

Course on Integrated Waste for a Smart City
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Module 12
Tutorial I

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Tutorial 1

Question No. 1

Determine the amount of air supply required to compost 1 tonne of the MSW using an in-vessel composting system with forced aeration. Oxygen demand for the successive days of the 5-day composting period days

Days	1	2	3	4	5
%	20	35	25	15	5

The ammonia produced during the aerobic degradation of the MSW is lost to the atmosphere. Air contains 23% of oxygen by mass and the specific weight of air is equal to 1.29 kg/m³. A safety factor of 2 has to be considered for the actual air supply. Chemical formula to be used is C₇₄H₁₁₄O₄₄N.

Assume:

- Moisture content of the organic fraction of MSW = 25%,
- Volatile solids, VS = 93% of total solids,
- Biodegradable volatile solid, BVS = 60% of VS,
- Expected BVS conversion efficiency = 95%,
- Composting time = 5 d.

Welcome to the NPTEL course on integrated waste management for smart city. So we will be doing a tutorial on the air calculations and anaerobic digestion and incineration in this session. Now we will just look into the question number one, so we will to determine the amount of air supply required to compost 1 ton of municipal solid waste using an in-vessel composting system with forced aeration.


So the oxygen demands for the successive days of the 5 day composting periods have been provided in this table. The ammonia produced during the aerobic digestion degradation of MSW is lost to the atmosphere and air contains 23 percent of oxygen by mass and the specific weight of the air is equal to 1.29 kg per metre cube. The safety factor of 2 has to be considered for the actual air supply.

And the chemical formula to be used is given over here and we will be assuming moisture content of the organic fraction of the municipal solid waste is 25 percent, the volatile solids is 93 percent of the total solids, and biodegradable volatile solid BVS fraction is 60 percent of the volatile solids, and expected BVS conversion efficiency is 95 percent, the composting time is the 5 days.

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Solution



- **Total Mass of biodegradable Volatile solids in one tonne of MSW**
$$\text{BVS} = 1.0 \text{ ton} \times 1000 \text{ kg} \times 0.75 \text{ (dry matter content)} \times 0.93 \times 0.60$$
$$= 418.5 \text{ kg}$$
- **Expected BVS conversion**
$$= 418.5 \text{ kg} \times 0.95 = 397.58 \text{ kg}$$



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→ $1 \text{ ton} \times 1000 \text{ kg} \times \frac{0.75}{\downarrow \text{dry matter}} \times \frac{0.93}{\downarrow \text{BVS}} \times 0.60 = 418.5 \text{ kg}$

→



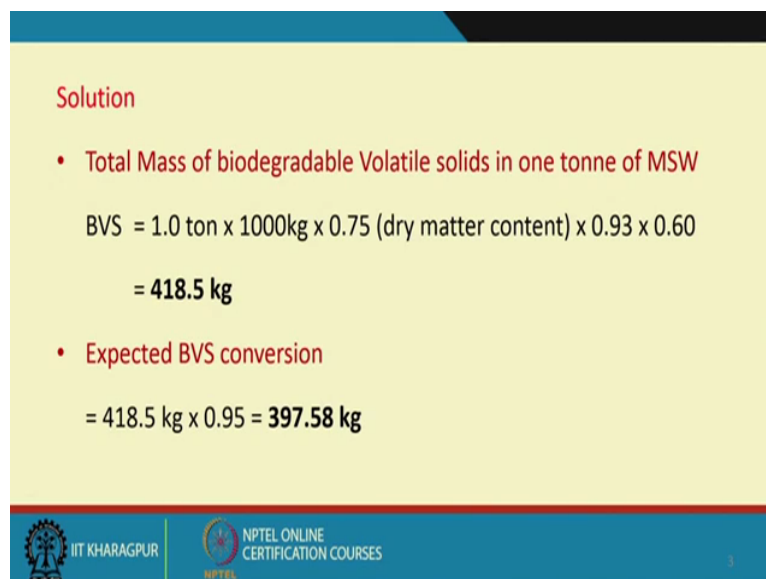
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And come to the solution, the initial step of solution we have to calculate the total mass of biodegradable volatile solids in 1 ton of municipal solid waste. So here the 1 ton, so we have one ton so when we are converting it to the KG, it will be 1000 KG so multiplied by the 0.75, this 0.75 has been arrived from the moisture content determination.

