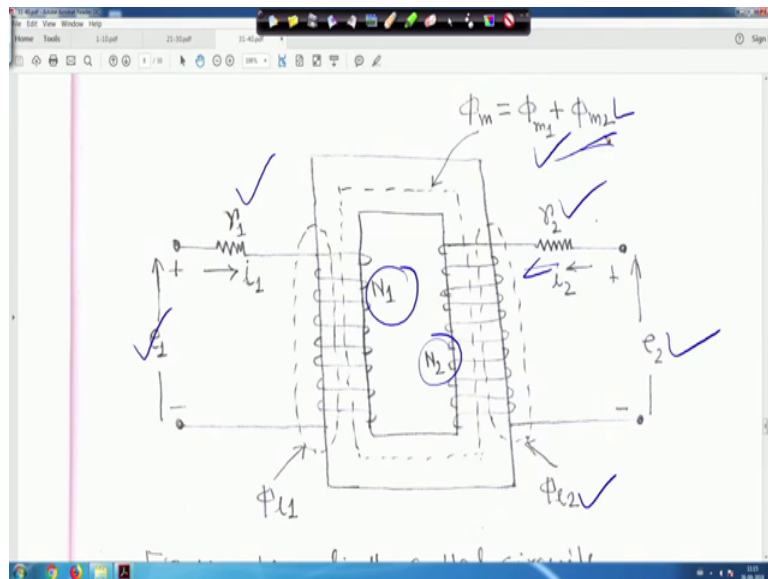


Power System Dynamics, Control and Monitoring
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Lecture – 04
Power System Stability (Contd.)

We are back again. So, next we will go for coupled circuit, right.

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So, this I told you that in fundamentals of electrical engineering couple circuits it is convention other thing how to take mutual induced voltage plus or minus sign everything is explained in detail, right. So, just to brush up our memories for this course, right. So, just I have taken a different example, right.

So, you have here you have a before giving the nomenclature here you have two coils and a your what you call this is a couple of circuit this turn of this number of turns of this coil is N_1 this is your; this is your N_1 and number turns of this coil is N_2 , right. And, resistance of this coil is r_1 and it is here r_2 , right and this voltage is e_1 this voltage is e_2 and now both the currents i_1 , i_2 entering into the your what you call into this into this coil, right and direction of the flux other thing can be applied through your right hand rule, right.

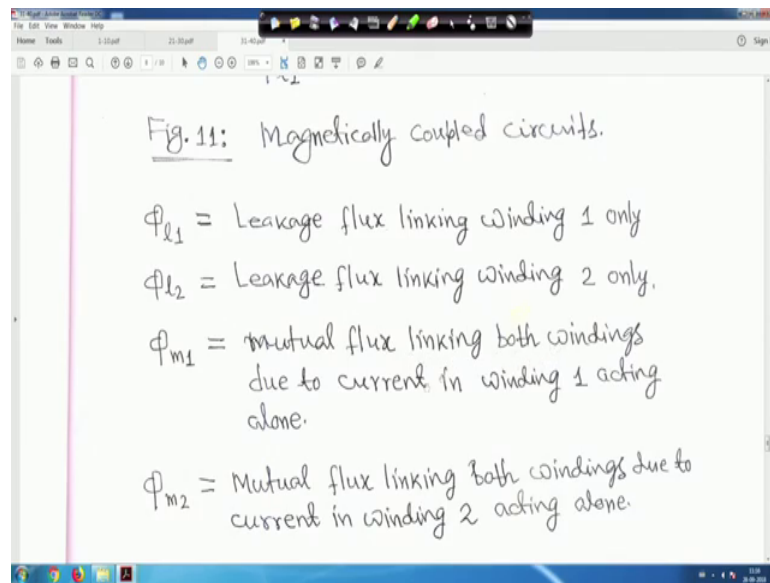
And, now question is that these things this whenever they whenever you have a you have your current is showing to this then the flux what will happen part for your part of the flux wilding this coil N_1 , right and part of this wilding this coil that is mutual one that is your this coil that is second coil right with number of turns is N_2 , right. So, that means, your what you call that is your ϕ_{m1} because of this one.

Similarly, if you have current i_2 then it will see it is your say your what you call self linkage is your flux will be ϕ_{l2} , right and because of this current some flux also ϕ_{m2} wilding this coil, right. So, in this case your ϕ_m is equal to ϕ_{m1} plus ϕ_{m2} . So, both if you what you call that if you take the your what you call that your right hand rule, then you will find these two will be additive for this I refer to the fundamentals of electrical engineering, right that magnetic circuit.

So, and these two are your N_1 , N_2 number of turns and from that we will write that equation, right. So, in that case actually for right hand rule is that this is your coil if you grasp the coil like this in the direction of the current, then this will be the direction of the flux the thumb will be direction of the flux. So, in this case this is ϕ_1 and this is entering also if you direction of the current if you grasp it, right. So, it will be also in the downward direction and this is upward directions. So, that is why these two are plus ϕ_{m1} plus ϕ_{m2} . So, that is why I refer it I request you that just have a look on that if you have any doubt otherwise I believe that you know this, right.

So, this is your what you call the coupled coil. Now, how to couple circuit? How to write those equations? So, in this case your this is magnetically coupled circuit.

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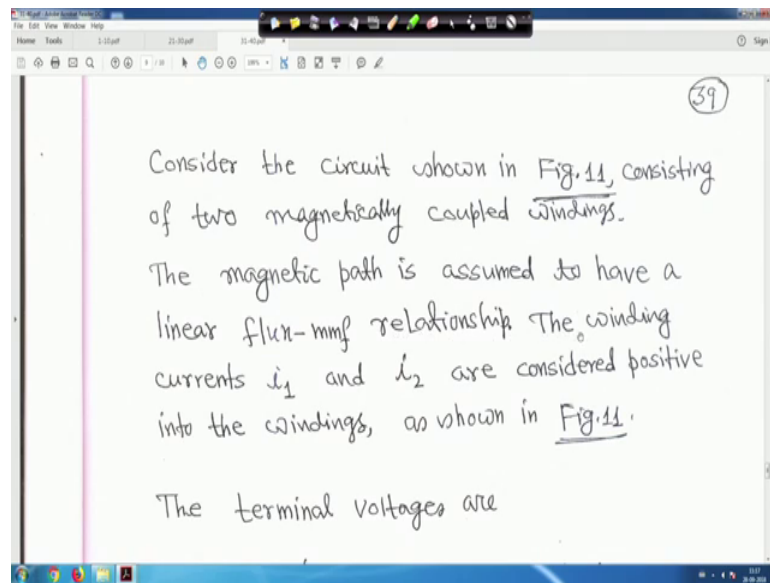


Now, ϕ_{l1} , the leakage flux linking winding 1 only this is only they were linking only winding 1; ϕ_{l2} leakage flux linking winding 2 only. So, this your winding 2, right and ϕ_{m1} mutual flux linking both windings due to current in winding one acting alone. I mean this is your ϕ_{m1} ; so, because of this your what you call because of this current in i_1 most of the flux will link this your coil 1 and part of this also your what you call link that your what you call that other coil. Apart from this coil other coil; that means, total flux linkage of this coil that is N_1 ; N_1 number of turns basically you have ϕ_{l1} plus ϕ_{m1} . Because ϕ_{l1} is self linkage, right plus this ϕ_{m1} , but this ϕ_{m1} also will link this one.

Similarly, for your other one, right ϕ_{l2} will be there ϕ_{m2} also winding this one. So, total flux linkage of this coil will be ϕ_{l2} plus ϕ_{m2} , but this ϕ_{m2} also winding this one and this ϕ_{m2} because of this your current i_2 in the second circuit that is your what you call the other coil, right. So, that is why ϕ_{m1} mutual flux linking both windings due to current in winding 1 acting alone, right. Similarly ϕ_{m2} mutual flux linking both windings due to current in winding 2 acting alone, right.

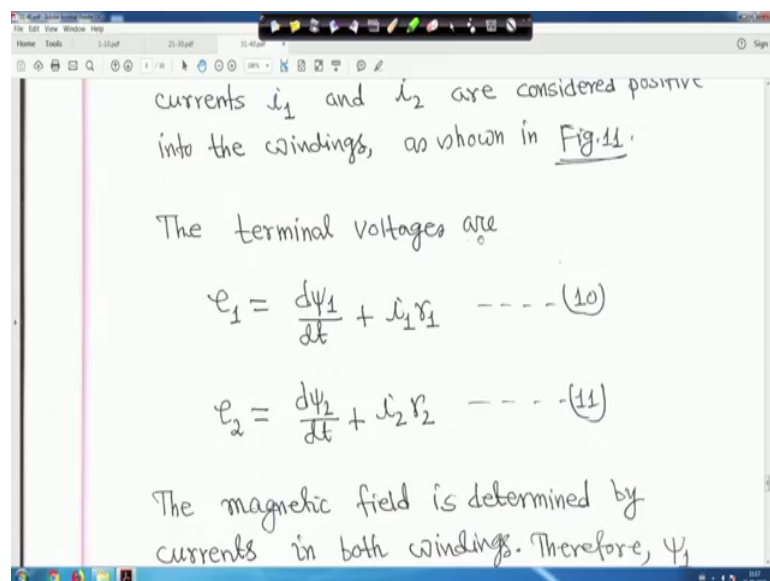
So, this is your what you call that your what you call the coupled circuit. Now, you have to write down the few equation.

