

**Basic Environment Engineering and Pollution Abatement**  
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**Lecture 21**  
**Air Pollution Control 1**

Hello everyone. Now, we will start discussion on the topic Air Pollution Control part 1. So, far we have discussed that our first strategy should be to prevent pollution in spite of that, there might be some possibilities to create pollution, we cannot prevent 100 % pollution creation, although we take sufficient care. So, in that case, what pollution is generated that has to be controlled and this can be done by using different equipment and instrument and different methods. So, that part we will discuss in this module.

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Air pollution control equipment

Contents

- Typical air pollutants
- Typical composition of different gases causing air pollution
- Processes and equipment for removal of unwanted elements from gas
- Removal of specific gas components like SO<sub>2</sub>, NO<sub>x</sub> and CO<sub>2</sub>
- Ambient air cleaner, air filter

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And the contents are typical air pollutants, typical composition of different gases causing air pollution, processes and equipment for removal of unwanted elements from gas, removal of specific gas components like SO<sub>2</sub>, NO<sub>x</sub> and carbon dioxide and ambient air cleaner and air filter. So, this content we will cover in four classes. Now, we will see typical air pollutants, already we have discussed that there are a number of criteria pollutants, which are very very important for the quantification of air quality. Those are particulate matters, SO<sub>x</sub>, NO<sub>x</sub>, ozone, lead.

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**Typical air pollutants**

- Particulate matter (PM<sub>10</sub> and PM<sub>2.5</sub>, ...)
- Ozone (O<sub>3</sub>)
- Nitrogen dioxide (NO<sub>2</sub>)
- Carbon monoxide (CO)
- Sulphur dioxide (SO<sub>2</sub>)
- Lead
- CO<sub>2</sub>
- Methane ✓
- Chlorofluorocarbon (refrigerants in air conditioners)
- VOC ✓

**Source of Pb**  
some aircraft fuel, metal processing plants, waste processes such as incineration and battery acid production

**Source of O<sub>3</sub>**  
chemical reactions between multiple different oxides found in the air,

**Methane comes from** livestock, swamps and human activities

**Source of VOCs** ✓  
Vaporization of petroleum fuels, personal care products such as perfume and hair spray, cleaning agents, dry cleaning fluid, paints, lacquers, varnishes, hobby supplies and from copying and printing machines.

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And apart from these, we have VOC, CFC, chlorofluorocarbon and NO<sub>2</sub> nitrogen dioxide and ozone. The sources of these pollutants we have already discussed, it can enter into the environment through natural sources as well as manmade sources, and some sources are also mentioned here that is source of lead, source of ozone and methane and volatile organic carbons.

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**Typical composition of different gases causing air pollution**

Process	Typical Gas composition	Elements to be removed
Combustion ✓	CO <sub>2</sub> , H <sub>2</sub> O, NO <sub>x</sub> , SO <sub>x</sub> , PM, N <sub>2</sub>	NO <sub>x</sub> , SO <sub>x</sub> , PM, CO <sub>2</sub>
Gasification ✓	CO, H <sub>2</sub> , CO <sub>2</sub> , H <sub>2</sub> S, COS, PM, CH <sub>4</sub>	CO <sub>2</sub> , H <sub>2</sub> S, COS, PM
Pyrolysis of biomass and wastes	Hydrocarbons, CO, CO <sub>2</sub> , H <sub>2</sub>	CO <sub>2</sub>
Pyrolysis of waste plastics ✓	Hydrocarbons, CO, CO <sub>2</sub> , H <sub>2</sub> , HCl, dioxins	CO <sub>2</sub> , HCl, dioxins
Anaerobic digestion ✓	CH <sub>4</sub> , CO <sub>2</sub> , H <sub>2</sub> S, H <sub>2</sub> O	CO <sub>2</sub> , H <sub>2</sub> S, H <sub>2</sub> O

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Now, we will see different types of gases which are responsible for the generation of pollutions in the air, examples are say combustion gases, so when some fuel or carbonaceous material is combusted, then we get a flue gas which mainly contains carbon dioxide, NO<sub>x</sub>, SO<sub>x</sub>, H<sub>2</sub>O that is in vapor and particulate matter and nitrogen.