So we have 25 percent moisture in the municipal solid waste. So we will if we just see here the moisture content of the organics fraction of municipal solid waste is 25 percent, so 100 minus 25 percent is the 75 percent which is the dry fraction, dry matter or content, dry matter so that multiplied by 0.93. The 0.93 is the volatile solids content and multiplied by point 60 which is the BVS fraction, so total it will be 418.5 KG.

So next we have to determine the expected BVS conversion factor, so the expected BVS converts fraction is the actual biological volatile solids that what we are going to get in our study. So here we are given the expected BVS conversion efficiency is 95 percent.

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Solution

- **Total Mass of biodegradable Volatile solids in one tonne of MSW**
$$\text{BVS} = 1.0 \text{ ton} \times 1000\text{kg} \times 0.75 \text{ (dry matter content)} \times 0.93 \times 0.60$$
$$= 418.5 \text{ kg}$$
- **Expected BVS conversion**
$$= 418.5 \text{ kg} \times 0.95 = 397.58 \text{ kg}$$

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$$\rightarrow 1 \text{ ton} \times 1000 \text{ kg} \times \underset{\substack{\downarrow \\ \text{dry matter}}}{0.75} \times \underset{\substack{\downarrow \\ \text{BVS}}}{0.93} \times 0.60 = 418.5 \text{ kg}$$

$$\rightarrow 418.5 \times 0.95 = \underline{\underline{397.58 \text{ kg}}} \text{ [Expected BVS Content]}$$


So now take the 418.5 KG the total mass of biodegradable volatile solids multiplied by 0.95 we will get the actual content that is 418.5 into 0.95 which is giving is to 397.58 KG which is the expected BVS content, so we will be using this value in our calculations. So in the examinations we request all the students to go for the 2 decimals percussions.

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- The amount of oxygen required for aerobic decomposition of 1 tonne of MSW containing 397.58 kg of BVS can be estimated using the following equation



$$C_aH_bO_cN_d + \left(\frac{4a+b-2c+d}{4}\right)O_2 \longrightarrow aCO_2 + \left(\frac{b-3d}{2}\right)H_2O + dNH_3$$

For the known chemical formula $C_{74}H_{114}O_{44}N$:

$a = 74, b = 114, c = 44, d = 1$; i. e. the chemical equation for this case will be

$$\begin{array}{ccc} C_{74}H_{114}O_{44}N + 80.75O_2 & \longrightarrow & 74CO_2 + 55.5H_2O + NH_3 \\ \begin{array}{cc} 1720 & 2584 \end{array} & & \begin{array}{ccc} 3256 & 999 & 17 \end{array} \end{array}$$

Oxygen requirement = $\frac{2584}{1720} \times (397.58 \text{ g}) = 597.29 \text{ kg}$

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Now we will be calculating the oxygen required, so the amount of oxygen required for an anaerobic decomposition of 1 ton of municipal solid waste container 397.58 KG of BVS can be estimated using the following equation. So in the PowerPoint presentation we can just see the equation which has been developed over here and it has been taken from the standard literature and textbooks.

So in this already the Ca Hb Oc Nd is the chemical formula and we have been already provided with the chemical formula $C_{74}H_{114}O_4N$, so where the a will become 74, and b is equal to 114, and c is equal to 44, and d is equal to 1. So the chemical equation for the case will be written in the format where we will the molecular weight of the given chemical is 1720 and for the oxygen we calculated 4 a plus b minus 2 c plus d divided by 4 we will get the molecular weight of oxygen 80.75 molecules is 2584.

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$$\rightarrow 1 \text{ ton} \times 1000 \text{ kg} \times \underset{\substack{\downarrow \\ \text{dry matter}}}{0.75} \times \underset{\substack{\downarrow \\ \text{BVS}}}{0.93} \times 0.60 = 418.5 \text{ kg}$$

$$\rightarrow 418.5 \times 0.95 = \underline{\underline{397.58 \text{ kg}}} \text{ [Expected BVS Content]}$$

$$\rightarrow \text{Oxygen requirement} = \frac{2584}{1720} (397.58 \text{ kg}) = \underline{\underline{597.29 \text{ kg}}}$$

Now the oxygen requirement is oxygen requirement is equal to 2584 divided by 1720 into 397.58 KG, which is equal to 597.29 KG, so we required 597.29 KG of oxygen. And now we have to calculate the amount of oxygen, after calculating the total amount of oxygen will calculate the total amount of air required for 1 ton on the municipal solid waste.