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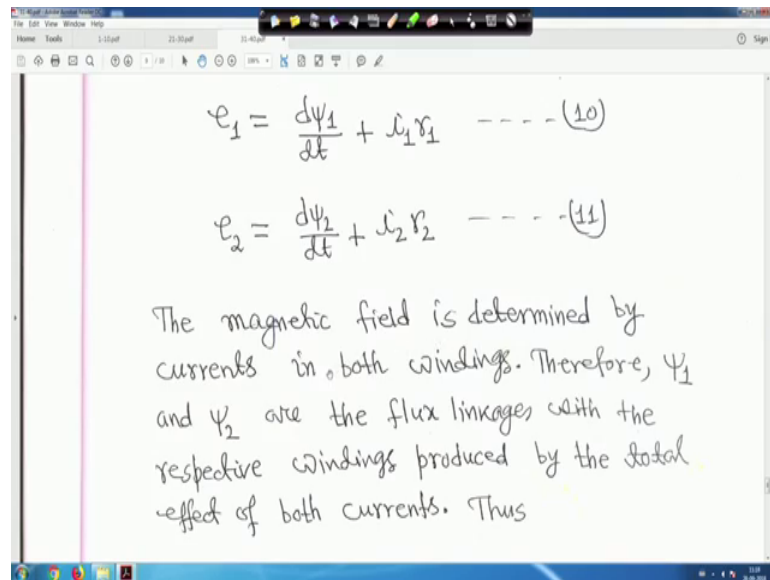
Now, consider the circuit shown in figure 11 constitute of two magnetically coupled windings. So, this is my figure 1, this is my figure 1, right sorry figure 11, figure 11, right. And, therefore, the magnetic path is assumed to have a linear flux-mmF relationship we will assume a linear relationship between flux and mmf, right that is between ϕ and $n i$, right. The winding currents i_1 and i_2 are considered positive into the winding as shown in figure 11. So, as this two currents are entering into this coil whereas, shown in it is positive, right some convention we have to make.

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Therefore the terminal voltages you can write for e_1 will be $\frac{d\psi_1}{dt} + i_1 r_1$ and for this coil if you write the terminal about a e_1 it will be $i_1 r_1$ into your $\frac{d\psi_1}{dt}$, right. So, that is your $\frac{d\psi_1}{dt}$ for coil 1. Similarly for coil 2 it will be $\frac{d\psi_2}{dt} + i_2 r_2$. So, ψ_1 , ψ_2 are the flux linkages, right.

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The magnetic field is determined by currents in both windings, right because both winding currents are there. Therefore, ψ_1 and ψ_2 are the flux linkages with the respective windings produced by the total effect of both currents, right. Thus we can write ψ_1 is equal to $N_1 \phi_{m1} + N_1 \phi_{m2}$. Now, if you come to that if you come to this circuit, right.

If you I mean why I am telling these when I write the synchronous machine equation directly we will write and we will find it is easy. For this coil see the your what you call the flux linkages right, one is that your what you call that ψ_1 for this thing that ψ_1 is equal to that one thing is there that is a ϕ_{l1} is there plus ϕ_{m1} this ϕ_{m1} is also there, right. So, ϕ_{m1} is also there so; that means, ψ_1 is equal to current is i_1 , right.

So, from that you can make out that your what you call what will be the flux linkage right what about turns. So, in that case it will be $N_1 \psi_{l1} + \psi_{m1}$ plus because of these things ψ_{m2} also there is a flux linkage of ψ_{m2} here. So, it will be $N_1 \psi_{m2}$ these are ψ_{m2} , right.

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and Ψ_2 are the flux linkages with the respective windings produced by the total effect of both currents. Thus

$$\Psi_1 = N_1(\Phi_{m1} + \Phi_{L1}) + N_1\Phi_{m2} \quad \dots (12)$$
$$\Psi_2 = N_2(\Phi_{m2} + \Phi_{L2}) + N_2\Phi_{m1} \quad \dots (13)$$

So, that means, that is why these equation this equation is written that N_1 into Φ_{m1} plus Φ_{L1} this is your what you call that your Φ_{L1} plus Φ_{m1} already linking N_1 and this Φ_{m2} is coming because of the current in the second coil i_2 and linking this flux their coil your one that is number of you can say N_1 so, that why N_1 into Φ_{m2} . Similarly, this is equation 12. Similarly, Ψ_2 will be N_2 into Φ_{m2} plus Φ_{L2} plus N_2 into Φ_{m1} just other way, right and this is your Ψ_1 and Ψ_2 the flux linkages, right.

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The flux linkages can be expressed in terms of self and mutual inductances whose expressions are given below.

Self inductance, by definition, is the flux linkage per unit current in the same winding.

Accordingly, the self inductances of windings 1 and 2 are, respectively,

$$L_{11} = N_1(\Phi_{m1} + \Phi_{L1}) \quad \dots (14)$$

So, that means, the flux linkages can be expressed in terms of self and mutual inductances whose expressions are given below, right we will see that self inductance by definition is the flux linkage per unit current in the same winding that you know this, right. So, accordingly the self inductances of windings 1 and 2 are respectively you can write L_{11} will be N_1 into $\phi_{m1} + \phi_{l1}$ upon i_1 because, if you come to this diagram if you come to this diagram this because of this current i_1 the flux linkage actually $\phi_{l1} + \phi_{m1}$, right. So, and similarly because of this current i_2 flux linkage this coil, right $\phi_{m2} + \phi_{l2}$ and other thing that is mutual one linking that is your what you call that ϕ_{m1} linking this coil also.

Similarly, ϕ_{m2} plus linking this coil also, but our interest is now self inductance. So, it will be basically ϕ_{l1} your flux linking this coil $\phi_{l1} + \phi_{m1}$. So, that is why we are writing that self inductance is this one your $L_{11} = N_1$ into $\phi_{m1} + \phi_{l1}$ divided by i_1 , right.

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$$L_{11} = \frac{N_1(\Phi_{m1} + \Phi_{l1})}{i_1} = \frac{N_1\Phi_{m1}}{i_1} + \frac{N_1\Phi_{l1}}{i_1} \quad (14)$$

$$L_{22} = \frac{N_2(\Phi_{m2} + \Phi_{l2})}{i_2} \quad (15)$$

OR

$$L_{11} = (L_{m1} + L_{l1}) \quad (16)$$

$$L_{22} = (L_{m2} + L_{l2}) \quad (17)$$

Similarly, for L_{22} just same thing N_2 into ϕ_{m2} plus ϕ_{l2} upon i_2 ; this is 14 and 15, these two equation number, right or we can write L_{11} is equal to L_{m1} plus your L_{l1} ; that means, that things we have what we are writing actually this term say this term this term you can break it like this it is N_1 your ϕ_{m1} divided by i_1 plus you can write $N_1 \phi_{l1}$ divided by i_1 , right.

So, this term $N_1 \phi_{m1}$ by i_1 this is your this one and this term $N_1 \phi_{l1}$ this is your this term, right. So, this is equation 16.

(Refer Slide Time: 10:15)

OR

$$L_{11} = (L_{m1} + L_{l1}) \quad \dots (16)$$

$$L_{22} = (L_{m2} + L_{l2}) \quad \dots (17)$$

Where L_{m1} and L_{m2} are the magnetizing inductances, and L_{l1} and L_{l2} are the leakage inductances, of the respective windings.

So, similarly your L_{22} . Similarly, it will be L_{m2} it is nothing, but $N_2 \phi_{m2}$ upon i_2 this is L_{m2} plus your $N_2 \phi_{l2}$ upon i_2 this is L_{l2} this is equation 17, right where L_{m1} and L_{m2} are the magnetizing inductances, right or sometimes we call mutual inductances, right and L_{l1} and L_{l2} are the leakage inductances of the respective windings. So, just hold on.

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(4)

Mutual inductance between two windings, by definition, is the flux linkage with one winding per unit current in the other winding. Therefore, the mutual inductances between windings 1 & 2 are

$$L_{12} = \frac{N_1 \phi_{m2}}{i_2} \quad \dots (18)$$

So, now mutual inductance between two windings by definition is the flux linkage with one winding per unit current in the other winding therefore, the mutual inductances between windings 1 and 2 are these also you know, this also you know, right. So, this is your this is your mutual inductance between two windings by definition is the flux linkage with one winding per unit current in the other winding. Therefore, the mutual inductances between windings 1 and 2 are L_{12} will be $N_1 \phi_{m2}$ and it is actually this ϕ_{m2} this flux actually mutual flux that is linking the coil 1 whose turn is N_1 and that is due to the current is i_2 you can write L_{12} is equal to $N_1 \phi_{m2}$ upon i_2 this is your equation 18, right.

