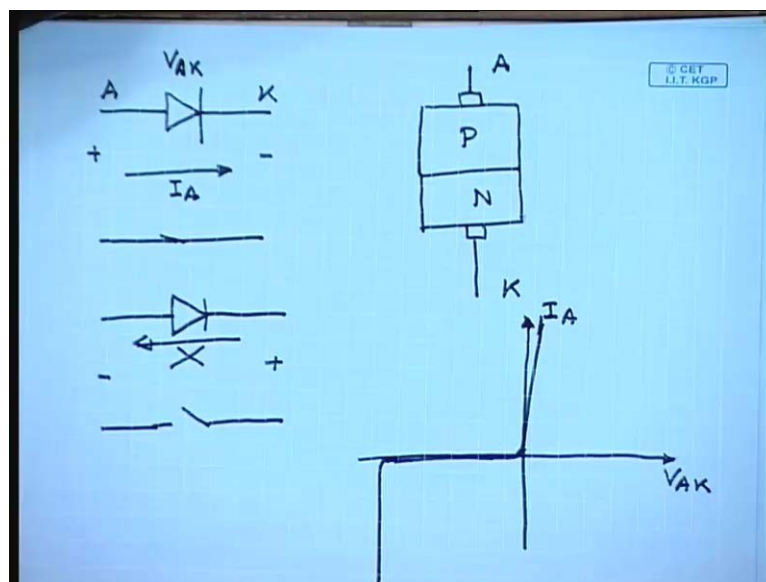


Electrical Machines-I
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Lecture - 34
Electronic Control of DC Shunt Motors

We have seen that in order to use a DC shunt motor, we need separate arrangement for starting it, controlling its speed and stopping it. Now this equipment if we use the conventional equipment is bulky and sometimes also very lossy causing a lot of power loss. Therefore, the modern trend has been to use power electronic devices to control all aspects of operation of a shunt DC motor.

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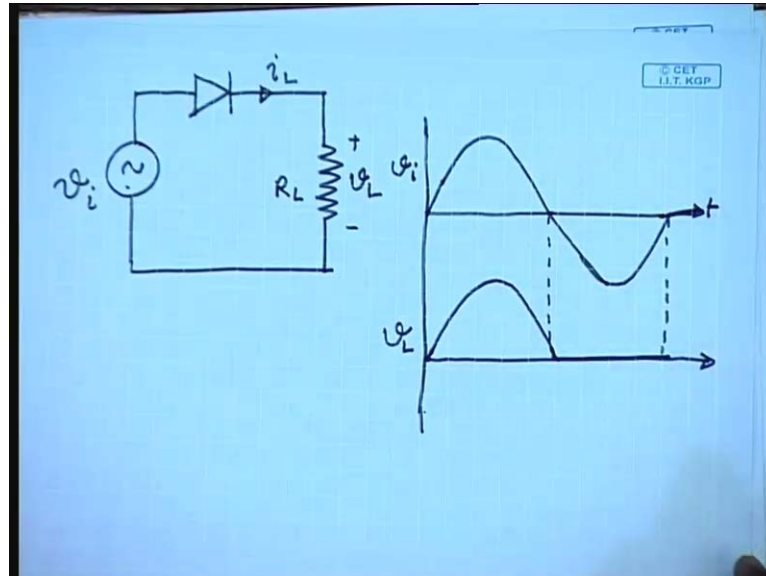


Let us see what are these electronic devices? The first device that is used is a simple diode. As you all know a diode is a PN junction semiconductor device. The characteristics of diode are that if you apply a positive voltage between the terminal anode and the terminal cathode, then it behaves like a closed switch with very little voltage drop. But if we apply a reverse polarity of voltage, it behaves like an open switch.

The current through a diode can flow only in one direction from anode to cathode. It cannot flow from cathode to anode; this is not possible. If you look at a practical characteristic of a diode the IV characteristics of a diode that is if you plot voltage $V_A K$

