C_m = 0$ a and b equilibrium point you know that if we want to insure that statically stable then this $dC_m/d\alpha$ in less than zero. The positive alpha C_m negative the negative alpha C_m should be positive. We translate the understanding in the mathematical form is let the slope at equilibrium should be negative.

The equilibrium we identify point of the a and b and see the slope at a and the slope at b was a negative. So both are statically stable place right and what are difference. We find out send after all the trim at trim. I want positive alpha for that lift is possible after all lift equal to weight is one of all equilibrium point. Of course it also debit in comorbid you can have lift positive lift given at negative angle.

We have not positive in that ok so these are the trim points realize and slope about the trim point should be negative now between two radians resaleone and realize that this a is equal to alpha = 0 this b is = to alpha positive how requirement is two design a aircraft cm is = alpha should be close and difficultly should be like this not this because it is following the trim of the figure 2 can derived positive alpha.

The positive alpha for weighting lift that is how for the put another condition the static stability find $dc_m/d\alpha < 0$ but for trim of the positive angle at that c_m at $\alpha = 0$ are $c_m > 0$ and this is the condition. We put mathematically throw our understanding of aircraft of the static and trim right. What is that nut shell of our understanding as for as designer is concerned that we need to

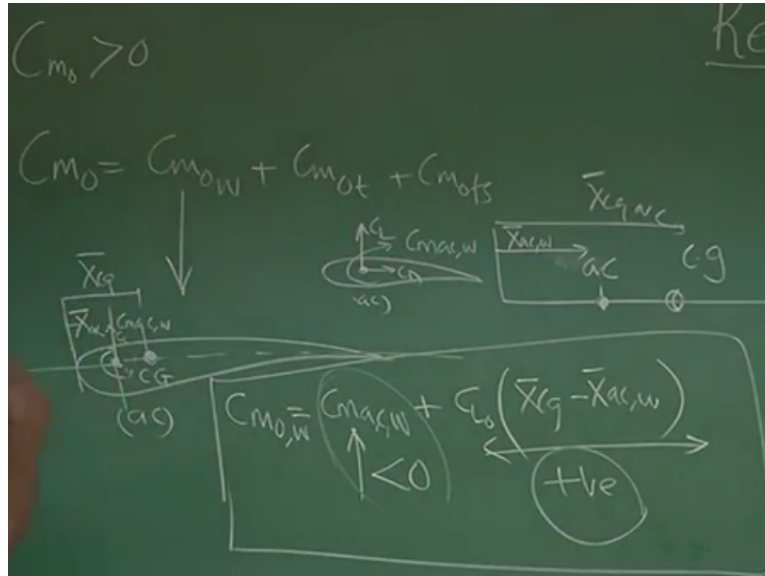
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Insure the $dc_m/d\alpha < 0$, we know is equal in $dc_m/d\alpha < 0$ because c_l not + c_l alpha into alpha second thing for trim we want to ensure that $c_m > 0$ finally. We are focused to version of c_m

and versus alpha like this. This is C_m not and this is C_m alpha the catch point is C_m alpha the slope of this line at trim at this point that is important trim point right clear .

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We are talking about C_m not > 0 and also because that C_m not = C_m not wing + C_m not tail + C_m not fs. I will just try to C_m not wing understand if we using the cambered aero foil wing suppose then this is the cg let this is the ac and this is \bar{x}_{ac} this is \bar{x}_{cg} I put the bar. You know what is bar, is the non-dimensional as in the aerodynamic chord. This is the aero foil you know that I represent at ac for a cl this is cd and there will be C_m as was know these.

So there is an ac wing for cl and cd then you know that then we calculate C_m not that will be of the wing = C_m ac wing then +cl not($\bar{x}_{cg} - \bar{x}_{ac,w}$). Please understand here the C_m al w became a < 0 as aim C_m not positive or negative next negative finally. We want $C_{m_0,w}$ is = positive ok. This is negative so. I try margin throw this expression and that is possible and the when \bar{x}_{ac} of the wing is ahead of cg otherwise this became negative the \bar{x}_{ac} of the wing this is \bar{x}_{ac} of the ac in the center and this is the center of gravity of the airplane is \bar{x}_{ac} of the wing this is \bar{x}_{cg} aircraft.

If would see that cg it give it statically and stable contribution at C_m not is constant. It could \bar{x}_{ac} the one and only becomes positive right .We are not the burgherat about become contribution at

static stability because we have a tail it just stable at and this is very important should not forget this lessons.