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and

$$L_{21} = \frac{N_2 \phi_{m1}}{i_1} \quad \dots (19)$$

If P is the permeance of the mutual flux path,

$$\phi_{m1} = N_1 i_1 P \quad \dots (20)$$

$$\phi_{m2} = N_2 i_2 P \quad \dots (21)$$

From Equations (19), (20), (21) ...

Similarly, your similarly L_{21} will be $N_2 \phi_{m1}$ upon i_1 this is equation – 19, right. So, if P is the if you assume that P is the permeance of the mutual flux path the nu can we know that ϕ_{m1} will be $N_1 i_1$ into P , right. So, anyway mmf into permeance is equal to flux linkage so, but in terms of your what you call P is the permeance of the mutual flux path then we can write ϕ_{m1} is equal to $N_1 i_1$ into P similarly ϕ_{m2} is equal to $N_2 i_2$ into P , right.

(Refer Slide Time: 12:19)

If μ is the permeance of the mutual flux path,

$$\Phi_{m2} = N_2 i_2 \mu \quad \dots (20)$$

$$\Phi_{m1} = N_1 i_1 \mu \quad \dots (21)$$

From Eqn (18), (19), (20) & (21), we get that

$$L_{12} = L_{21} = N_1 N_2 \mu \quad \dots (22)$$

Now, equation is 18, 19, 20 and 21 if you use 18, 19, 20 and 21 you will get L_{12} is equal to L_{21} is equal to $N_1 N_2 \mu$, right. That means, this equation your what you call your, just hold on I will make it for you these equation you multiply numerator and denominator by your $N_1 N_2$, right yes, by N_1 . If you do so, just hold on; just hold on I will go to the equation – 18, that will be easier, right.

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between windings 1 & 2 are

$$L_{12} = \frac{N_1 \Phi_{m2}}{i_2} \quad \dots (18)$$

and

$$L_{21} = \frac{N_2 \Phi_{m1}}{i_1} \quad \dots (19)$$

If μ is the permeance of the mutual flux path,

$$\Phi_{m1} = N_1 i_1 \mu \quad \dots (20)$$

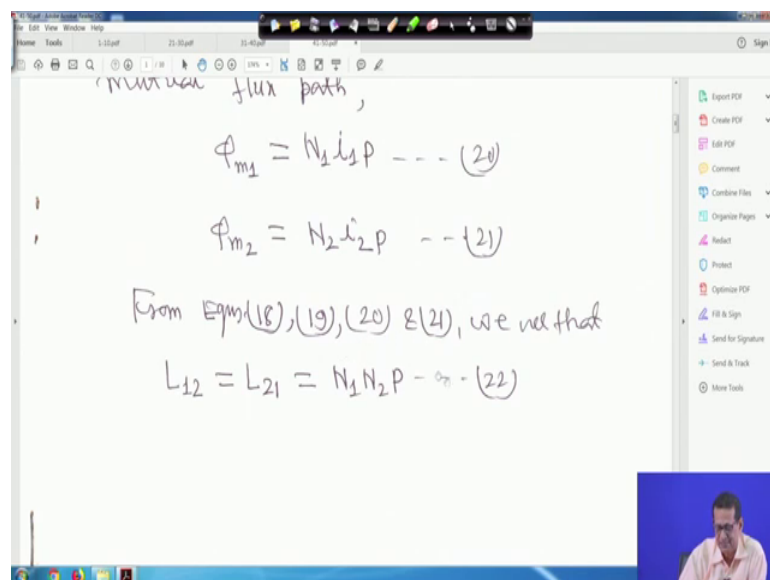
Annotations: $H_1 N_1 = \frac{\Phi_{m2}}{H_2 i_2}$ and $(H_1 N_1) = \frac{\Phi_{m1}}{N_1 i_1}$

Just hold on these equation if you multiply by your N_1 your N_1 is there, multiply numerator and denominator by your N_2 , right and if you do so, then just hold on space

is space is not there I making it here these equation I making it here it is N 1 the numerator and denominator we multiplied by N 2 this is N 2 then this one you can write phi m 2 by your N 2 into i 2, right.

So, this is nothing, but your permeance this is your flux by your what you call that your mmf this is N 2 in i 2, right. So, this one you can make it as a P, right that is the permeance. So, that similarly this one if you multiply this one by your N 1 term then it will be N 1 N 2, right; it will be N 1 N 2, then this 1 you can write phi m 1 upon N 1 i 1, this is also expression for permeance, right.

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So, that is why if you do so; if you do so; that means, so, that is why this equation can be written as you phi m 1 is equal to N 1 i 1 P phi m 2 we have already written; therefore, these two we find L 12 is equal to L 21 because N 1 N 2 into P because this permeance expressions are given here P P the your permeance for the path P will be remain same right, but your right. Therefore, P is equal to your phi m 1 upon N 1 i 1 or is equal to phi m 2 upon N 2 i 2. So, basically it will be N 1 N 2 into P right. So, that is L 12 is equal to L 21 is equal to N 1 N 2 P. So, that is same this is equation – 22 right.

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Substitution of Eqm.(16) to (19) in Eqm(12) and (13) gives the following expressions for flux linking windings 1 and 2 in terms of self and mutual inductances:

$$\Psi_1 = L_{11} i_1 + L_{12} i_2 \quad \text{--- (23)}$$
$$\Psi_2 = L_{21} i_1 + L_{22} i_2 \quad \text{--- (24)}$$

In the above equations it is important to

So, substituting substitution of equation 16 to 19 in equation 12 and 13 you give the following expression for flux linkage of winding 1 and 2 in terms of self and mutual inductance. So, if you substitution of equation 16 to 19; that means, your whatever you have in the previous page 16 to 19, right 16, 17, 18 and 19, right. So, in equation 12 and 13 just you do this, I am not going back that is the very simple thing just you do this. So, you will get the flux linkage psi 1 will be L 11 i 1 plus L 12 i 2, right that is equation 23 and similarly psi 2 will be L 21 i 1 plus L 22 i 2, this is equation 24.

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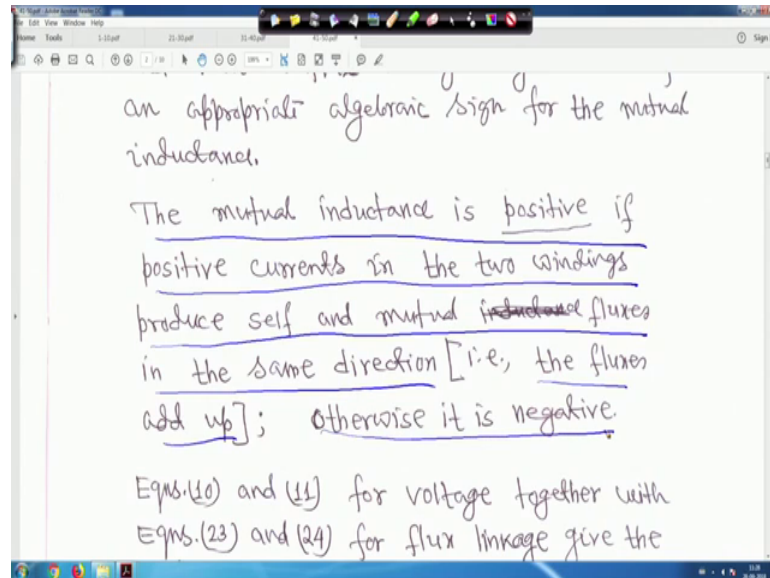
$$\Psi_1 = L_{11} i_1 + L_{12} i_2 \quad \text{--- (23)}$$
$$\Psi_2 = L_{21} i_1 + L_{22} i_2 \quad \text{--- (24)}$$

In the above equations, it is important to recognize the relative directions of self and mutual flux linkages by the use of an appropriate algebraic sign for the mutual inductance.

The mutual inductance is positive if

So, in the above equations it is important to recognize the relative direction of self and mutual flux linkages by the use of the appropriate algebraic sign for the mutual inductance, right.

