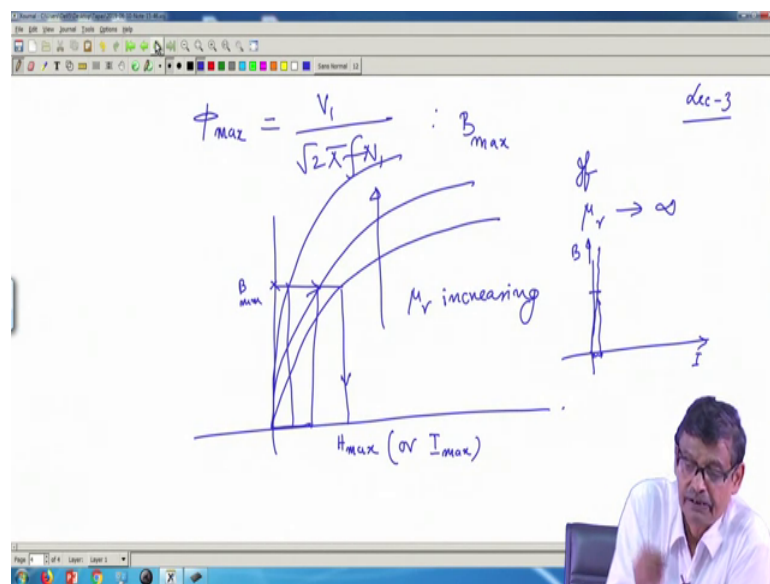


Electrical Machines - I
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Lecture - 03
Ideal Transformer, dot Convention and Phasor Diagram

Welcome to lecture 3. So, in my last class, I was talking about the magnetizing current necessary to create a flux.

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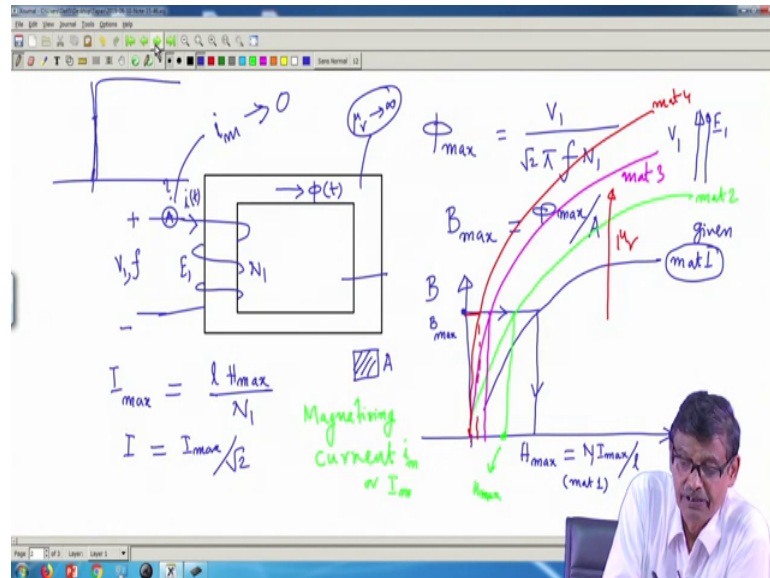


The flux is decided by the supply voltage and I will be writing many a times this. So, that you also become accustomed with this one. So, this is the thing. So, phi max gets fixed and then from this I will be able to calculate B max and from B max then I will say, where is your B H curve? What is the core material? B H curve is like this suppose then corresponding to B max, you read H max. This axis can be for a given value of number of turns and magnetic length l, this can be also treated as I H max or I max. Is not? I can always do that because N by l come as a constant.

So, corresponding to this B max, you get H max, hence I max hence the current drawn from this supply and the another important thing I told if you have better and better magnetic material another material, then the current needed will be only this much not this much have another better material current will be needed this much. So, essentially this mu r is increasing mu r increasing ok. Now, I will be telling you about the ideal

transformer ok. Therefore, if the magnetic material is very highly permeable, if μ_r tends to infinity very large that is this curve will become almost like a vertical line, then to create a flux current needed will be vanishingly small to establish the flux ok.