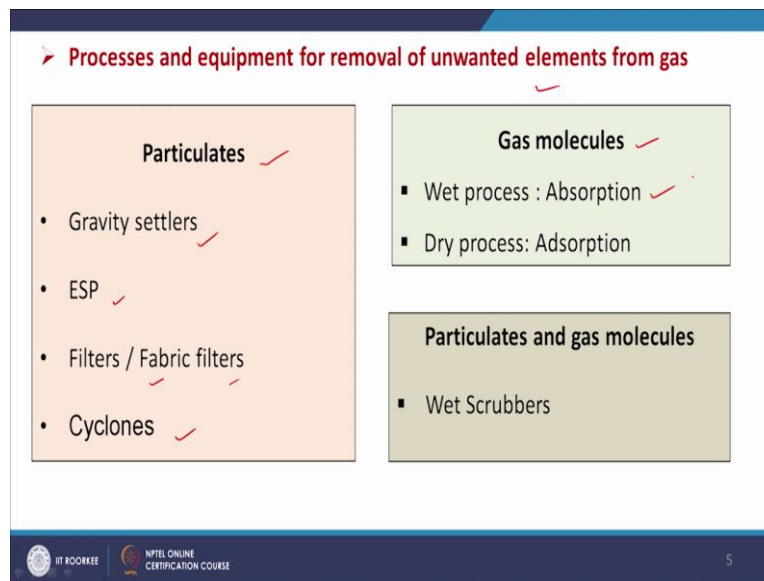
And in this case, we need to develop some methodology to remove the components like  $\text{NO}_x$ ,  $\text{SO}_x$  particulate matter and carbon dioxide. So, similarly through a gasification process, we can get different gas in the produced gas stream like carbon monoxide, hydrogen,  $\text{CO}_2$ ,  $\text{H}_2\text{S}$ ,  $\text{COS}$ ,  $\text{PM}$  and  $\text{CH}_4$  these are the major components and we need to remove these also carbon dioxide  $\text{H}_2\text{S}$ ,  $\text{COS}$  and  $\text{PM}$ .

Pyrolysis of biomass and waste through this route also the gas comes out to the environment which contains carbon monoxide, carbon dioxide, hydrogen and hydrocarbons, we need to remove carbon dioxide from this. And pyrolysis of waste plastics also gives us different gases that also contains hydrocarbons, carbon monoxide, carbon dioxide, hydrogen,  $\text{HCl}$  and dioxins.

So, this dioxin is very very toxic and we need to remove carbon dioxide,  $\text{HCl}$  and dioxins from these gas streams also and anaerobic digestion through this process, we get the gas which contains methane, carbon dioxide,  $\text{H}_2\text{S}$  and  $\text{H}_2\text{O}$  that is moisture or vapor and removal of  $\text{CO}_2$ ,  $\text{H}_2\text{S}$ ,  $\text{H}_2\text{O}$  are very very important. So, this removal normally takes place in the premise where the gases are produced in industrial scale.

Apart from that, so vehicular emissions that is very difficult to control basically and it contributes to the ambient air quality. So, to make the environment clean, we need to control the emission of these gas components when it get entry into the atmosphere. Here we have not mentioned regarding hydrocarbons, hydrocarbons mostly is available in terms of unconverted hydrocarbons in terms of suits or it may be as volatile compounds, so, those are also needed to be removed.

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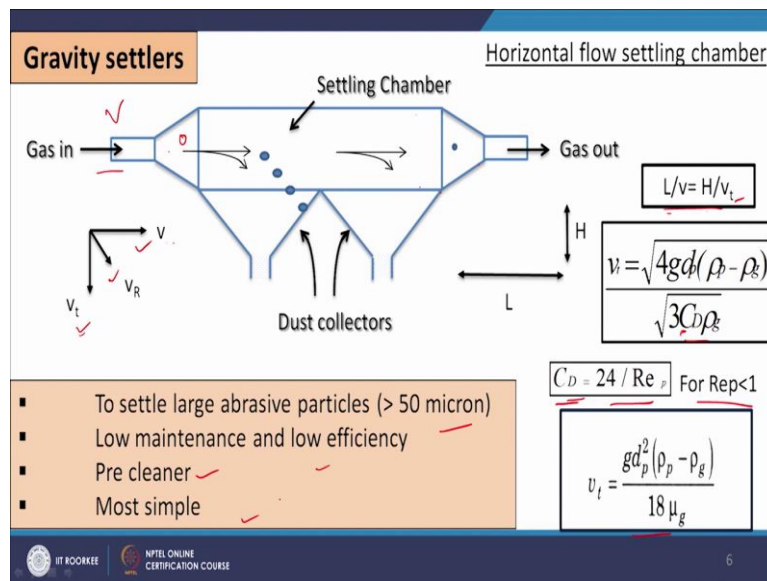
Now, we will see processes and equipment for removal of unwanted elements from gas. So, in the gas, one is particulate matter and another is other gas components we need to remove which are not desirable in the environment. So, for the separation of particles or the particulates there are a number of techniques and methods, we will be discussing those like say gravity settlers, then electrostatic precipitator and filters that is fabric filters and cyclones.

So, these are the mostly used equipment or the processes which are used for the removal of particulates from the gas stream, so, we will be discussing those. And for the removal of gas molecules like say  $\text{SO}_x$ ,  $\text{NO}_x$ , etc. we will be discussing two major methods, one is based on absorption that is wet process and another is dry process which is based on adsorption.