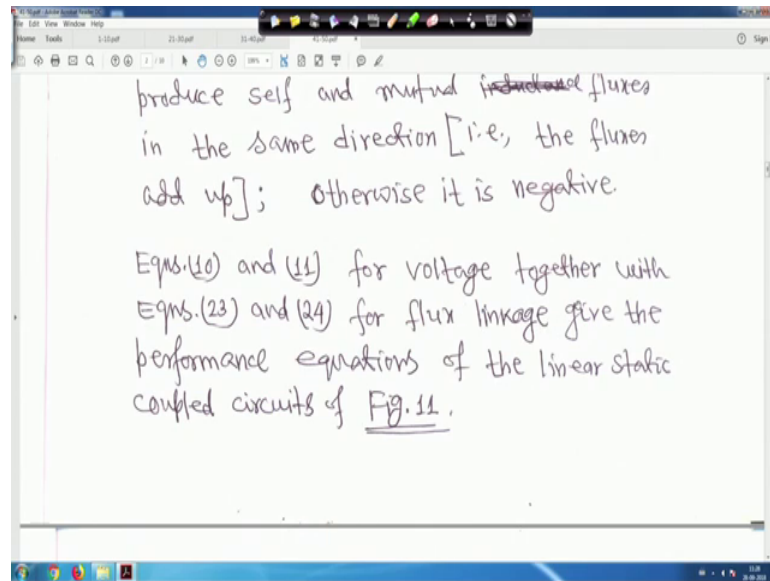
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So, the mutual inductance is positive if positive currents in the two windings produce self and mutual fluxes in the same direction, right. So, that you have to this is from your this you have to keep it in your mind. The mutual inductance that is your I am just underlining; in the mutual inductance is positive if positive currents in the two windings produce self and mutual fluxes in the same direction, that is the fluxes add up, right.

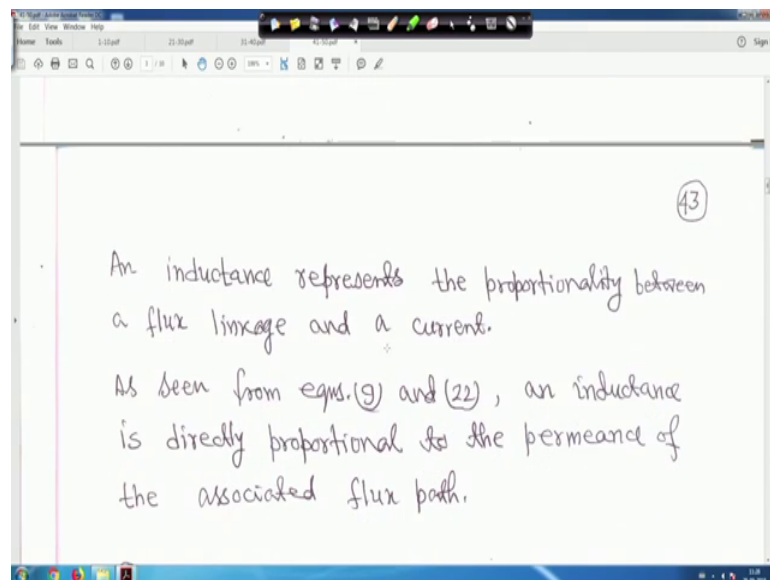
So, there we have seen know ϕ_{m1} plus ϕ_{m2} , right and just you apply the your right hand rule and change the direction of the current and have a look that is why I refer again and again the magnetic and coupled circuit. You read any book or that fundamentals of electrical engineering course. The magnetic circuit course just brush up your memories if you have if you if you want to have a look on this, right, that is the fluxes add up otherwise it is negative, right.

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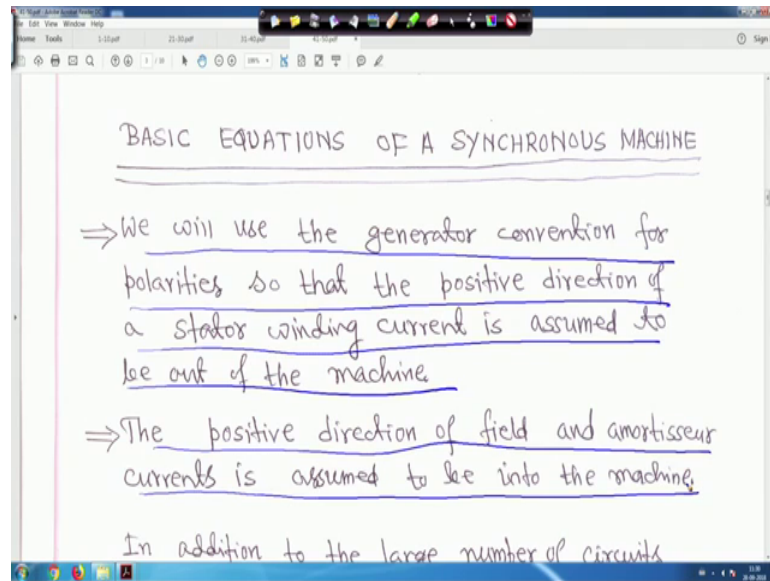
Therefore, equation 10 and 11 for voltage together with equation 23 and 24 for flux linkage give the performance equation of the linear static coupled circuit, right, that is the figure 11.

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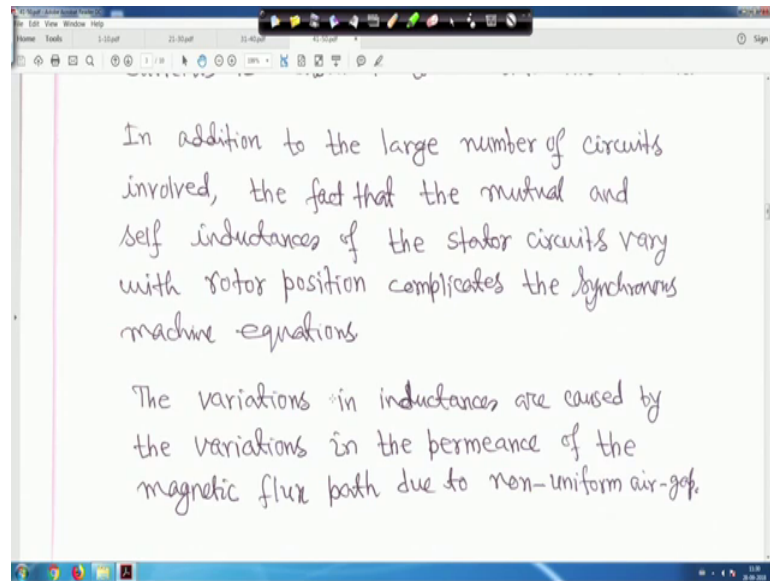
So, now an inductance actually represent the proportionality between a flux linkage and a current, right. As seen from equation – 9 and 22 and inductance is directly proportional to the performance of the associated flux path, right that we have seen.

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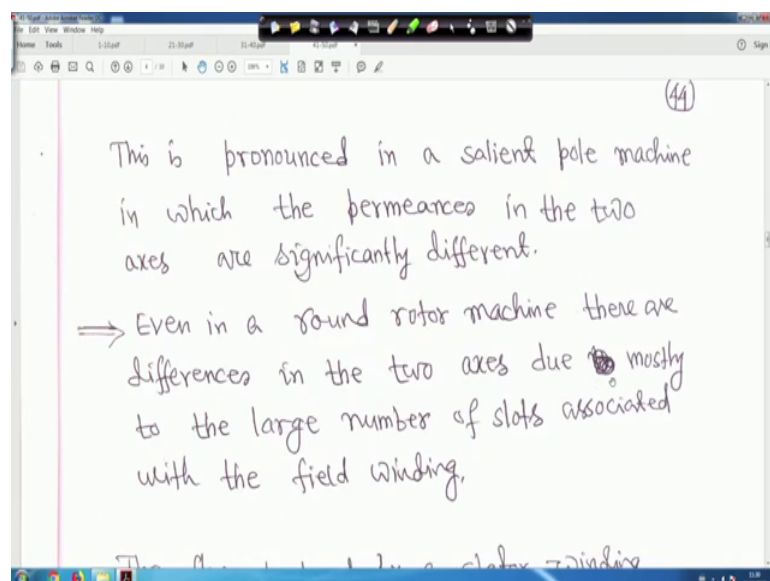
Now, once this is your once this is done, right, then we have to see the basic equations of a synchronous machine, right. So, we will use the generator convention for polarities, so that the positive direction of the stator winding current is assumed to be out of the machine. This when you will write the flux linkage equation these thing should be your in your mind that when we will use the generator convention for polarities, so that the positive direction of a stator winding current is assumed to be out of the machine, right. Therefore, the positive direction of the field and amortisseur currents is assumed to be into the machine, that is your figure – 9, the diagram right I am not going to the diagram, but when we will listen to the video just open the diagram, right.