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- The total amount of air required for one tonne of MSW

$$\text{Volume of air} = \frac{597.29 \text{ kg} \times 2(SF)}{0.23(\%O_{2,air}) \times 1.2928 \text{ kg/m}^3 (\rho_{air})} = 4,017 \text{ m}^3$$

Variable Pump is required for the composting process

- Air supply of the aeration system = $4017 \times 0.35 \text{ m}^3/\text{day}$ (Consider critical day demand)

Ans = 1406 m³ /day

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And we have been given that the air supply of the aeration system for 0.53 that is where we are taking the day 2, so here the day 2 has been considered to be the critical. So that percentage will be 35 percent, so we will multiply the air supply of the aeration required for the critical demand.

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$$\begin{aligned} \rightarrow & 1 \text{ ton} \times 1000 \text{ kg} \times \underset{\substack{\downarrow \\ \text{dry matter}}}{0.75} \times \underset{\substack{\downarrow \\ \text{BVS}}}{0.93} \times 0.60 = 418.5 \text{ kg} \\ \rightarrow & 418.5 \times 0.95 = \underline{\underline{397.58 \text{ kg}}} \text{ [Expected BVS content]} \\ \rightarrow & \text{Oxygen requirement} = \frac{2584}{1720} (397.58 \text{ kg}) = \underline{\underline{597.29 \text{ kg}}} \\ \rightarrow & \text{Volume of air} = \frac{597.29 \text{ kg} \times \text{Safety factor (2)}}{0.23(\%O_2 \text{ Air}) \times 1.2928 \text{ kg/m}^3} = 4017 \text{ m}^3 \\ \rightarrow & \text{CRITICAL DEMAND} = 4017 \times 0.35 (\text{m}^3/\text{day}) = (1406 \text{ m}^3/\text{day}) \end{aligned}$$

So the critical demand the air required is equal to 4017 multiplied by 0.35 meter cube per day, which is arriving to 1406 meter cube per day. And now we will just look in to the next numerical, that is anaerobic digester is to be designed for a dairy farm; the dairy farm has 12 cows. Assume each cow producing 10 KG of dung daily, the Cow dung from all the cows.

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- The total amount of air required for one tonne of MSW

$$\text{Volume of air} = \frac{597.29 \text{ kg} \times 2(SF)}{0.23(\%O_{2,air}) \times 1.2928 \text{ kg/m}^3 (\rho_{air})} = 4,017 \text{ m}^3$$

Variable Pump is required for the composting process

- Air supply of the aeration system = $4017 \times 0.35 \text{ m}^3 / \text{day}$ (Consider critical day demand)

Ans = 1406 m³ /day

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Now we will design an anaerobic digester, an anaerobic digester is to be designed for a dairy farm, the dairy farm has 12 cows. Assume each cow producing 10 KG of dung daily. The cow dung from all the cows is available to the feedstock this is the assumption. Assume the temperature is 30 centigrade, and the solid content of the cow dung is 15 percent and hydraulic retention time HRT is 45 days for the anaerobic digester.

And Determine the total volume of the digester for the present case and then the diameter of the digester, the height of the digester. It is the wall here we are use the formula V_3 that is the volume of cylindrical portion V_3 of the digester can be computed by this formula. In the examination we will be providing this formula.

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Solution

a) The total volume (V) of the digester for the present case


- Total discharge = $10 \text{ kg} \times 12 = 120 \text{ Kg/day}$
- Total Solids of fresh discharge = $120 \text{ kg} \times 0.15 = 18 \text{ Kg}$.

In 8% concentration of Total Solids (To make favourable condition)

8 Kg. Solid	=	100 Kg. Influent
1 Kg. Solid	=	$100 / 8 \text{ Kg. Influent}$
18 Kg. Solid	=	$100 \times 18 / 8 = 225 \text{ Kg. Influent.}$

- Total influent required = 225 Kg

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Now we will be calculating the total volume of the V of the digester for the present. Here the total discharge is 10 KG of the cow dung that is arriving from the 12 cows which is 120 KG per day. And the total solids of fresh discharge be 0.15 percent that is 120 KG into 0.15 which is equal to 18 KG. And to have the favourable condition we will have 8 percent concentration of the total solids. So now in the 8 KG of solids is equal to 100 KG influent, so 1 KG will be 100 divided by 8 KG of the influent and for the 18 KG's, it will be 100 into 18 by 8 which is equivalent to 225 KG of the influent. So the total influent that is required is 225 KG.