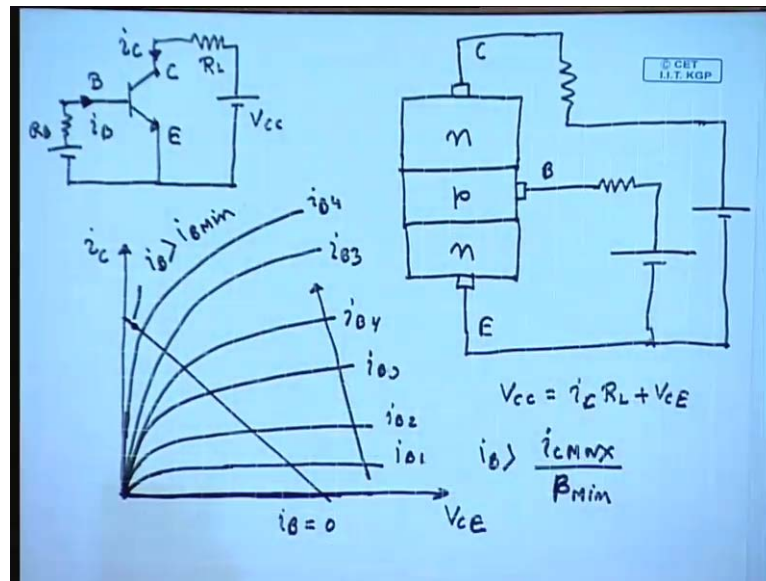
versus the current I_A , it looks somewhat like this. In the forward direction it almost does not have any voltage drop; in the reverse direction it almost does not carry any current.

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So, if I use such a device let us say with a simple AC circuit single phase AC circuit like this; this is current, this is input voltage, this is load current, this is load resistance, this is load voltage. Then this is the input voltage the load voltage. When the input voltage is positive, then this will behave like a closed switch. Hence the input voltage will appear across the load, but when the voltage is negative there will be no voltage. So, this is called a half wave rectifier circuit. While a diode is a useful switch, it cannot control; it cannot be turned on or off by a control signal. That is the conduction interval of the diode will be solely determined by the voltage across it. It cannot be controlled in any other manner there are other switches in which that is possible.

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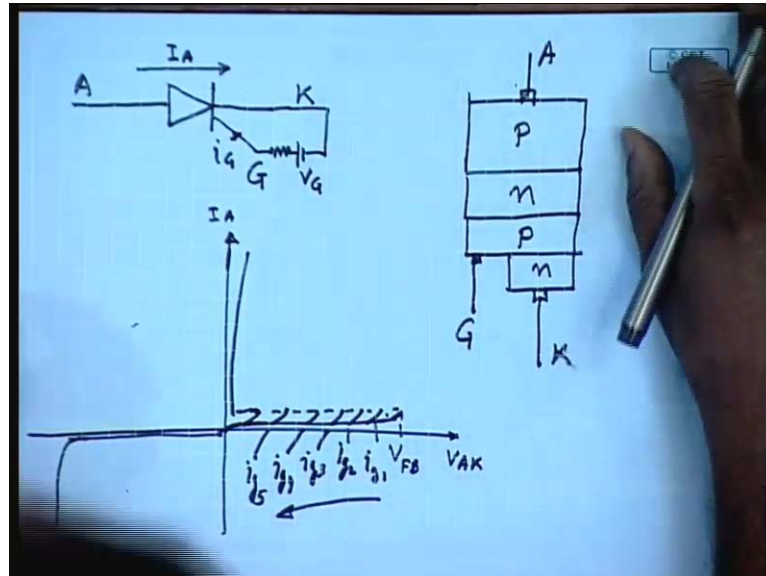
For example, the next switch is the known transistor. This is what is called a n p n transistor. This terminal is called collector; this terminal is called base; this terminal is called emitter. You all know that if certain current is injected into the base, then a proportional current flow through the collector terminal. The characteristic of this is also known. We plot i_c versus V_{cE} ; when there is no base current applied the collector current is 0. So, this transistor behaves like an off switch. As we keep on increasing the base current for a given load resistance R_L as we increase the base current the collector current starts increasing and then saturates at a particular value for a given base current determined by the device characteristics.

So, this is i_{B1} , this is i_{B2} , this is i_{B3} , this is i_{B4} , this is i_{B5} , and it is increasing in this direction. The load line if this is V_{cE} is given by $V_{cE} = i_C R_L + V_{cE}$ which look somewhat like a straight line. Now for this load if the applied base current let us say is larger than i_{B5} , then the voltage across the device will be almost 0. So, by knowing what is the maximum current that can flow through the transistor and if we increase i_B to be larger than some i_{Cmax} by what is called the minimum current gain β_{min} , then we can ensure that the drop across the transistor will be very small. And hence, in that case it will act as a closed switch.

So, here we have a switch in which we can control the base current to determine the state of the switch whether it will be off state where corresponds to $i_B = 0$ or in the on

state corresponding to I_b larger than some I_b minimum. So, this is another power electronic switch which is a controlled one unlike the diode.