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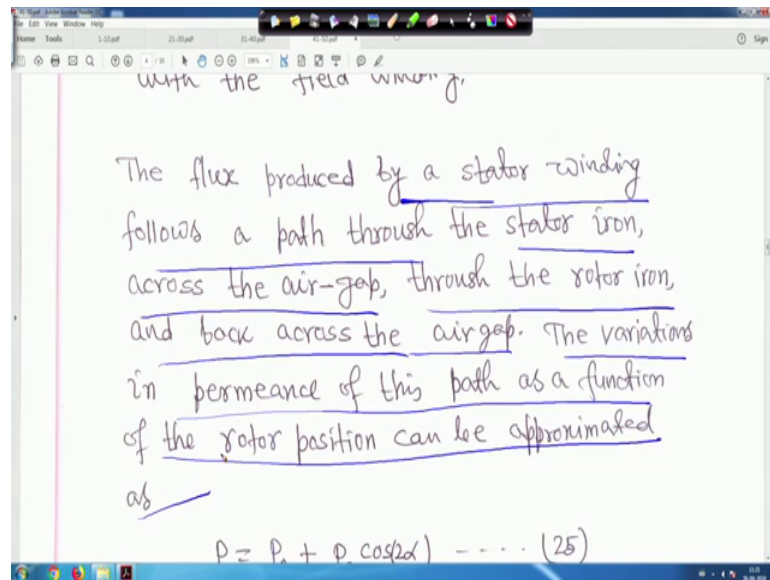
So, in addition to the large number of circuits involved the fact that the mutual and self inductances of the stator circuits vary with rotor position, it complicates the synchronous machine equations, later we will see that, right. So, the variations in inductances are caused by the variation in the permeance of the magnetic flux path due to non uniform air gap, right. So, there permeance also will be vary your what you call it will be a it is not a constant variable and later we will see that will be a double frequency term, right.

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So, this is pronounced in a salient pole machine in which the permeances in the two axes are significantly different right particularly for salient pole machines. Even in a round rotor machines there are differences in the two axes due to mostly to the large number of slot associated with the field winding here also permeance may be different, right.

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Therefore, the flux produced by a stator winding follows a path through the stator iron, across the air-gap, through the rotor iron and your back across the air-gap. So, the actually the flux produced, right by a stator winding follows through the stator iron across the air-gap and through the rotor iron and back across the air-gap, this you have studied for in synchronous machine, right. Therefore, the variations in permeance of this path as a function of the rotor position can be approximated as.

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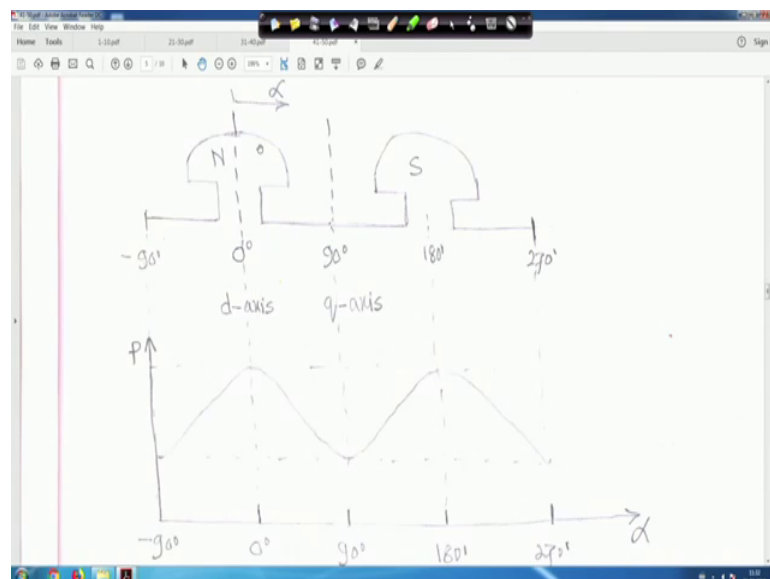
and back across the airgap. The variations in permeance of this path as a function of the rotor position can be approximated as

$$P = P_0 + P_2 \cos(2\alpha) \dots (25)$$

In the above equation, α is the angular distance from the d-axis along the periphery as shown in Fig. 12

So, what we have what we will do is we will approximate this permeance thing that P is equal to P 0 plus P 2 cos 2 alpha. What is alpha? We will through diagram also we will see. So, this is equation – 25, right. In the above equation this equation alpha is the angular distance from the d-axis along the periphery as shown in figure – 12 before these thing this is figure – 12, right.

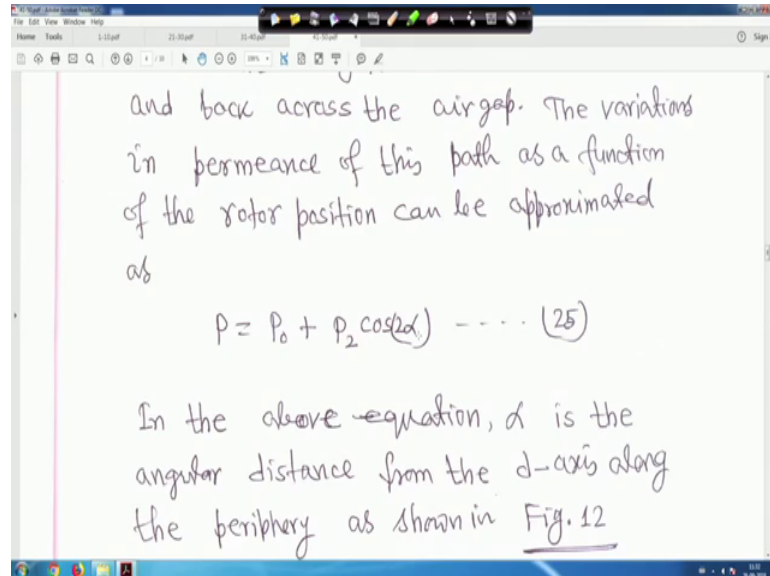
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And, this is your d-axis this is from this one this alpha is measured, right and this is your alpha and this is minus 90, 0, 90 degree, 180 degree, 270, this is N-pole, this is S-pole,

this is d-axis and this is q-axis, right and your and this side is the your plot of permeance, right.

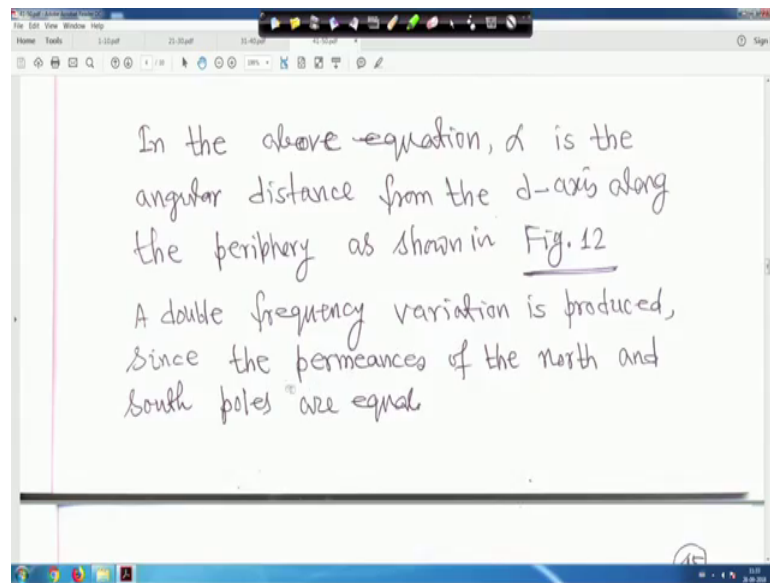
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So, when alpha is equal to if you see this when your if you put alpha is equal to minus 90 you have a cos minus theta is equal to cos theta. So, whatever it will come that is your this is your P plot for you just put alpha is equal to minus 90 degree. Put alpha is equal to 0 degree, right if you put alpha is equal to 0 degree it will P 0 plus P 2, right so, that P, q is actually P 0 plus P 2, right and if you put alpha is equal to your what you call minus 90 degree it will be cos 180 degree, right. So, it will be P 0 your minus P 2. So, this is the minimum, this is the maximum, it is a doubled frequency curve sin your what you call sin curve, right. So, variation of permeance with rotor position so, this is your alpha.

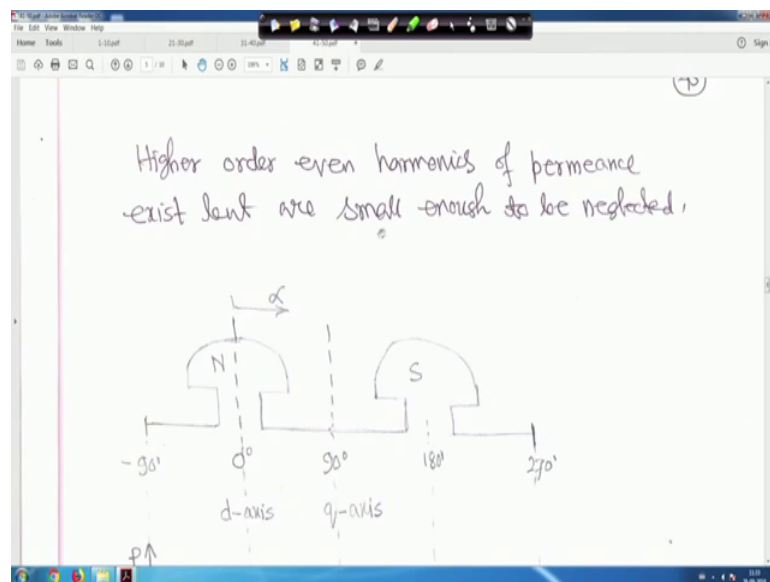
So, that is why this you have taken P is equal to P 0 plus this is you have approximated as well. Derivation, other things we are not going for this course we have assumed that this is valid I mean it is valid actually, right.