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- Water to be added to make the discharge 8% concentration of TS**
 $= 225 \text{ Kg} - 120 \text{ Kg} = 105 \text{ Kg}.$
- Working volume of digester** $= V_g + V_d * V_g + V_d = Q \times \text{HRT}$
 $= 225 \text{ Kg/day} \times 45 \text{ days} = 10125 \text{ kg} (1000 \text{ kg} = 1\text{m}^3)$
 $= 10.125 \text{ m}^3$
- From geometrical assumptions:**
 $= V_g + V_d = 0.80 V$
 $= V = 10.125 / 0.8$

Ans = 12.65 m³

Vc is gas collection volume
 Vg is gas storage volume
 Vd is active digestion volume
 Vs is sludge layer volume

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So now the water to be added to make the discharge 8 percent concentration of the total solids we have to check out. It is 225 KG minus the 120 KG so which is equivalent to 105 KG, so this is the total amount of water to be added to make the discharge of 8 percent concentration of total solids.

Now to determine the working volume of the digester, so in the diagram you can see the different portion of the digester, where Vc is the gas collection volume. So in after the digestion process once the gas is been generated it will be collected in the Vc, and Vg is the gas storage volume and Vd is the active digestion volume and Vs is the sludge layer volume.

So in the anaerobic digestion process once the active digression volume, the municipal solid waste will undergo the degradation process like hydrogenises, acitogeogenesis and methenogenesis and we will get the gas and the sludge. The sludge will be stored in the sludge layer volume and the gas will be stored in the gas storage volume and it will be collected from the collection volume area.

Now we are interested in calculating the working volume which is equivalent to the volume of the active digestion volume V_d plus V_g that is the gas storage volume, so which is equivalent to the flow into the hydraulic retention time. So the flow Q is equal to 225 KG per day and the hydraulic retention time is provided to be the 45 days, so multiplying this will get 10,125 KG and when we are converting it to metre cube, 1000 KG is equal to 1 meter cube, which is equivalent to 10.125 meter cube.

And for the geometrical we are taking V_g plus V_d is equal to 0.8 of the total volume. We can see from the diagram even the V_g and V_d will be covering 80 percent of the anaerobic digester. So the geometrical assumption that means the construction process we have to take that portion geometrical assumption which is equivalent to 0.8 of the total volume. So the V is equal to 10.125 divided by 0.8 which is coming to 12.65 meter cube. So this is the volume of the anaerobic digester.

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b) **Diameter of the digester**

$$D = 1.3078 V^{1/3} = 1.3078 * (12.65 \text{ m}^3)^{1/3}$$

Ans = 3.05 m

c) **Height of the digester** ($V_3 = 3.14 * D^2 * H / 4$)

Putting $V_3 = 0.3142D^3 = 8.89 \text{ m}^3$

$$3.14 \times D^2 \times H / 4 = 0.3142D^3$$

$$H = (4) \times (0.3142) \times (3.05 \text{ m}) / 3.14$$

Ans = 1.22 m

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Now we will calculate diameter of the digester, so the diameter of the digester can be directly collected from the formula $1.3078 V^{1/3}$ raise to the volume raise to the power of 1 by 3. So the volume has already been calculated from the previous slide that is 12.65 m cube, so simply substituting this into the given formula, 1.3078 multiplied by 12.65 metre cube raise to the power of 1 by 3, we will get the diameter which is equivalent to 3.05 meter.

Now we will calculate the height of the digester, so for calculating the height of the digester we have V_3 is equal to 3.14 into D^2 into H divided by 4 that is height divided by 4. So

putting the V_3 value which has been given as 0.3142 D cube is equivalent to 8.89 meter cube. We will calculate the substituting this we will get the height of the digester as 1.22 meter.