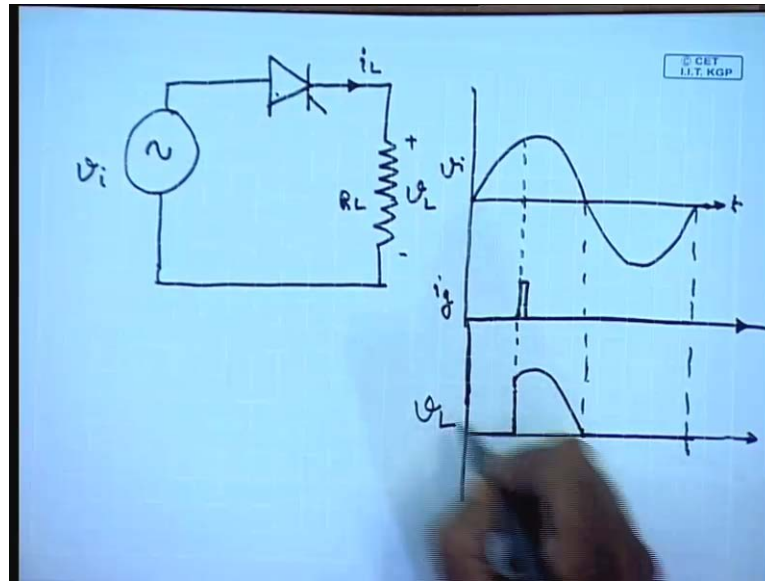
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The next control switch is called a thyristor. It has also three terminals; like diode it has anode and cathode and like transistor it has another terminal called gate which is the control terminal. In construction it is a PN-PN construction. This is anode; this is cathode, and this is where the gate terminal is, okay. Operation of this device is slightly more complicated, and we will not have occasion to discuss that in detail. It will be sufficient to tell that this is also a controlled switch which can be turned on by injecting a current through the gate terminal. However, in order to turn it off the current flowing through anode and cathode has to be disrupted brought below a certain level, only then it will turn off.

The characteristics look somewhat like this. As you keep on applying forward voltage, the device conducts very little current if there is no gate current up to. Then once it reaches certain maximum voltage called the forward breakdown voltage, then the device turns on; after that it behaves almost like a diode. The reverse side it is like a diode; however, the point at which the device turns on can be controlled by controlling the gate current. Therefore, we can apply different gate current to turn it on at different forward voltage level. So, this is for $i_g 1$, this is for $i_g 2$, this is for $i_g 3$, this is for $i_g 4$, $i_g 5$, etcetera. So, the gate currents increase in this direction.

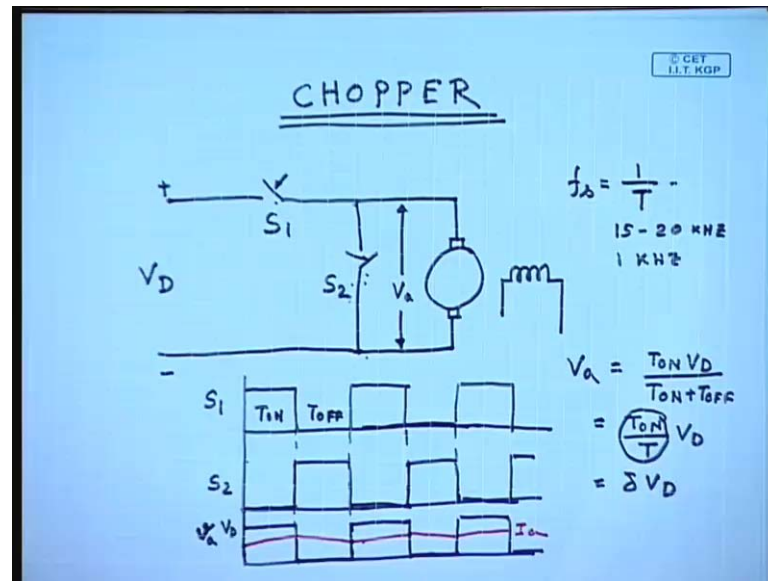
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So, if we use this kind of a device with our AC circuit with diode, then we find the following waveforms. This is V_i , and let us say a gate current is applied at this instant. It is to be understood that it is not necessary to continuously apply the gate current. Once the device has turned off, the gate pulse can be removed and the device will remain on. It can only be turned off when the current through it becomes 0. In that case V_L up to this point, this device will behave as an open switch.

And at this point when the large gate current is applied then it will become a closed switch, and afterwards it will follow the input voltage. So, this is how the load voltage will look like. So, these are some the devices which can be used to control the voltage applied to a DC shunt motor and hence control its speed. Now what type of device or circuit will exactly be used depends on what type of supply is available.