And there are some methods where both particulates and gas components can be removed like say scrubbing. So, wet scrubbers are also available, we will discuss all those processes and devices and we will learn how to remove the particulates and other gas components from the exit gas and what are the mechanism of these equipment and the principle of working of these equipment's. And in this part 1, we will be mainly focusing on the gravity settlers.

So, here this slide shows us a horizontal flow settling chamber, as we know, if we fall a ball or any particle from a height, so, initially the velocity is 0, then gradually its velocity will increase and it will attain a maximum velocity that will be stable thereafter, that is called terminal settling velocity. So, this terminal settling velocity bigger the particle size more the terminal settling velocity. So, to travel a certain distance the more the terminal settling velocity lesser the time required. So, the same principle will be applicable for the separation of the particles in the gravity settlers.

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So, this figure if we see, so, here is the gas in, so inlet gas is coming here. So, it will be having some velocity, so, that velocity is equal to say  $v$ . So, this velocity gas is coming so, if particles are present in it so, that particles will also be having the velocity  $v$  and here the gravity is also working on the particle, so the particle is under the action of multiple forces.

So, one trajectory we will get through which this particle will move. So, now it is having a horizontal velocity  $v$  and vertical velocity  $V_t$  that is terminal settling velocity. So, this is our resultant velocity. Now, if you see one particle is here, so, I want to get it separated. So, the basic principles or separation of any particles while it is in motion, just if we can put something in its path and then its flow will be arrested and the velocity in that particular direction will be 0 and the particle will fall.

So, if this particle we want to settle here certainly, the time required to travel from this point to this point, the inlet to outlet within this time the particle must travel the vertical distance which is, as per the dimensions of this settling chamber. So, this is the basic requirement or the design principle for this settling chamber. So, if we consider the length is  $L$  and height is  $H$ .

So, in this case,  $\frac{L}{v} = \frac{H}{v_t}$

$V$  is the horizontal velocity,  $L/V$  is the time required to travel from inlet to outlet by the particle,  $V_t$  is the terminal settling velocity that is the time required to travel the particles from the top to the bottom of this chamber, so this time requirement should be equal.

So, this is that critical condition for the separation. So,  $L/V = H/V_t$ .

Now, this  $V_t$  is equal to what?  $V_t$  is terminal settling velocity and terminal settling velocity will depend upon the particle size, the viscosity of the fluid, the density of the particle etc and what is the  $g$  value? That is a gravitational acceleration, so, those values will be influencing the value of  $V_t$ .

$$V_t = \frac{\sqrt{4gd_p(\rho_p - \rho_g)}}{\sqrt{3C_D \rho_g}}$$

So, these expressions we will discuss where from this is coming by the force balances on it and the  $C_D$  is nothing but the drag coefficient.

So, this drag coefficient will be depending on the velocity of the gas stream. So the velocity is higher that is your it will be in turbulent but velocity is less we will be getting this in laminar flow. So, up to certain Reynolds number we will be getting laminar flow and, in that case, when the Reynolds number is less, the  $V$  will be getting the laminar flow and, in that case,  $C_D = \frac{24}{Re_p}$ .  $Re_p$  is nothing but the particle Reynolds number so this  $C_D$  value we can replace it by 24 by  $Re_p$ .

$$V_t = \frac{gd_p^2(\rho_p - \rho_g)}{18\mu_g}$$

So, this expressions is the expression for the terminal settling velocity of a particle which is falling in a laminar zone the flow of the particle is not that high so, that the Reynolds number be less. And this equipment the gravity settlers are very simple and it is not costly and to settle large abrasive particles like say greater than 50 micron these devices is workable and it has low maintenance and low efficiency as well and it is also considered as pre cleaner. So, for the separation of very fine particles, it may not be that good device, but for the separation of relatively larger particle this can be a good option and this is a very simple method.

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**Gravity settlers contd..**

**Force balance on particle and terminal settling velocity**

Particle

$F_d$  : drag force =  $F_R$  = kinetic force

$F_b$  : buoyancy force

$F_g$  : force of gravity

Resultant force =  $F_g - F_b - F_d(F_R)$   $\Rightarrow$   $ma_\epsilon = mg - \left(\frac{m}{\rho_s}\right)\rho_f g - F_R$

At steady velocity  $mg \left[1 - \frac{\rho_f}{\rho_s}\right] = F_R$   $\rho_f$  = density of fluid in this case fluid is gas =  $\rho_g$

If particle is assumed to be spherical, then  $\left(\frac{\pi d_p^3}{6}\right)\rho_s g \left[1 - \frac{\rho_f}{\rho_s}\right] = F_R$

Where  $C_D$  is drag coefficient

$F_R = AKC_D$   $A$  = Characteristic area of the system

$A = \frac{\pi d_p^2}{4}$   $K = \frac{1}{2}v_t^2\rho_g$   $K$  = Characteristic kinetic energy per unit volume

$v_t = \frac{4gd_p(\rho_p - \rho_g)}{3C_D\rho_g}$   $v_t$  = relative velocity between the particle & liquid fluid (terminal settling velocity)

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Now, we will see how the  $V_t$  expression we are getting. So, let us see this is the particle which is falling. So, there is one force that is  $F_g$  that is gravitational force which is working in downwards direction. So, upward directions on force is working that is  $F_b$  that is Buoyancy force, as we know when a solid particle falls, then in a fluid, same volume of fluid is replaced and it gives a force to the particle in opposite directions.