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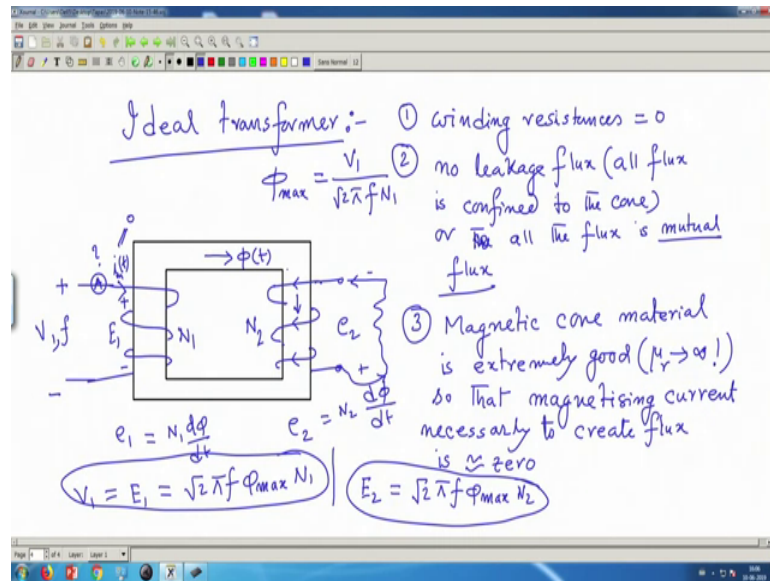


Therefore, we can say that, if this material μ_r tends to infinity what will be the ammeter reading? You think a bit. Ammeter reading will be vanishingly small some finite current is necessary, but that current you can make it as small as possible provided you do not have any restriction on using better and better magnetic material.

Important thing is flux is finite like this, μ_r tending to infinity means that this ammeter reading i_m magnetizing current will tend to 0 that is all, it only means that. No point in telling why 0 current how it can create flux it takes a current no matter how good your magnetic material is, it will definitely take a current, but that current is very small and will see that, it will be very small compared to the rated current of a transformer.

So, like that therefore, in an ideal situation; very ideal situation will say that as μ_r attains to infinity the current drawn that is I and this is B . This magnetizing current drawn can be made as small as possible. So, I will now we are now in a position to talk about ideal transformer ok.

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Now, for the first time I am writing this ideal transformer and if the concept of ideal transformer is clear, you can deal with any situation you can deal with a practical transformer very nicely, because the concepts are so interesting.

So, ideal transformer let us say that the first two conditions remains same winding or coil resistance are 0 winding resistances 0 2 no leakage flux, that is all the flux is confined to the core or all the flux or all the flux is mutual flux of course, this mutual flux what it is I will tell write now. And number 3 is magnetic core material is extremely good μ_r tending to infinity I put a this mark also here means vanishingly small current extremely good.

So, that magnetizing current necessary to create flux is practically 0. These are the 3 properties. Now, it is I will now draw the core of the transformer from my previous diagram, which I have already drawn that is I come here and copy it and then please bear with me till that time, because and is the best; this is the thing. So, this was the thing. Now you see in this it is not a transformer a single coil. So, far I was discussing.

Now what I will do is this; I will draw another coil suppose here is another coil. So, on the magnetic circuit, now 2 coils are connected and this two terminals of this second coil I have not connected anything. Therefore, whatever I discussed in my previous lectures a single coil excited with a voltage V_1 from frequency f remains intact I mean, because

this coil whether it is present or not no one bothers, because nothing have connected no current in this coil.

Therefore, you and suppose this has got a N number of turns N_2 is that clear? Therefore, you have created these then flux is created mind you although you require vanishingly small current, but ϕ_{max} is finite and its strength is this one. That is what? But current needed magnetizing current, it will draw magnetizing current and this current is practically 0. If I assume the magnetic material is of very high quality having very large permeability and all the flux here is confined to the core.