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If the available supply is DC then the circuit that is used is called chopper. The chopper circuit is very simple. You have one switch here; you have another switch here. These are controlled switches like the transistor, and then you have the DC machine. The pin is normally separately excited. So, let us say this is the input DC voltage. The turn on and turn off of these two switches are complementary; that is when s 1 is on s 2 is off, when s 2 is on s 1 is off. This is necessary; otherwise, if s 1 and s 2 are simultaneously on then there will be a short circuit across the DC supply which must be avoided. So, the on period of s 1 may be something like this. The on period of s 2 will be its logical complement.

So, what will be the waveform of the voltage applied across the armature? Obviously, whenever s 1 is on the applied voltage across the armature is same as V d. During this period the armature voltage, this is V D. During this period when s 2 is on the applied voltage is 0. So, what is the average armature voltage V a? if this period is T on, this period is T off, then V a equal to average voltage V a equal to T on into V D divided by T on plus T off which comes to T on by T V D. The quantity T on by T is called the duty ratio of the chopper delta equal to delta V D. So, you see this chopper provides a convenient means of controlling the average voltage applied across the DC machine armature terminal.

Now the speed of a DC machine will mostly depend on the average voltage, because this chopping is done at a very high switching frequency. The switching frequency f_s equal to $1/T$ is usually kept constant, and this can range in the range of 15 to 20 kilohertz for smaller machine. Even for larger machine it will be greater than 1 kilohertz. Now the DC motor armature because it contains winding it also has some amount of inductance. So, if we look at the current waveform even when the applied voltage looks like a pulsed waveform the current it is almost DC; the pulsation in the current is very small. This is I a. Hence, torque is almost smooth, and speed is determined by the average DC voltage. So, what will be the torque speed characteristics of a DC motor driven by such a chopper?

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$$\omega = \frac{V_a}{k\phi} - \frac{r_a}{(k\phi)^2} T_e$$

$$V_a = \delta V_d$$

$$\omega = \frac{\delta V_d}{k\phi} - \frac{r_a}{(k\phi)^2} T_e$$

$$V_d = k\phi \omega_0$$

$$\omega = \delta \omega_0 - \frac{r_a}{(k\phi)^2} T_e$$

$$\frac{\omega}{\omega_0} = \delta - \frac{r_a}{k\phi V_d} T_e$$

$$= \delta - \frac{T_e}{k\phi I_{a_{max}}} = \delta - \frac{T_e}{T_{e_{max}}}$$

$$\eta = \frac{\omega}{\omega_0}$$

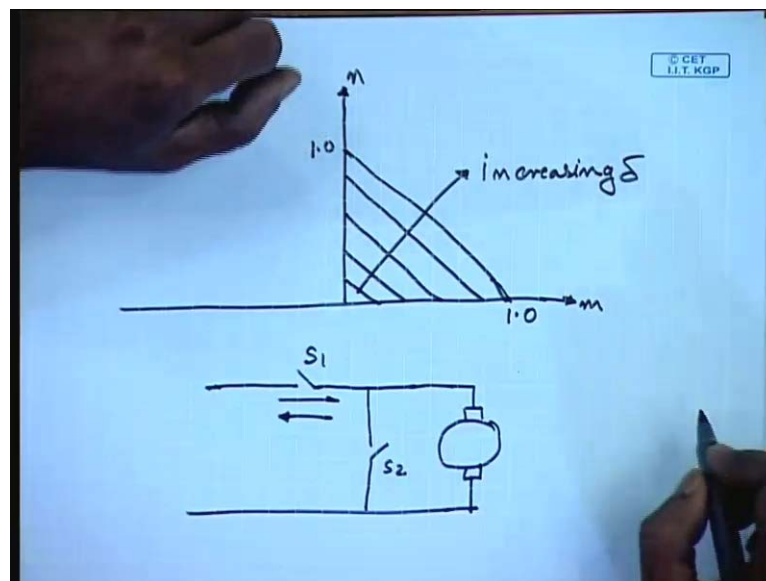
$$m = \frac{T_e}{T_{e_{max}}}$$

$$\boxed{\eta = \delta - m}$$

We know that the torque speed characteristics of a DC machine is given by $\omega = \frac{V_a}{k\phi} - \frac{r_a}{(k\phi)^2} T_e$. Now we have seen with a chopper $V_a = \delta V_d$, so $\omega = \frac{\delta V_d}{k\phi} - \frac{r_a}{(k\phi)^2} T_e$. Now let us say the DC machine is rated such that when $\delta = 1$ that is the full voltage V_d is applied across its terminal, the DC machine operates at its rated no load speed. So, in other words if we say $V_d = k\phi \omega_0$, where ω_0 is the rated no load speed of the DC machine. Then we can write $\omega = \delta \omega_0 - \frac{r_a}{(k\phi)^2} T_e$, or $\frac{\omega}{\omega_0} = \delta - \frac{r_a}{k\phi V_d} T_e$.