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Question No. 3

The Kolkata City operates a state-of-the-art volume reduction incinerator with a rocking kiln. It is currently handling 400 tonnes (dry basis) of semi-sorted waste per day. That is, the majority of glass and metals are sorted out through central depots. However, paper is left in the waste stream to maintain the required energy. Local authorities feel that not separating out the paper gives a poor environmental image. As such they propose a source separation model that removes 40% of the paper content before incineration. Neglecting the costs of collection (which will be significant), what is the price per tonne of paper that they need to receive to offset the cost of purchasing additional gas as a supplement fuel

Given:

• Original mass of paper	= 45%
• Energy content of paper	= 16,300 kJ/kg
• Energy content of natural gas	= 37,300 kJ/m ³
• Cost of natural gas	= Rs. 30 per m ³

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Now we will just calculate the numerical on the incineration. So the Kolkata city operates a state of the art volume reducing incinerator with a working kiln. It is currently handling 400 tons on dry basis of semi-sorted waste per day. And this is the majority of class and metals are sorted out through the central depots. However, paper is left in the waste stream to maintain the required energy. The local authorities feel that not separating out paper gives a poor environmental image. As such they propose a source segregation model that removes 40 percent of the paper content before incineration.

So neglecting the cost of collection which will be significant and what is the price per tonne of paper that they need to receive to offset the cost of purchasing additional gas as a supplement fuel. So in the given data, we have the original mass of paper as 45 percent, energy content of paper is 16300 kilo joule per KG, the energy content of natural gas is 37300 KG per metre cube and the cost of natural gas is rupees 30 per metre cube.

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• **Total mass of paper from the MSW containing 45% of paper**
= $440 \text{ (t/d)} \times 0.45$ = **180 t/d**

• **Energy value from paper**
= $180 \text{ (t/d)} \times 10 \text{ m}^3 \text{ (per t)} \times 16,300 \text{ (kJ/kg)}$ = **$2.93 \times 10^9 \text{ kJ/d}$**

• **Energy lost through separation of 40% of paper content**
= $2.9 \times 10^9 \text{ (kJ/d)} \times 0.4$ = **$1.17 \times 10^9 \text{ (kJ/d)}$**

• **Energy content of the natural gas** = **$37,300 \text{ kJ/ m}^3$**

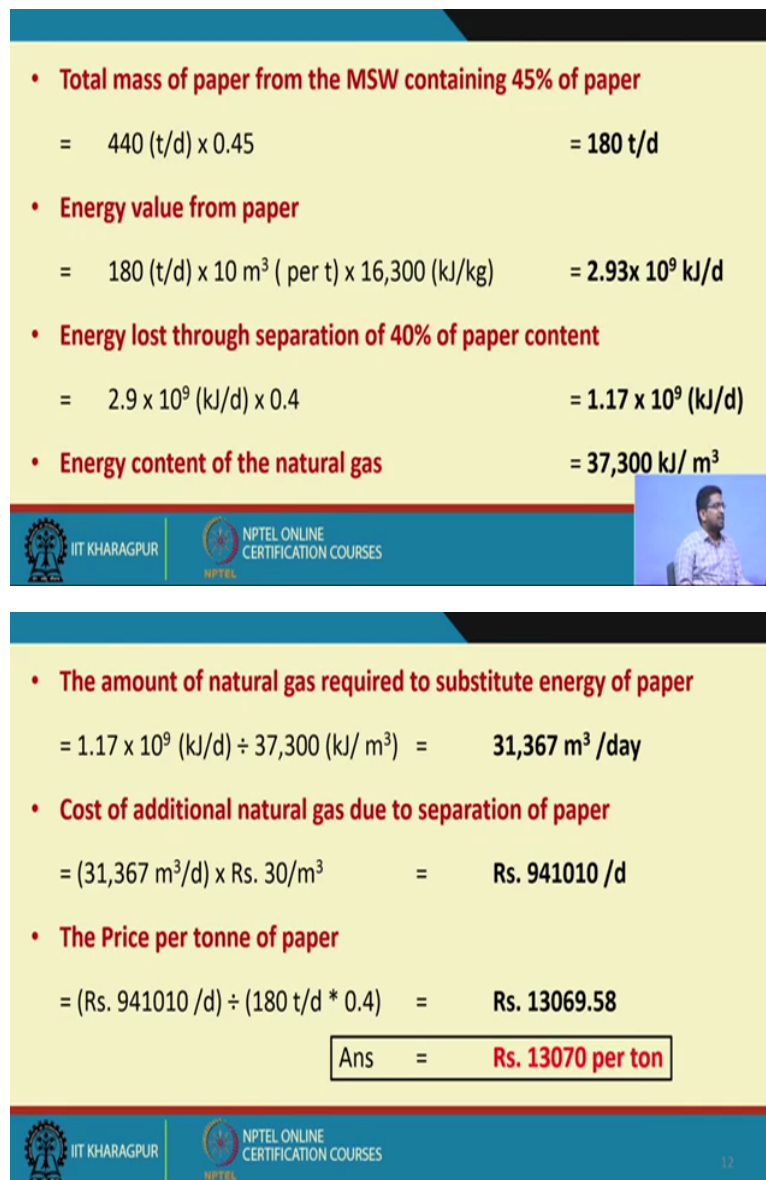
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Now initially we have to calculate the total mass of the paper from municipal solid waste containing 45 percent of the paper. So we are generating 440 tons per day out of which 45 percent that is 0.45 will be the total mass of the paper. So 440 tons per day multiplied by 0.45 we have 180 tons per day.