So, what is mutual flux that is what I have to tell you mutual flux is the flux which is common to both N_1 and N_2 turns. So, mutual flux will be the flux, which is confined to the core ok. Therefore, same flux will be linking both the primary coil, this I will call now primary and in this coil no source is connected, this flux is also changing with respect to time therefore, with respect to I mean applying Faraday's law I will then also conclude that these two will become a seat of emf.

So, e_1 is $N_1 \frac{d\phi}{dt}$ e_2 will be equal to $N_2 \frac{d\phi}{dt}$ is not same flux. Rms value of the induced voltage, see polarity of that voltage I have found it out without I mean thinking so, much about that negative sign. I have applied physical (Refer Time: 11:58) and told that if supply voltage at any time is increasing, then flux is increasing this terminal has to become plus and minus so far as even is concerned.

Similarly, and E_1 is equal to root 2 rms value $\phi_{max} N_1$, which of course, happens to be equal to V_1 , because kvl is to be satisfied. Similarly, in the second one; if I say induced voltage in the second coil E_2 in which way it will be different same flux only N_2 comes in therefore, it will be equal to root 2 $\pi f \phi_{max}$ into N_2 that is all. Is not I am not deriving once again differentiating and trying to write. This is going to be what else. So, rms value of the induced voltage in the primary, which happens to be equal to V_1 , because there is no resistance, no leakage flux, V_1 is equal to E_1 .

On the second side this will be this one. Now I should not of course, jump to the conclusion that, this is plus, this is minus will see now that one. So, at a particular instant, if this is plus this is minus, what will be the polarity of this induced voltage e_2 here; e_2 here, whether, this is plus this is minus or this is minus this is plus, that I have to decide ok. The polarity of the induced voltage will be such that, it will try to oppose

the very cause for which it is due, I am repeating the same statement. Means what this flux about this flux, what I told the flux is positive and it is increasing.

Now, there are only two possibilities, either this is plus this is minus or this is minus this is plus, either of one of this is true correct, that way if you think. Suppose I say that, I am not sure, suppose this has happened, when this is plus this is minus this has become plus this is minus; suppose, let us assume it is like that. Now let us verify whether this assumption is correct or not [FL] it has become a seat of emf.

Now you imagine that, this \mathcal{E} I will allow it to act; \mathcal{E} as it is open circuited nothing happens no current etcetera, only thing it has become a seat of EMF and somebody says this is plus this is minus. Now I am telling you that, if it \mathcal{E} is allowed to act on a circuit, then it will deliver current at that instant and what will be the direction of this current? If you imagine that you have connected some loads; some resistance here I will connect it some resistance here.

Then at that instant current supplied by the coil will be like this is not it will go this is the source like a battery current will go like this and the direction of the current in the windings will be like this. Now this is what in accordance with Lenz's law the answer is no why? Because the cause of the voltage induced is that ϕ was increasing is not? ϕ was positive and increasing $d\phi/dt$ was positive that was our assumption.

Now I find at that instant if current flows the flux in the core produced by this current will be; flux produced by core in this coil will be also in this same direction; are you getting? This was the flux created by i_m , it was going up in this direction now also flux. So, the flux is strengthened, the cause for which it is due is strengthened, but that is not in accordance with Lenz's law.

It will try to oppose the very cause for which it is due. What is the very cause? ϕ from top to bottom was increasing. So, the polarity of this induced voltage we will be such that, if this \mathcal{E} is allowed to act, it should pass current through this winding in such a direction, that it will try to oppose this flux that is what has to be. That is therefore, it looks like this is not correct no. So, this cannot be like this, what is the other possibilities? Other possibilities is this has become plus, this has become minus.