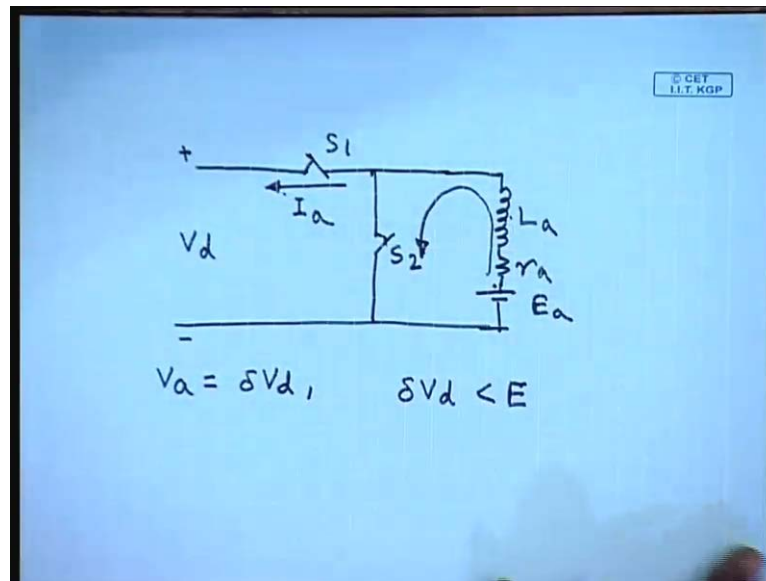
But V_d by r_a is the short circuit I mean direct online starting current of the DC machine. So, this is equal to $\Delta - T_e$ divided by $k \phi I_a \max$; that is $\Delta - T_e$ by $T_e \max$ which is the maximum torque at direct online starting with a voltage of V_d . So, if we define per unit speed n to be equal to ω by ω_0 and per unit of m to be T_e by $T_e \max$, then the torque speed characteristics is given by the simple equation n equal to $\Delta - m$.

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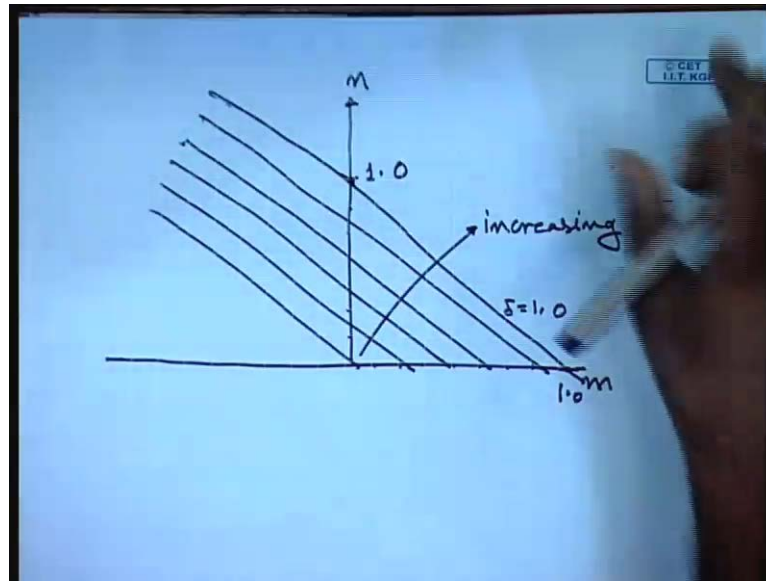
That is the torque speed characteristics of a chopper driven DC machine normalized torque speed characteristics is this is n ; this is m . These are straight lines 45 degree slope. This is increasing Δ . Interesting thing to note is that if these switches can allow average current to flow in the reverse direction; that is instead of current flowing in this direction if it allows in this direction also then the same circuit can be used for regenerative braking; reason is very simple.