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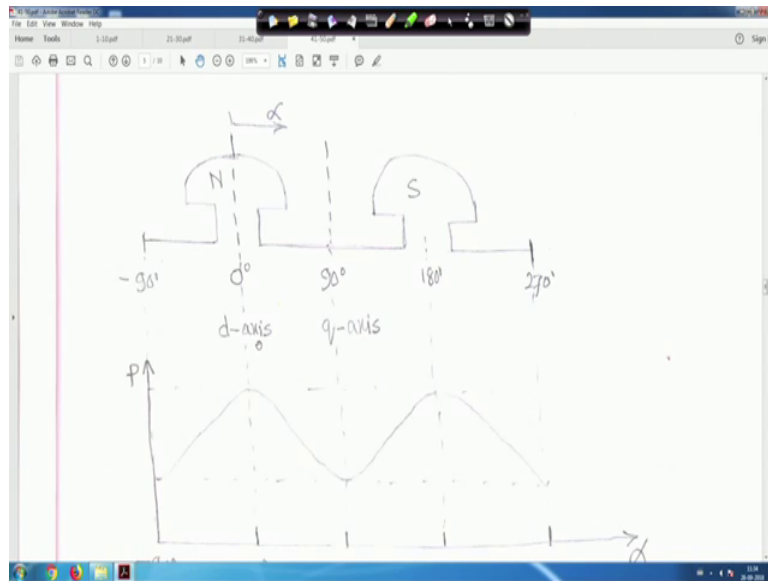
And, so, if you come to this your what you call these thing a double frequency variation just now, I produced since the permeance of the north poles south poles are equal, right.

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So, that is your higher order even harmonics of permeance exist, but are small enough to be neglected. So, higher order harmonics are not considered, right. Even higher order even harmonics right, not considered.

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So, this is your figure – 12, right. This is slightly this is this figure is I hope it is readable right just after 3 – 4 hours lecture, you will find everything is ok, one or two figures are like that because of scanned copy from the photocopy, right.

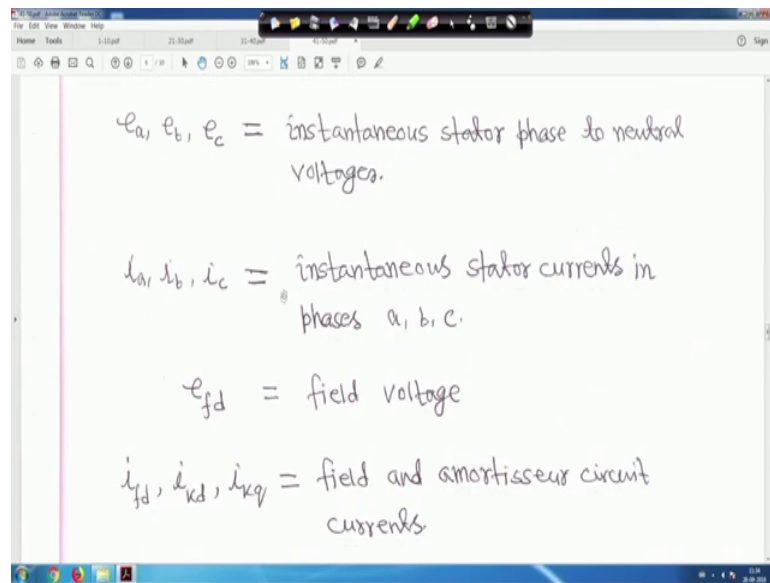
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Fig.12: Variation of permeance with rotor position.

⇒ Following notation will be used in writing the equations for the stator and rotor circuits.

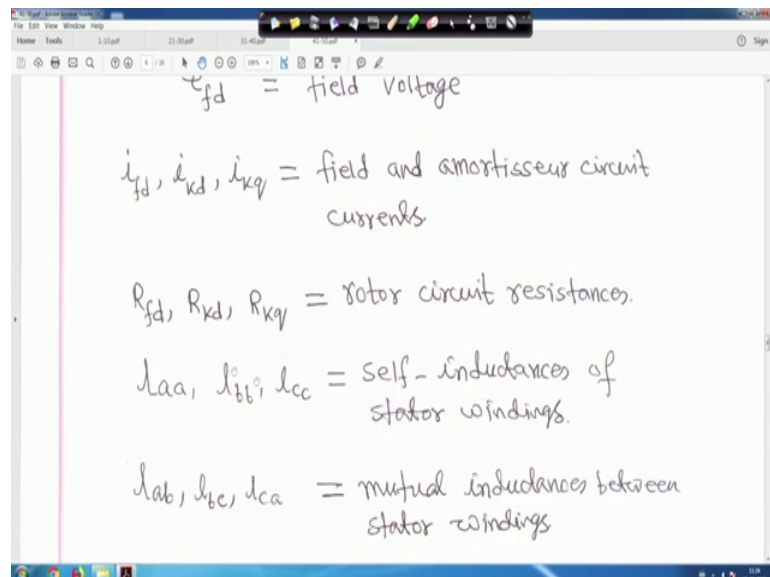
And, following notations will be used in writing the equations for the stator and rotor circuit. So, notation means these are the your nomenclature.

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So, again and again I will not come, but I will tell from these thing that e_a, e_b, e_c is equal to instantaneous stator phase to neutral voltages, right. i_a, i_b, i_c is equal to instantaneous stator currents in phases a, b, c. e_{fd} is equal to field voltage that is DC. i_{fd}, i_{kd}, i_{kq} field and amortisseur circuit currents, right.

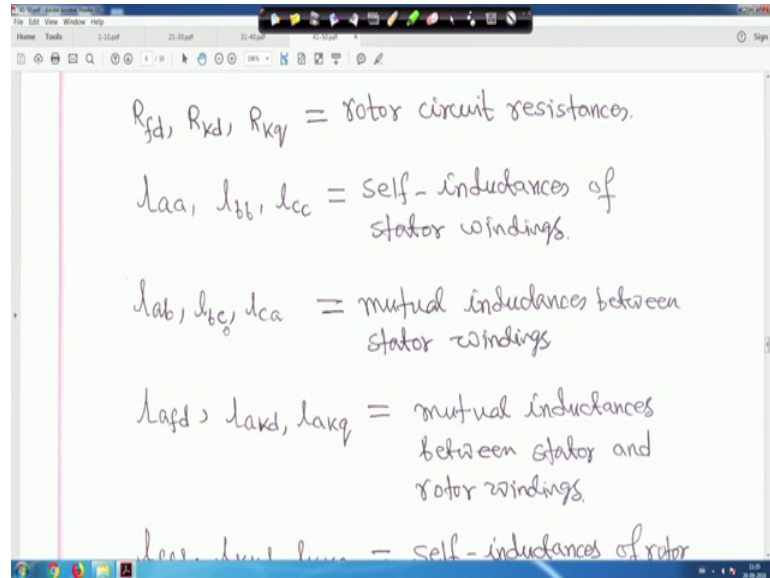
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Then, R_{fd} capital R R_{kd} , capital R R_{kq} rotor circuit resistances; this is field resistance, this is your amortisseur winding on d-axis and amortisseur winding on q-axis

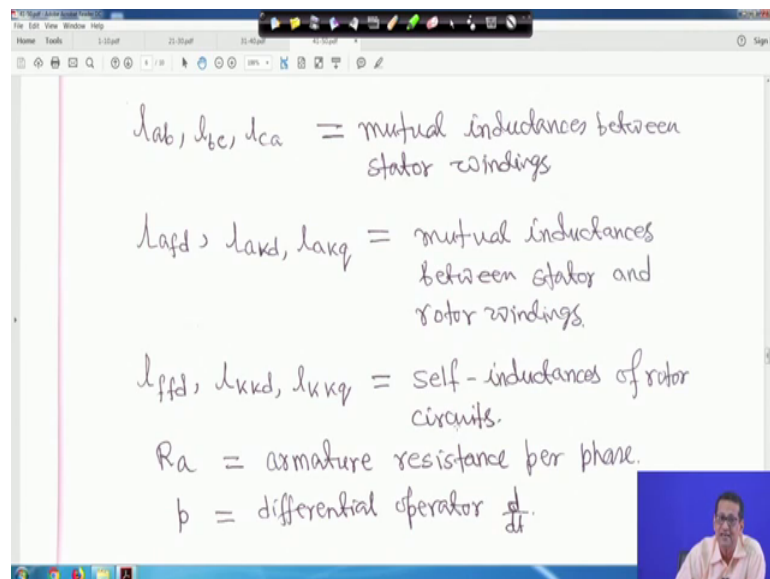
the resistances are. Then small l_{aa} , small l_{bb} , small l_{cc} is suffix it is self inductances of stator windings, right.