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Ideal transformer :-

- ① winding resistances = 0
- ② no leakage flux (all flux is confined to the core) or all the flux is mutual flux
- ③ Magnetic core material is extremely good ($\mu_r \rightarrow \infty!$) so that magnetising current is \approx zero

Diagram: A transformer with primary turns N_1 and secondary turns N_2 . Flux $\Phi(t)$ is shown circulating in the core. Primary voltage is V_1 and secondary voltage is V_2 . Induced EMFs are e_1 and e_2 .

$$\Phi_{max} = \frac{V_1}{\sqrt{2} \pi f N_1}$$

$$e_1 = N_1 \frac{d\phi}{dt} \quad e_2 = N_2 \frac{d\phi}{dt}$$

$$V_1 = E_1 = \sqrt{2} \pi f \Phi_{max} N_1 \quad E_2 = \sqrt{2} \pi f \Phi_{max} N_2$$

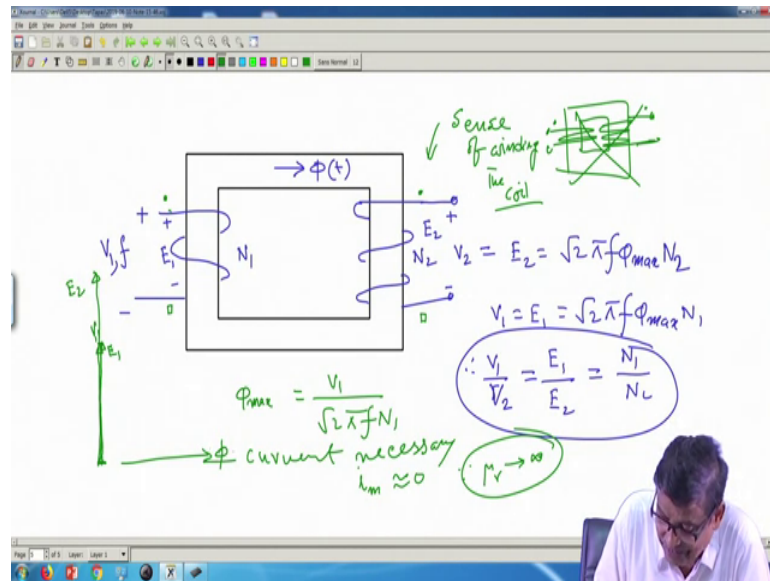
Let us see, whether this will be consistent mind you this is the continuous thing I have been only corrected no.

Student: Ok.

What is the other possibility? This is plus this is minus is it consistent? Let us see, if this emf is allowed to act on its own to an external circuit like r you have connected, then at that instant it will try to send current in this way. Because this is battery it is the source, current comes current goes current goes current goes like this current goes. So, this coil, when it delivers current it will create flux in a direction opposite to these phi t which has been created by this one.

So, it is trying to oppose the very cause for which it is due. Therefore, at a given instant of time, if this terminal is plus this terminal is also plus. Let me repeat this point in a Nicer diagram; it is like this.

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So, let me sketch it that will be faster. So, I sketch because let us spend some time on this; sorry, I have not selected I will cut it out. See so, let us do it like this, suppose this is your. Now I had got 2 coils let me repeat this point emphasize this point. This is suppose one coil have been N_1 turns, this is suppose another coil with N_2 turns, you have applied I will not just simply say that you have applied V_1 rms voltage of frequency f with this is plus this is minus.

E_1 has appeared here, it will have polarity like this here also I applied the Lenz's law and the flux in the code is $\phi(t)$. Then this two terminals also become a seat of emf. The value of this voltage V_2 is nothing, but E_2 only V_2 is the terminal voltage there is no distinction between E_2 and V_2 right now.

So, V_2 is equal to E_2 is equal to $\sqrt{2} \pi f \phi_{max} N_2$ and also I know V_1 is equal to E_1 is equal to $\sqrt{2} \pi f \phi_{max} N_1$, this is N_2 sorry and this is N_1 and it is easy to show that $V_1/V_2 = E_1/E_2 = N_1/N_2$. This is one famous formula ok. So, that is the thing, but I was discussing about the polarity of this induced voltage instantaneous polarity.