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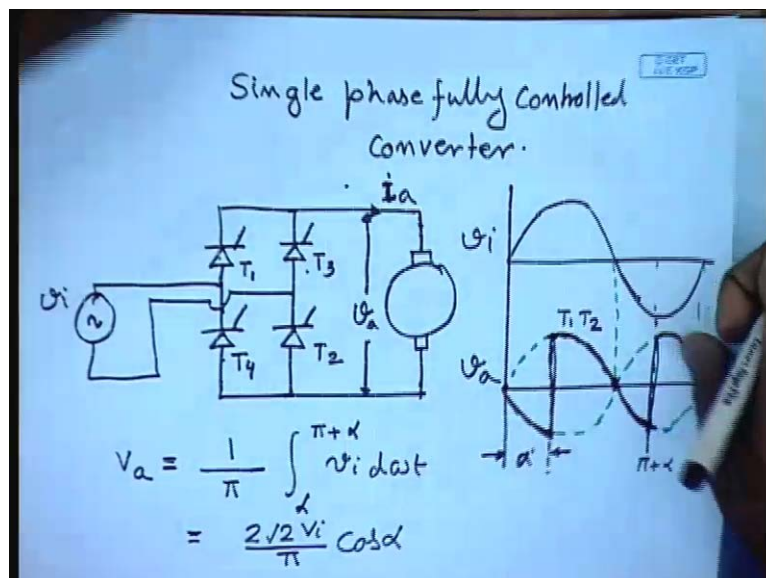
If we draw the transient equivalent circuit of the DC machine we will find that in addition to resistance it has an armature inductance. This is the back E m f. This is called the L_a, r_a, E_a . So, whenever S_2 is turned on the current flows through the armature inducting in this way, and when it is turned off then the inductor current cannot vanish immediately. Hence, it starts flowing through the switch S_1 . So, we see if this switch is still on then you can send the current back to the supply. When will this current be reserved? we have seen the terminal voltage V_a equal to $V_d - \delta V_d$. So, if δV_d is less than the induced back E m f be it E , then of course, the direction of the current will change and hence it can be used for regenerative braking purpose.

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Therefore, the torque speed characteristic of such a chopper driven DC machine is the same on both the quadrants. So, one advantage we see of using a chopper that regional braking is now possible even below base speed. This is n equal to 1.0 corresponding to the base speed. This is because the effective voltage applied across the DC machine can be controlled by controlling the duty cycle δ . This is when a chopper is DC supply is available and a chopper is used, but more often the not the available supply is AC.

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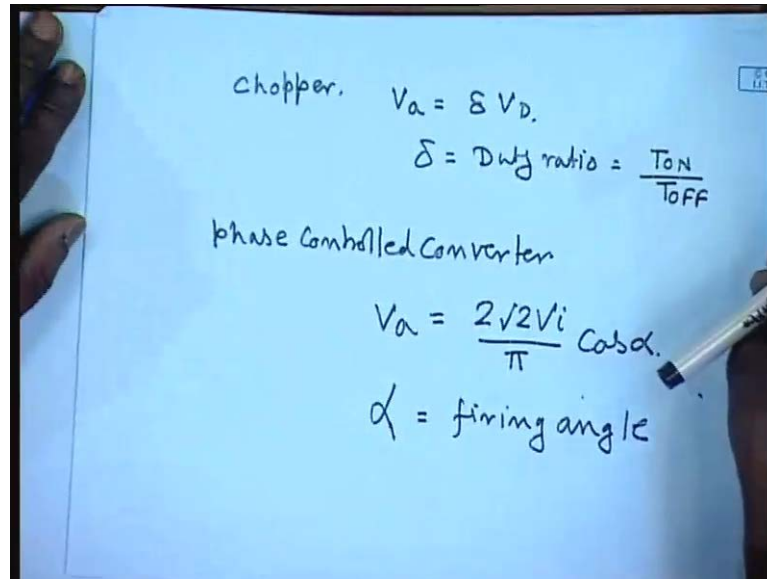


So, if we have a single phase AC then we can use another power electronic convertor called the single phase fully controlled convertor. In this you have the convertor looks like a diode rectifier bridge, but instead of diode we use thyristors. This is say T 1, this is T 2, this is T 3, this is T 4. This is the AC source and the DC machine is connected here. Let us say this is the input voltage V_i , had this been diodes we know that the voltage waveform would have been a full wave rectifier sin wave. But since this is the thyristor, the full wave rectifier sin wave is not possible. So, we delay the firing of the thyristor T 1 with respect to the zero crossing of the supply by an angle let us say α which is called the firing angle.

Then the voltage starts, the V_a starts following the rectifier sign wave from this point; however, as we have mentioned that this armature has inductance. So, even though the armature voltage becomes zero here the current through the armature may not be zero, and hence it will continue to follow the T 1 T 2 will then not turn off, because until and unless current through them becomes 0; these devices will not turn off. So, it will continue to follow the input voltage V_i . And if the current does not becomes zero, before the next set of thyristor that is T 3 T 4 here, T 1 and T 2 are fired firing that is gate pulses applied to them. So, it will continue up to the point where T 3 and T 4 are gated.