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Then small l_{ab} small l_{bc} small l_{ca} is equal to mutual inductances between stator winding, right, then l_{afd} small l_{afd} , small l_{akd} , small l_{akq} is equal to mutual inductances between stator and rotor winding, right.

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Then, l_{ffd} , l_{kkd} , l_{kkq} that is yourself inductances of rotor circuit, right and capital R_a is equal to armature resistance per phase and p is differential operator that is d by dt ,

right because instead of d by dt we will use your p and later you will see many interesting your things on synchronous machine. So, these are all the nomenclature these are all the nomenclature before moving further, right.

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The screenshot shows a presentation slide with the following content:

(47)

STATOR CIRCUIT EQUATIONS

The voltage equations of the three phases are

$$e_a = \frac{d\psi_a}{dt} - i_a R_a = p\psi_a - i_a R_a \quad \dots (26)$$

$$e_b = p\psi_b - i_b R_b \quad \dots (27)$$

$$e_c = p\psi_c - i_c R_c \quad \dots (28)$$

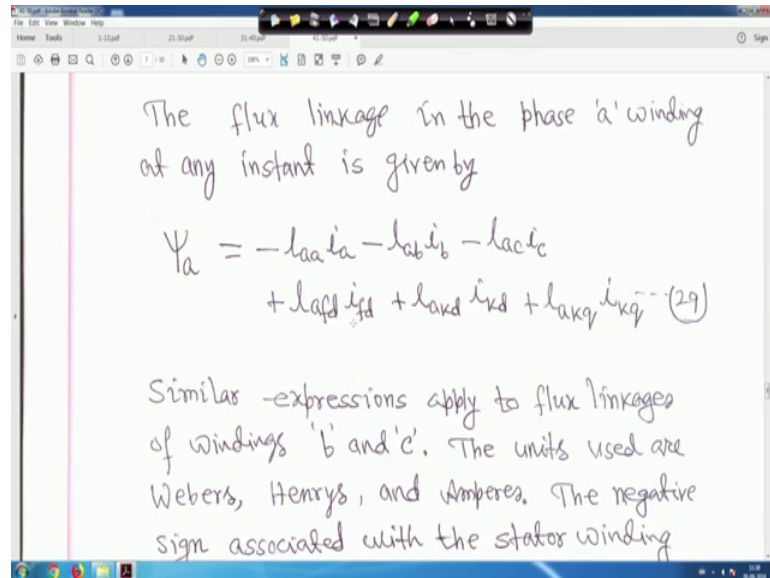
A small video inset in the bottom right corner shows a man speaking.

So, now, stator circuit equations. Now, the voltage equations of the three phases are if you go back to whenever you read these thing I am not going back you please go to figure – 9, right you will and just see this how we are writing this just see this. If you look at the circuit of figure – 9, everything is coming from figure – 9, right. So, I am not going back, right. So, then little bit time we will be save just when you will my suggestion to you when you will read these thing that figure – 9 you redraw, right. For draw the whole circuit or if you have a download and you can have a printout also no problem right and just see this once that how you can write looking at the flux linkage equation and the direction, right.

So, it is basically it will be e a plus i a R a is equal to d phi a upon dt look at the direction of the flux linkage whatever is given and the and the e a, e b, e c, right. So, the polarity; so, e a is equal to then you can write d d psi a upon dt minus i a R a and d by dt is equal to p, right that is your i 2 mention you the differential operator we will take d by dt therefore, this equation you can write p psi a minus i a R a this is equation – 26.

Similarly, e_b is equal to you can write $p \psi_b - i_b R_b$, it is 27 p is nothing where differential operator d by dt , right and e_c is equal to $p \psi_c - i_c R_c$ for phase c , this is equation 28.

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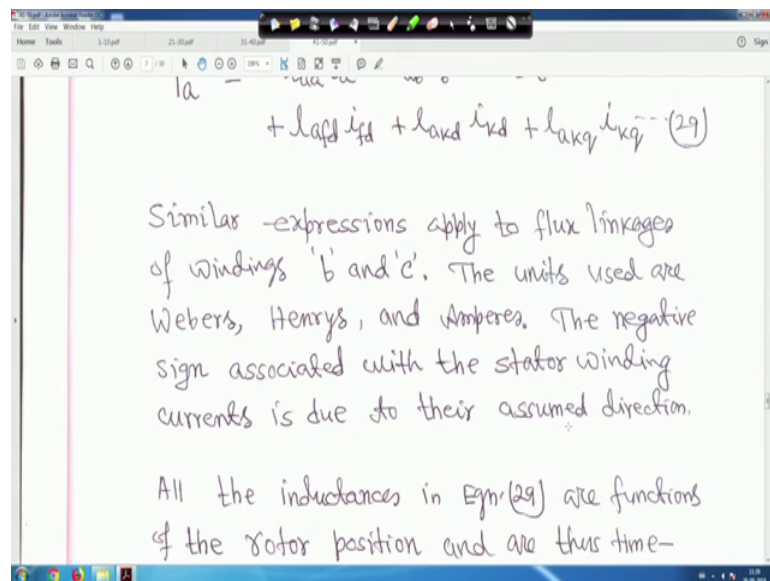


Therefore, the flux linkage in the phase a winding at any instant is given by like this I told you that look at the direction of the flux and I told you once you look at the figure – 9 and the convention we have taken when current leaving the terminal a, b, c we have taken positive direction and for the field winding and for the damper windings on the d-axis or amortisseur winding, on the d-axis or q-axis. When it is entering it we have taken the positive direction and when the current actually leaving the terminal of the stator side that is i_a, i_b, i_c we have taken positive convention and look at the flux linkage in your figure – 9, right just imagine that figure – 9.

So, ψ_a will be it will be you can write it will be minus $L_{aa}i_a$ right then minus the mutual $L_{ab}i_b$ and minus $L_{ac}i_c$, right. Look at the direction of flux linkage and direction of the current the way you have taken your what you call the current leaving the terminal is the positive convention for generator, right, only this part little bit very easy actually very easy actually to write those equations, right. Nothing to be your what you call confused step forward you can write and other is and when you write that all the mutual thing, right that is plus direction because current entering into this field winding as well as current your what you call in the positive direction you have taken.

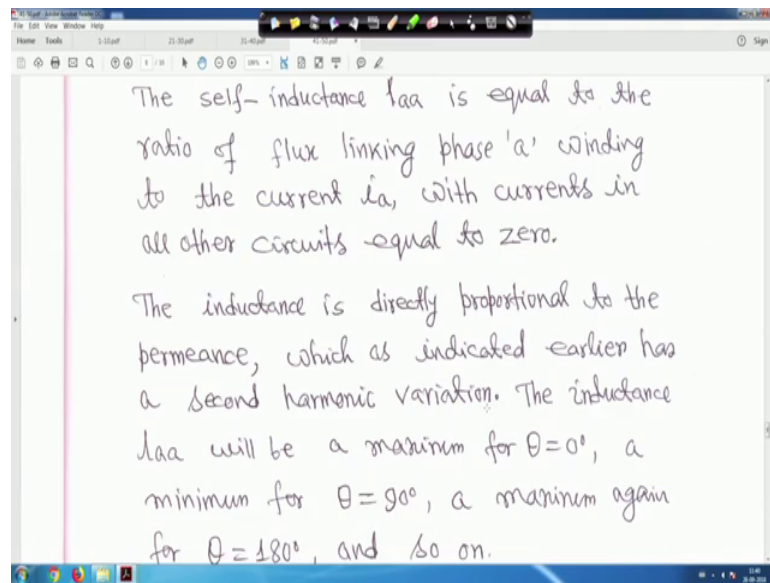
Similarly, for the amortisseur winding on the d-axis and q-axis. So, you can write plus 1 and all the nomenclature is given i_{fd} plus L_{akd} i_{kd} plus L_{akq} i_{kq} this is equation - 29. Similarly, for phase b and phase c you can be written, but we will see later, right. So, similar expressions apply to flux linkage of windings b and c we will see later because we have to consider all, right. The units used are Webers, Henrys and Amperes, right. So, the negative sign associated with the stator winding currents is due to their assumed direction. I just told you, I just told you, right.

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All the inductances in equation - 29 are functions of the rotor position and are thus time varying. So, all these inductances depend on the rotor position and their time varying; that means, this makes things more mathematically more complicated, right.