So, that is buoyancy force and another force we will be seeing here that is drag force. So, this drag force is also working on this particle when it is falling in the air so that force will also work in the same direction of the buoyancy force opposite to the gravitational force. So, if we think about the force acting on this particle, and we consider the force balance, then we can say that the resultant force on this particle is equal to the (force due to gravity) – (force due to buoyancy) – (force due to drag). So, these are  $F_g - F_b - F_d$ .

So, this drag force is basically mentioned as kinetic energy force. So, in many books, it is written as  $F_R$  that is related to the kinetic energy of unit volume of the of the fluid. So, this is the expression for the resultant force on this particle. Now, when it will be moving with terminal settling velocity, so, there will be no resultant force, so that it will be moving into constant velocity that is terminal settling velocity.

So, in this case, we will be getting resultant force equal to 0. So, now, let us express this resultant force. So,  $m$  is the mass of the particle and  $a_E$  is the resultant acceleration. So,  $m$  into  $a_E$  that is the resultant force.

$$ma_\epsilon = mg - \left(\frac{m}{\rho_s}\right)\rho_f g - F_R$$

So,  $F_R$  is a drag force. So, drag force as I mentioned it is related to the unit kinetic energy per unit volume.

$$F_R = AKC_D$$

So, A is the cross-sectional area and K is the characteristic kinetic energy per unit volume and  $C_D$  is nothing but the drag coefficient.

$$K = \frac{1}{2}v_t^2 \rho_g$$

So, if I take one volume unit volume of the fluid, so v into rho g, so, that is equal to mass of the fluid and then  $\frac{1}{2}mv^2$  that is kinetic energy of the fluid. So, this is the expression of K and the expression of A, A is a particle is falling from this so, we will be taking the cross-sectional area here, so this cross-sectional area is A.

$$A = \pi r^2 = \frac{\pi d^2}{4}$$

so this is our A the K expression we have described, if we put the value of A and K in this  $F_R$  and also put the values of this  $F_R$  here in this expression and put  $m_{aE}$  equal to 0 then we will be getting the value of  $V_t$ . say in this case what is  $F_R$ .

$$F_R = mg - \left(\frac{m}{\rho_s}\right) \rho_f g$$

$$mg \left[1 - \frac{\rho_f}{\rho_s}\right] = F_R$$

So, if we are interested to convert this m in terms of volume, because, you know we cannot measure the weight, we do not need to measure the mass, but dp is known to us so, we can get the volume. So, accordingly mass can be converted to this volume.

$$\left\{\frac{\pi d^3}{6}\right\} \rho_s g \left[1 - \frac{\rho_f}{\rho_s}\right] = F_R$$

If we consider it the particle as a spherical particle.

So, when you will be considering the particle as a spherical particle, so, this expression will be like this so here  $F_R$  value will be putting like  $AKC_D$  and A value is given here, K value is given here we will put this expression here, so by we arranging will be getting the value of  $V_t$

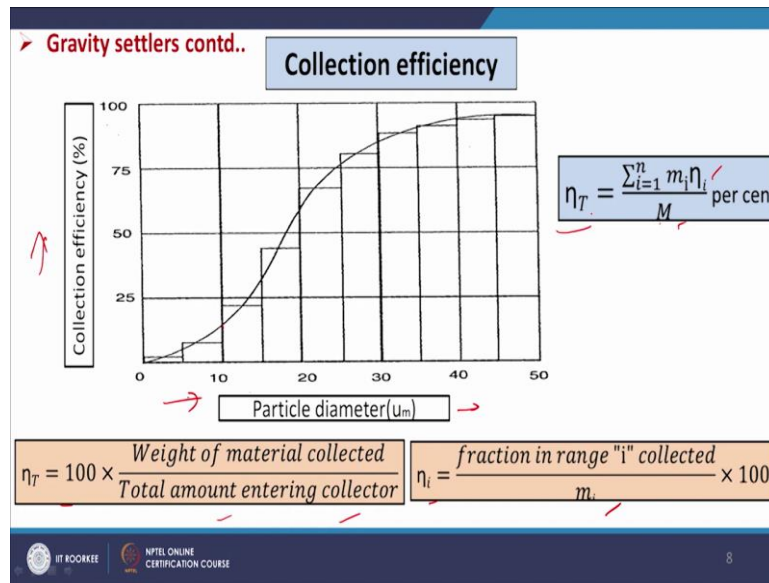
$$v_t = \sqrt{\frac{4gd_p(\rho_p - \rho_g)}{3C_D \rho_g}}$$

So,  $V_t$  is the terminal velocity within the particle and liquid and the fluid in this case that is air. Now, we are able to understand, how the particle will be separated in the gravity settler



and how the  $V_t$  value can be calculated. Now, how the collection efficiency can be calculated, because you know, the more the particle size, more will be the terminal settling velocity less will be the time requirement. So, the time required to travel from inlet to outlet within this time all particle size will not be equally settled, so bigger the particle more easily settle, lighter the particle it will be lesser settled, so we can get one cumulative analysis.