If at any instant of time this is plus this terminal as to become plus no way; the other possibility that at that instant this is plus this is minus will violate Lenz's law and this ratio of this voltage is this one and from this many things can be told it is merely the ratio of N_1 by N_2 manipulating this ratio N_1 by N_2 you can step up the voltage this is

called secondary coil or step down the voltage depending upon, whether N_2 is greater than N_1 or N_1 is greater than N_2 depending on that.

But anyway, this is the thing. Now people use you know some dot marking to communicate this particular important aspect of a transformer by using known as dot convention. It merely tells you that any given instant of time, if the polarity of this induced voltage is this is plus, induced voltage in the other coil instantaneous polarity will be also this is plus and this is done by dot convention.

Now I must also point out see, I have drawn the core material and drew the coils primary coils and the secondary coils rather carefully. What do I mean by carefully; that you can draw suppose you have a magnetic circuit like this as a you draw the coils like these. It is for better than this, what I mean to say that this coils I have drawn. So, that you know what is the sense of the winding, you take the coil this way then turn it like that, but from this sense you cannot figure out, how this coils went somebody draws like this.

Then of course, you cannot point out if this is dot which one is dot this side. No out of question you cannot do that. Perhaps by doing some experiments you will be able to do, but as such on pen and paper you cannot predict ok, this is plus this will be plus that you can only do provided you know the sense of the winding; sense of winding the coil. If that is meticulously shown, then you can figure out. [FL] Before I tell some more interesting thing; also you note that if these two are dots after some time; you know because it is after all AC supply, it will be better if we say dot terminals are those terminals which have like polarities of the induced voltage.

For example if you say this is plus this will be plus, you rub this off for the same transformer I am talking this point you listen, suppose this dot I remove if somebody says no this is dot. Then also he is correct are you getting like terminals, if it is minus that will be minus whenever it will become plus because polarity reverses this will be also plus.

In other words, what I am telling no point in showing so many dotted it is understood that, wherever you have shown dots; good enough other two terminals are also like terminals you can put some square brackets to indicate that. They are like terminals they are like, whenever this is plus this will be plus, whenever this is plus this will be plus, whenever this is minus this will be minus and so on like that.

So, we have we had discussing about ideal transformer and the ideal transformer is that transformer, who which requires vanishingly small magnetizing current to create a finite flux of strength V_1 by $\sqrt{2} \pi f N_1$ is not current necessary, that is magnetizing current is vanishingly small 0.

Since, μ_r is infinitely large, that is the idea. Apart from the fact that all flux is confined to the core there is no winding resistance, which allows me to write V_1 is equal to E_1 RMS values is equal to $\sqrt{2} \pi f \phi_{max} N_1$ and the last thing I will tell in this class, then if I draw the phasor diagram, what should I draw this is the applied voltage is not?

Let me just draw it give you some idea, then the current drawn; magnetizing current drawn although vanishingly small it will be lagging 90 degree. So, magnetizing current will be along this line, because after all pure inductance it has got only inductance; inductance value is very large if μ_r is tending to infinity we have shown wrote some expression for inductance, if μ_r goes to infinity inductance goes to infinity, you can now interpret the things from different angle inductance point of view very large μ_r , but the current drawn from the supply will be 90 degree lagging and this length is pretty small 0, so, this V_1 .

So, primary current is this where is E_1 ? E_1 will be also like this same as these one and where will be E_2 same, because same $N \frac{d\phi}{dt}$. So, E_2 will be also like this, all voltages induced voltages, applied voltages this is V_1 they will be all in time phase and this is the direction of ϕ . Why ϕ ? Because ϕ is proportional to i_m although i_m is vanishingly small, but it creates a finite flux. So, flux phasor will be along this line. We will continue with this in the next lecture.

Thank you.