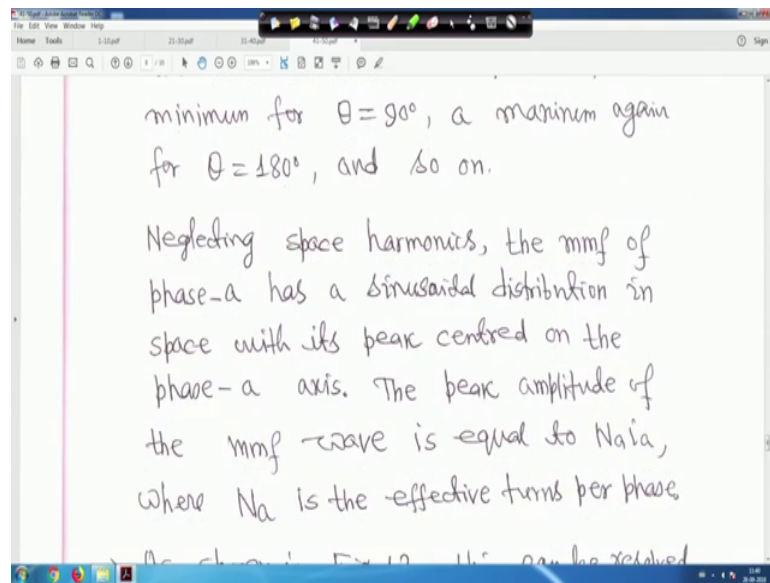
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So, stator now all these things you call the stator self inductances. The self inductance L_{aa} is equal to the ratio of the flux linking phase a winding to the currents i_a with currents in all other circuit equal to zero. Same that is when you when you reviewing the magnetic circuit philosophy is remain same right philosophy is remain same.

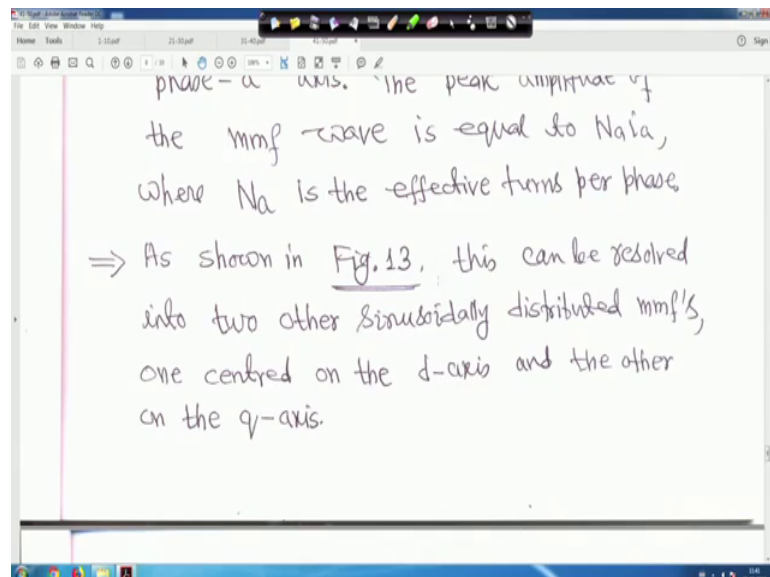
The inductance is directly proportional to the permeance that also we have; that also we have seen which is indicated earlier has a second harmonic variation, right. The inductance L_{aa} will be maximum for theta is equal to 0 and a minimum for theta is equal to 90 degree a maximum again for theta is equal to 180 degree and so on, right.

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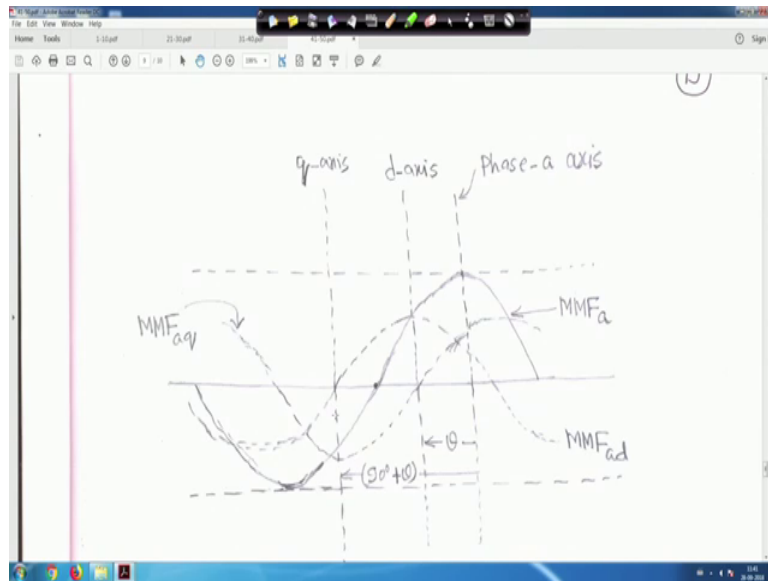
Therefore, neglecting if you neglect the space harmonics, right. The mmf of phase a has a sinusoidal distribution in space with its peak centred on the phase-a axis. Therefore, the peak amplitude of the mmf wave is equal to $N_a i_a$ that is that your what you call ampere turns, right; where N_a is the effective turns per phase so, as shown in figure – 13, right.

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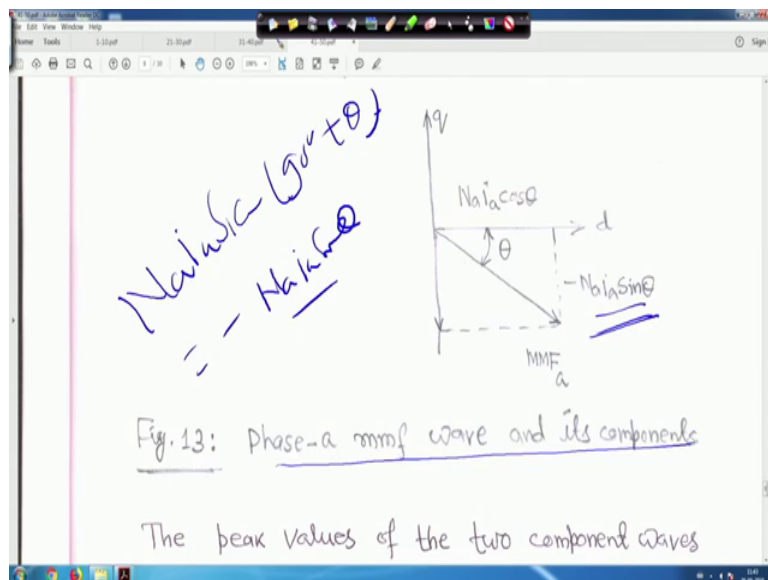
So, this is your as shown in figure – 13. This can be resolved into two other sinusoidally distributed mmf one centred on the d-axis and other on the q- axis.

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Now, these thing is that we know that your what you call that this is my mmf say $N a i_a$, right and their one component is $N a i_a \cos \theta$ another is minus $N a i_a \sin \theta$.

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Now, if you look into this. This is my your what you call mmf for phase a. Suppose, this is the MMF plot, right, this is the MMF plot and you know that from axis d-axis actually leaving the phase a by an angle theta, this. That is why this theta is marked and q-axis leaving this one that is total is 90 degree plus theta, right and this is my MMF wave.

Now, if you have if you just make it the two component. This is MMF your for phase along d-axis and this is another one that MMF that for phase a your what you call MMF that is your two break up we have taken this is MMF a one is along d axis that is MMF ad and this is along q axis MMF aq, right.

So, if you if you look into this that one is $N_a i_a \cos \theta$ because d-axis is leading phase a by an angle θ and q-axis leading phase a by angle 90° plus θ . Earlier we have seen again we will go back to figure – 9, right. Again we will go back to figure – 9, everything is marked there. So, in this case when you write your $N_a i_a$ it is it is you can basically what will become it will become $N_a i_a$ then it is \sin your what you call that one is $\cos \theta$ another is your what you call $\sin \theta$, right.

So, whenever because that is that is your $\cos 90^\circ$ your what you call that your $\cos 90^\circ$ plus θ . So, this side will become your $\sin \theta$ a this one will become $\sin \theta$ a $\sin \theta$. So, $N_a i_a \cos \theta$ and another will be $\sin \theta$ a $\sin \theta$ a $\cos 90^\circ$ plus θ , right that will be your $\sin \theta$ a your $\sin \theta$, right.

So, these two component that is why it is $\sin \theta$ a $\sin \theta$. This is phase-a mmf wave for it is your what you call this is phase-a mmf wave and its components. So, two components your two components for these thing your one is your along d-axis, another is along q-axis. Actually these makes our analysis you will be you know little bit your simpler later we will see that, right.

With this thank you very much. We will back again.