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And if we say x axis if we plot the particle diameter and y axis if we write the collection efficiency, we will see that when the particle diameter is less, the collection efficiency will be less, gradually it will increase cumulatively when we can get the maximum collection efficiency when we will be considering the particle size in the higher range, so that way physically it is happening.

So, now mathematically if we want to express then we can write that

$$\eta_T = 100 \times \frac{\text{Weight of material collected}}{\text{Total amount entering collector}}$$

$$\eta_T = \frac{\sum_{i=1}^n m_i \eta_i}{M}$$

$$\eta_i = \frac{\text{fraction in range "i" collected}}{m_i} \times 100$$

So, that way we can calculate the collection efficiency by using this formula. Now, we will see one numerical problem.

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➤ Gravity settlers contd..

Dust size	Weight per 100 g of dust	Fractional efficiency $\eta_i$ (%)
<5	2	1
5-10	2	7
10-15	4	16
15-20	7	44
20-25	10	67
25-30	8	81
30-35	7	88
35-40	10	92
40-50	15	93
50-60	20	95
60-70	10	98
>70	5	100

$m_i = \frac{2}{100}$

The following table shows the size distribution of a dust sample and the fraction efficiency of removal in a gas cleaning equipment calculate the overall collector efficiency.

So, the following table shows the size distribution of a dust sample and the fraction efficiency of removal in a gas cleaning equipment, calculate the overall collector efficiency. So, this table is giving so, dust size less than 5 and then weight per 100 gram of dust equal to 2 gram and then fractional efficiency is given that is 1.

Similarly, for 5 to 10 it is 2 and it is 7 and 10 to 15 it is 4 and 16. So, 15 to 20 is 7 and 44. So, 20 to 25, 10 and 67 and 25 to 30, 8 and 81 and 30 to 35, 7 and 88 and 35 to 40, 10 and 92 and 40 to 50, 15 and 93 and 50 to 60 that is 20 and 95 and 60 to 70, 10 and 98 and greater than 70, 5 and 100. So, we are getting this is the data given to us we need to calculate the collection efficiency.

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➤ Gravity settlers contd..

$$\eta_T = \frac{\sum_{i=1}^n m_i \eta_i}{M} \text{ per cent} = \sum_{i=1}^n \omega_i \eta_i$$

Where  $\omega_i$  is the weight fraction in each size range.

$$\eta_T = \sum_{i=1}^n \omega_i \eta_i = \frac{(0.02 \times 1) + (0.02 \times 7) + (0.04 \times 16) + (0.07 \times 44) + (0.1 \times 67) + (0.08 \times 81) + (0.07 \times 88) + (0.1 \times 92) + (0.15 \times 93) + (0.2 \times 95) + (0.1 \times 98) + (0.05 \times 100)}{1} \eta_T = 80.17 \%$$

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➤ Gravity settlers contd..

Dust size	Weight per 100 g of dust	Fractional efficiency $\eta_i$ (%)
<5	2	1
5-10	2	7
10-15	4	16
15-20	7	44
20-25	10	67
25-30	8	81
30-35	7	88
35-40	10	92
40-50	15	93
50-60	20	95
60-70	10	98
>70	5	100

$w_i = \frac{m_i}{M}$

The following table shows the size distribution of a dust sample and the fraction efficiency of removal in a gas cleaning equipment calculate the overall collector efficiency.

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So, how we will do it we have the formula

$$\eta_T = \frac{\sum_{i=1}^n m_i \eta_i}{M} \text{ percent} = \sum_{i=1}^n w_i \eta_i$$

$w_i$  is the weight fractions in each size range, so, mass fraction and weight fraction both are same.

So, we have to find out the  $w_i$  value,  $w_i$  is nothing but  $m_i/M$ .