When T 3 and T 4 are gated, what will happen? This T 1 which was normally on switch, when T 3 is turned on then a reverse voltage V_i which is now positive. Well, minus V_i will be applied across T 1 and the current through it will transfer to T 3; that way T 1 will turn off. Hence, now the armature voltage will start following minus here; same thing will happen here. So, the final armature voltage will look somewhat like this. As we have seen that the speed of the DC machine depends on the average armature voltage. So, it will be imperative to find out what is the average armature voltage here V_a equal to V_i by, since it is symmetric over one cycle it will be sufficient to integrate over one-half cycle. This comes out to be, where V_i is the R m s of the input voltage.

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So, you have considered two power electronic convertors to control the average DC voltage applied across the armature of a DC shunt motor. For chopper average applied voltage V_a equal to δV_D where δ is the duty ratio equal to T_{ON} by T_{OFF} for phase control convertor. The second one V_a equal to $\frac{2\sqrt{2}V_i}{\pi} \cos\alpha$ which is α is called the firing angle. Unfortunately, for this case though there is no way this armature current can flow in the opposite direction.

So, degenerative braking in the forward direction is not possible, but we can see that if we make α larger than 90 degree then the average DC voltage becomes negative in which case when the current flows in this direction, then with this terminal positive and this terminal negative the power is still fed back to the supply. Hence regenerative braking is possible, but for that the direction of rotation of the motor must reverse; that is the back E m f must reverse. So, let us try to solve one or two problems to see how the speed of the machine can be controlled using single phase fully controlled convertor.

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200V, 875 RPM, 150A
 $r_a = 0.06 \Omega$
1 ϕ AC supply, 220V, 50 Hz
 $n = 750 \text{ RPM}$, $T_e = T_{e|\text{rated}}$, $\alpha = ??$
 $T_e = T_{e|\text{rated}}$, $I_a = I_{a|\text{rated}} = 150 \text{ A}$
 $E|_{875 \text{ RPM}} = 200 \text{ V} - 150 \times 0.06 = 191 \text{ V}$
 $E|_{750} = \frac{750}{875} \times 191 = \cancel{172.7} 163.7 \text{ V}$
 $V_a = E|_{750} + 150 \times 0.06 = 172.7 \text{ V}$

So, let us say we have a DC machine whose rated terminal voltage is 200 volts, speed is 875 RPM, and armature current is 150 amperes. The armature resistance r_a equal to 0.06 ohm. Now it is supplied from a single phase AC supply source voltage 220 volt 50 hertz. Let us say we want to operate the machine at 750 RPM, and torque should be equal to T_e rated; find out what should be the firing angle α ? So, under rated operation when T_e equal to T_e rated assuming rated flux I_a equal to I_a rated equal to 150 amperes, then what is E ? E equal to rated terminal voltage which is 200 volts minus at a rated speed that is at 870 RPM, because that is when 200 volt is applied minus I_a which is 150 amperes into armature resistance 0.06 ohms. This comes to 191 volts.

So, at E at f 750 RPM, how much it will be? This is 750 by 875 into 191 equal to 172.5 volts. So, what if we now want to operate the machine at the rated torque, at 750 RPM what should be the terminal voltage average armature voltage V_a should be? E 750 plus rated armature current 150 amperes into armature resistance. Sorry, this comes to 163.7 volts; this comes to 172.7 volts.

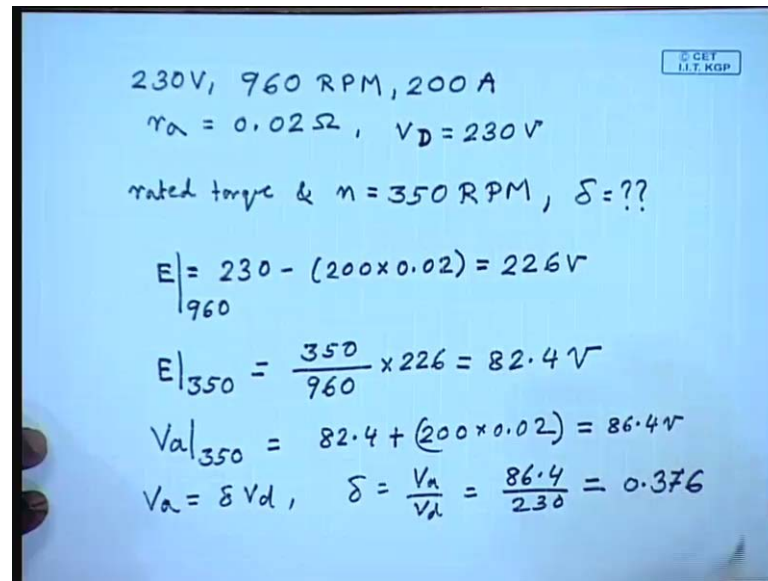
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$$V_a = 172.7V = \frac{2\sqrt{2} V_i}{\pi} \cos \alpha$$
$$= \frac{2\sqrt{2} \times 220}{\pi} \cos \alpha$$
$$\cos \alpha = 0.872, \alpha = 29.3^\circ$$
$$\alpha = 160^\circ$$
$$V_a = \frac{2 \times \sqrt{2} \times 220}{\pi} \cos 160^\circ = -186V$$
$$E = V_a - I_a R_a = -186 - 150 \times 0.06 = -195V$$
$$\text{Speed} = -\frac{195}{191} \times 875 = -893 \text{ RPM}$$