So the energy value from the paper is 180 tons per day into 10 meter cube per ton to 16300 kilo joule per KG, so which is equal to 2.93 into 10 to the power of 9 KG per day. The total energy value of the paper is 2.93 into 10 to the power of 9 KG per day. The energy lost through separation of 40 percent of the content, since we are segregating the paper, so we have to remove that energy loss.

So it is 2.9 into 10 to the power of 9 kilo joule per day into 0.4, so which is coming to 1.17 into 10 to the power of 9 kilo joule per day. So if we not taking this 10 power 9 in the assignments most of the students are solved with the full-length calculation just like 117346 the value is coming, so we request all the students to take this 2 decimal precision. So it is 1.17 to 10 to the power of 9 or 2.93 for the calculations.

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The slide contains the following calculations:

- Total mass of paper from the MSW containing 45% of paper**
$$= 440 \text{ (t/d)} \times 0.45 = 180 \text{ t/d}$$
- Energy value from paper**
$$= 180 \text{ (t/d)} \times 10 \text{ m}^3 \text{ (per t)} \times 16,300 \text{ (kJ/kg)} = 2.93 \times 10^9 \text{ kJ/d}$$
- Energy lost through separation of 40% of paper content**
$$= 2.9 \times 10^9 \text{ (kJ/d)} \times 0.4 = 1.17 \times 10^9 \text{ (kJ/d)}$$
- Energy content of the natural gas**
$$= 37,300 \text{ kJ/ m}^3$$

The amount of natural gas required to substitute energy of paper:
$$= 1.17 \times 10^9 \text{ (kJ/d)} \div 37,300 \text{ (kJ/ m}^3) = 31,367 \text{ m}^3 \text{ /day}$$

Cost of additional natural gas due to separation of paper:
$$= (31,367 \text{ m}^3/\text{d}) \times \text{Rs. } 30/\text{m}^3 = \text{Rs. } 941010 \text{ /d}$$

The Price per tonne of paper:
$$= (\text{Rs. } 941010 \text{ /d}) \div (180 \text{ t/d} * 0.4) = \text{Rs. } 13069.58$$

Ans = Rs. 13070 per ton

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The energy content of the natural gas from that equation will be you have to calculate, so the total amount of natural gas required to substitute the energy of paper. So the energy of paper is 1.17×10^9 divided by the energy content of the natural gas, so which is equivalent to 31367 meter cube per day.

Now we have to calculate the cost of additional natural gas due to separation of the paper. So for the amount of natural gas required to substitute the energy of paper that is 31367 into the 30 will be the additional cost of the natural gas, so which is equivalent to 941010 rupees per day. So the price per tonne of paper we have to calculate, so the overall ton as 180 tons we are receiving in the paper form, so for the each ton we have to divide this 941010 rupees per

day divided by 180 into 0.4, that is the total paperweight which is arriving to 13069.58, so rounding it off will get 13070 per tonne.

So in the assignment we have been like there are a few calculation mistakes their precision errors have done from our side and your side. We are calculated 2 decimal precision and the total number has been calculated by the students over there, so which is led to different answers. So what we suggest the student is to use the 2 decimal precision. So to arrive this sort of answers even in your examination there are questions of this model, so you just take the 2 decimal precision and calculate to reach the required answers. So all the best for your examinations, thank you.