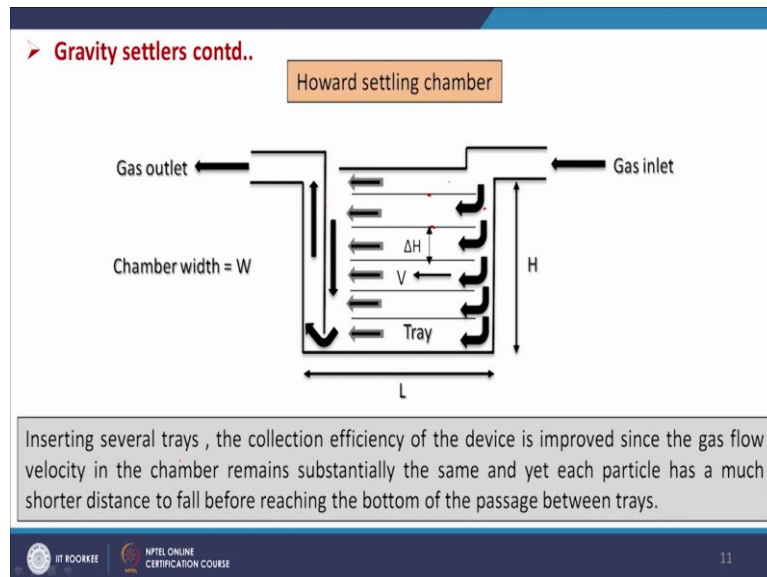
$$\eta_T = \sum_{i=1}^n w_i \eta_i = (0.02 \times 1) + (0.02 \times 7) + (0.04 \times 16) + (0.07 \times 44) + (0.1 \times 67) + (0.08 \times 81) + (0.07 \times 88) + (0.1 \times 92) + (0.15 \times 93)$$

$$+(0.2 \times 95) + (0.1 \times 98) + (0.05 \times 100)$$

$$\eta_T = 80.17 \%$$

Now, in practice, you know, if we can reduce the height for the separation, then more separation is possible.

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So, if we have like this figure, if this is our height in this height, if we place some horizontal trays, so in between inter tray distance will be reduced. So, air will pass through it. So, particle need to travel vertically from this point to this point, when in the same time when it is moving from inlet to outlet, but we do not put any internal share or any plates inside. So, then the particle has to remove from this to this the complete H height during the time when it will travel the length.

So, by inserting these plates, we are reducing them vertical length for travel by the particles. So, more separation is possible. So, inserting several trays, the collection efficiency of the device is improved since the gas flow velocity in the chamber remains substantially the same and yet each particle has a much shorter distance to fall before reaching the bottom of the passage between trays.

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➤ Gravity settlers contd..
Design concept

For a settling chamber having dimension  $L \times W \times H$  and  $n$  number of trays including the bottom surface. The hydraulic diameter for flow passage between the trays is:

$$D_h = \frac{2W\Delta H}{W + \Delta H} \quad \text{and} \quad Re = \frac{vD_h\rho_g}{\mu_a}$$

Where,  $v$  is velocity in the chamber and  $Q$  is the volumetric flow rate of the gas stream.  $v = \frac{Q}{nW\Delta H}$

Substituting for  $v$  and  $D_h$ ,  $Re = \frac{2Q\rho_g}{n\mu_a(W + H)}$  The spacing between the trays,  $\Delta H$ , is given by



Assuming there is no dust initially on tray, substituting for  $\Delta H$   $\Delta H = \frac{H}{n}$

If a layer of dust  $H_d$  is initially present, then

$$\Delta H = \frac{H}{n} - H_d$$

$$Re = \frac{2Q\rho_g}{\mu_a(nW + H)}$$

With this modification,  $Re = \frac{2Q\rho_g}{\mu_a(nW + H - nH_d)}$



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So, in this case what will be the mathematical expression that we are going to discuss. So, for a settling chamber having dimension  $L, W, H$ . So,  $L$  is the length. So,  $W$  is the width and this  $H$  is our height. So, in that case and  $n$  number of trays, including the bottom surface, the hydraulic diameter for flow passage between the trays is then if I want to calculate the hydraulic diameter that is

Hydraulic diameter =  $4 \times \text{Area (A)} / \text{Perimeter}$ .

So in these cases this is our  $W$  and  $\Delta H$  this side. Air is flowing from this direction, so this will be our surface area, so,  $W \times \Delta H$ .

$$W \times \Delta H = A$$

$$\text{Hydraulic diameter} = (4 \times W \times \Delta H) / 2(W + \Delta H)$$

$$D_h = \frac{2W\Delta H}{W + \Delta H}$$

We will be getting the Reynolds number we know that

$$Re = \frac{\rho v d}{\mu} = \frac{v D_h \rho_g}{\mu_a}$$

So,  $D$  will be this characteristic diameter that is  $D_h$  and  $V$  is the velocity in the chamber. So now, if we want to get the value of  $V$  in terms of the known dimension that is  $W$  and  $\Delta H$  then we can calculate

$$v = \frac{Q}{nW\Delta H}$$

where Q is the volumetric flow rate of the gas stream, n is the number of that channel. So, if we put this value v here so,

$$Re = \frac{2Q\rho g}{n\mu g(W+H)}$$

Now, when we do not have any interval, but if we have some, we have some plates and intervals then  $\Delta H$  is equal to  $H/n$ .

$$\Delta H = \frac{H}{n} - H_d$$

If there is no layer initially at the bottom of the any layer any plate then  $H_d$  will be 0

$$\Delta H = H/n$$

$$Re = \frac{2Q\rho g}{\mu g(nW+H)}$$

$$Re = \frac{2Q\rho g}{\mu g(nW+H-nH_d)}$$

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➤ Gravity settlers contd..