Now this V_a is equal to $2 \sqrt{2} V_i$ by $\pi \cos \alpha$ equal to $2 \sqrt{2}$ into 220 by $\pi \cos \alpha$. This gives $\cos \alpha$ equal to 0.872 or α equal to 29.3 degrees. So, almost at α equal to 30 degree we will be able to reduce the motor speed to 75 RPM while still supplying rated torque. Now looked at the other way, let us say now we have increased this α to 160 degree, but it is still developing rated torque. So, what will be the motor speed in that case? So, at α equal to 160 V_a equal to 2 into $\sqrt{2}$ into 220 by $\pi \cos 160$ degree. This comes to minus 186 volts. Then E is V_a minus $I_a R_a$.

Please note that in a phase controlled convertor, the current can flow only in one direction; that is it can flow only into the mode of terminal. So, this comes to minus 186 minus 150 into 0.6 ; this comes to minus 195 volts. So, the speed will be approximately minus 893 RPM. So, we see with α larger than 90 degree, the motor operates in the opposite direction and works in the degenerating braking port, because the terminal voltage is negative; the current is positive. Hence, power is fed back to the DC supply. Let us try to solve similar problems involving choppers.

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230V, 960 RPM, 200 A
 $r_a = 0.02 \Omega$, $V_D = 230V$
rated torque & $n = 350$ RPM, $\delta = ??$

$$E|_{960} = 230 - (200 \times 0.02) = 226V$$
$$E|_{350} = \frac{350}{960} \times 226 = 82.4V$$
$$V_a|_{350} = 82.4 + (200 \times 0.02) = 86.4V$$
$$V_a = \delta V_d, \quad \delta = \frac{V_a}{V_d} = \frac{86.4}{230} = 0.376$$

So, we have a 230 volt, 960 RPM, 200 ampere separately excited DC motor, its r_a is equal to 0.02 ohm. This motor is fed from a chopper, whereas supply voltage V_d is equal to 230 volt. If I want to operate this motor at a rated torque and a speed equal to 350 RPM, then what should be the delta? Under rated condition of the machine we know E is equal to 230 minus. So, this is E at 960 RPM; so E at 350 RPM. So, V_a at 350 RPM and rated torque this will be 82.4 plus, at rated torque the current is also rated. So, 200 into 0.02; this comes to 86.4 volt. We know V_a is equal to δV_d or δ is equal to V_a by V_d is equal to 86.4 by 230. So, this delta will be 0.376. So, it will be interesting also to find out what is the maximum control of speed control of such an arrangement?

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$$\begin{aligned} \delta|_{\max} &= 0.95, \quad I_a|_{\max} = 2 I_n|_{\text{rated}}. \\ n|_{\max} \\ V_a|_{\max} &= 0.95 \times 230 = 218.5 \text{ V} \\ E|_{\max} &= 218.5 + (200 \times 2 \times 0.02) \\ &= 226.5 \text{ V} \\ n|_{\max} &= \frac{226.5}{226} \times 960 = 962 \text{ RPM}. \end{aligned}$$

For that let us assume that maximum value of delta has certain limit 0.95. This comes because the switches which are power electronic switches require a minimum on time and off time. So, delta cannot really be made 1 or 0. So, under this condition and let us say the maximum permissible two times I_a rated. So, calculate the maximum possible speed without resorting to field weakening. Now since delta its maximum value is 0.95, then V_a maximum is 0.95 into 230 equal to 218.5 volts.

Please note that the speed in the regenerative breaking mode is higher than the motoring mode; therefore, maximum N will occur in the regenerative breaking mode. In that case the current will flow out of the motor terminal. So, E_{\max} equal to V_{\max} which is 218.5 volts plus maximum armature current which is two times the rated current of 200 into armature resistance. This comes to 226.5 volt. So, n_{\max} is E_{\max} that is 226.5 by E_{rated} into rated speed. So, this is 962 RPM.

Thank you.