For laminar flow conditions ( $Re < 2300$ ) within the trays, particles of size  $d_p$  of a particular material will settle a distance  $y$  with a terminal velocity  $v_t$  in time  $t$ . During this time the particles are transported a distance  $L$  with the velocity of the gas stream.

Equating these two, we have  $\frac{y}{v_t} = \frac{L}{v}$   $\checkmark$   $y = \frac{Lv_t}{v}$

The value of  $y$  can be found from a knowledge of the particle settling velocity. If the particles are uniformly distributed over the incoming stream, the efficiency of collection  $\eta = y / \Delta H$  or

$$\eta = \frac{Lv_t}{v\Delta H} = \frac{nWLv_t}{Q}$$

When  $y \geq \Delta H$ , all particles of that size (or larger) will be collected in the settling chamber

Force balances on a falling particle

$$F = C_D \left( \frac{\pi}{4} d_p^2 \right) \left( \frac{1}{2} \rho_g v_t^2 \right) = \frac{\pi}{6} d_p^3 (\rho_p - \rho_g) g$$

Or  $v_t = \sqrt{\frac{4g d_p (\rho_p - \rho_g)}{3C_D \rho_g}}$

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Now, we are assuming that the flow is laminar, but in reality it may not be laminar and it is very difficult to be laminar. So, which we are assuming that will not these expressions will not hold good and there needs some modification. So, for laminar flow conditions within the trays particles of size  $D_p$  of a particular material will settle a distance  $\Delta y$  with a terminal velocity  $V_t$  in time  $t$ , during this time the particles are transported a distance  $L$  with the velocity of the gas stream.

$$\frac{y}{v_t} = \frac{L}{v}$$

Similar expressions we have also had in the previous slide. So,  $y$  is replaced by capital  $H$  in that case, so, now, the value of  $y$  can be found from a knowledge of the particle settling velocity if the particles are uniformly distributed over the incoming stream the efficiency of the collection that  $\eta = y/\Delta H$ . That is very interesting equations or assumptions. So, say number of particles are there and it is falling vertically.

So, from the bottom initially maximum height is  $H$  and then it is falling. So, when the particles are at the bottom that will be certainly removed, but those particles at the top may not be able to come to the bottom so, may not be removed. So, efficiency is depending upon the term  $\Delta H$  term and the  $y$  value the distance through which the particle will travel during this time. So, that  $y/\Delta H$  this value is your efficiency.

So, now efficiency is equal to

$$\eta = \frac{Lvt}{v\Delta H} = \frac{nWLvt}{Q}$$

So, when  $y$  is greater than  $\Delta H$ , then all particles of the size are larger will be collected in the settling chamber and the force balance already we have discussed that

$$v_t = \sqrt{\frac{4gd_p(\rho_p - \rho_g)}{3C_D\rho_g}}$$

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➤ Gravity settlers contd..

Where  $C_D$  is the drag coefficient which is related to the particle Reynolds number  $Re = \frac{d_p \rho_g v_t}{\mu_g}$

The general drag coefficient curve for spherical particle may be presented by three relationship. In the Stokes law region  $C_D = 24/Re_p < 1$

In the turbulent region ( $Re_p > 1000$ ) the drag coefficient  $C_D$  become almost constant with a value of 0.45,  $C_D = 0.45$  For  $Re_p > 1000$

For the transition region several empirical equation have been suggested for this region such as the Given by Schiller and Naumann:

$$C_D = \frac{24}{Re_p} (1 + 0.15 Re_p^{0.687})$$

$d_p = \sqrt{\frac{18\mu_g v_t}{g(\rho_p - \rho_g)}}$

For stock's law region  $v_t = \frac{gd_p^2(\rho_p - \rho_g)}{18\mu_g}$

and minimum particle diameter can be separated  $d_{p,min} = \sqrt{\frac{18Q\mu_g}{nWL_g(\rho_p - \rho_g)}}$   $\eta = 1$

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➤ Gravity settlers contd..

For laminar flow conditions ( $Re < 2300$ ) within the trays, particles of size  $d_p$  of a particular material will settle a distance  $y$  with a terminal velocity  $v_t$  in time  $t$ . During this time the particles are transported a distance  $L$  with the velocity of the gas stream.

Equating these two, we have  $\frac{y}{v_t} = \frac{L}{v}$   $\checkmark$   $y = \frac{Lv}{v_t}$

The value of  $y$  can be found from a knowledge of the particle settling velocity. If the particles are uniformly distributed over the incoming stream, the efficiency of collection  $\eta = y / \Delta H$  or

$$\eta = \frac{Lv_t}{v\Delta H} = \frac{nW Lv_t}{Q}$$

When  $y \geq \Delta H$ , all particles of that size (or larger) will be collected in the settling chamber

Force balances on a falling particle

$$F = C_D \left( \frac{\pi}{4} d_p^2 \right) \left( \frac{1}{2} \rho_g v_t^2 \right) = \frac{\pi}{6} d_p^3 (\rho_p - \rho_g) g \quad \text{Or} \quad v_t = \sqrt{\frac{4g d_p (\rho_p - \rho_g)}{3 C_D \rho_g}}$$



And where  $C_D$  is the drag coefficient which is related to the particle Reynolds number and particle Reynolds number

$$Re = \frac{\rho v d}{\mu} = \frac{d_p \rho_g v_t}{\mu_g}$$

Now, the general drag coefficient curve for spherical particle may be presented with three relationships if we see the drag coefficient, so drag coefficient value will change with the Reynolds number.

If it is laminar flow, then Reynolds number is less so, in that case  $C_D$  it is equal to  $24/Re_p$  when  $Re_p$  is less than 1. And when the turbulent region that is  $Re_p$  greater than 1000, then again  $C_D$  is equal to 0.45 or somewhere it is 0.44. For the transition region, several empirical equations have been suggested. And one is here

$$C_D = \frac{24}{Re_p} (1 + 0.15 Re_p^{0.687})$$

So, if we consider the Stokes law, so

$$v_t = \frac{g d_p^2 (\rho_p - \rho_g)}{18 \mu_g}$$

Then what is the minimum particle diameter that can be separated from this expression we can get

$$d_{pmin} = \sqrt{\frac{18 Q \mu_g}{n W L g (\rho_p - \rho_g)}}$$

In this case,  $\eta$  is equal to 1. So, that is why we are getting this expression.



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**➤ Gravity settlers contd..**

Although the efficiency relationship is based on laminar flow conditions within the unit, it is practically impossible to achieve laminar conditions without a very large particle size or an inordinately large number of trays combined with an awkward shape of the chamber. Hence, the flow in the settling chamber will probably be turbulent rather than laminar.

**Turbulent flow**

Gas flow is totally mixed in y direction and no mixing in x direction.

Gravity settling in a horizontal duct : turbulent flow

$$\left( \text{Mass concentration of particles entering the elemental volume } (A dx) \right) = \left( \text{Mass concentration of particles leaving the elemental volume } (A dx) \right) + \left( \text{Rate at which particles are deposited within the volume } (A dx) \right)$$

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Now, although the efficiency relationship is based on laminar flow conditions within the unit, it is practically impossible to achieve laminar conditions, so, there will be some turbulence. So, there will be some variation as we have mentioned, now let us see, we have the velocity of the gas stream as  $v$  and it is going through this chamber and we are considering a small volume and this is the distance  $dx$ .

So, in this case if we get the mass balance,

$$\left( \text{Mass concentration of particles entering the elements volume } (A * dx) \right) = \left( \text{Mass concentration of particles leaving the elements volume } (A * dx) \right) + \left( \text{Rate at which particles are deposited within the elements volume } (A * dx) \right)$$

So, this is the mass balance of the particles.

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➤ Gravity settlers contd..

$$cAv = (c + dc) Av + cv_t W dx \quad A = W\Delta H$$

Thus,

Where, c is mass concentration of particles and

Rearranging and integrating  $\int_{c_{in}}^{c_{out}} \frac{dc}{c} = -\frac{v_t W}{Av} \int_0^L dx$  Or  $\ln \frac{c_{out}}{c_{in}} = -\frac{v_t WL}{Av}$

The efficiency  $\eta = 1 - \frac{c_{out}}{c_{in}}$  Or  $\eta = 1 - \exp\left[-\frac{nWLv_t}{Q}\right]$

Thus  $\eta_{turb} = 1 - \exp(-\eta_{laminar})$



$$cAv = (c + dc) Av + cv_t W dx, \quad A = W\Delta H$$

Where, c is mass concentration of particles and

$$\int_{c_{in}}^{c_{out}} \frac{dc}{c} = -\frac{v_t W}{Av} \int_0^L dx \quad \text{or} \quad \ln \frac{c_{out}}{c_{in}} = -\frac{v_t WL}{Av}$$

Now, if I want to get the efficiency.

$$\eta = 1 - \frac{c_{out}}{c_{in}} \quad \text{or} \quad \eta = 1 - \exp\left[-\frac{nWLv_t}{Q}\right]$$

$$\eta_{turb} = 1 - \exp(-\eta_{laminar})$$

So, laminar conditions if we can find out the efficiency of collection that can be converted into turbulent conditions by using this expression. So, these are the different mathematical expressions which can be used to calculate the efficiency for the separation of the particles, up to this in this class. Thank you very much for your patience.