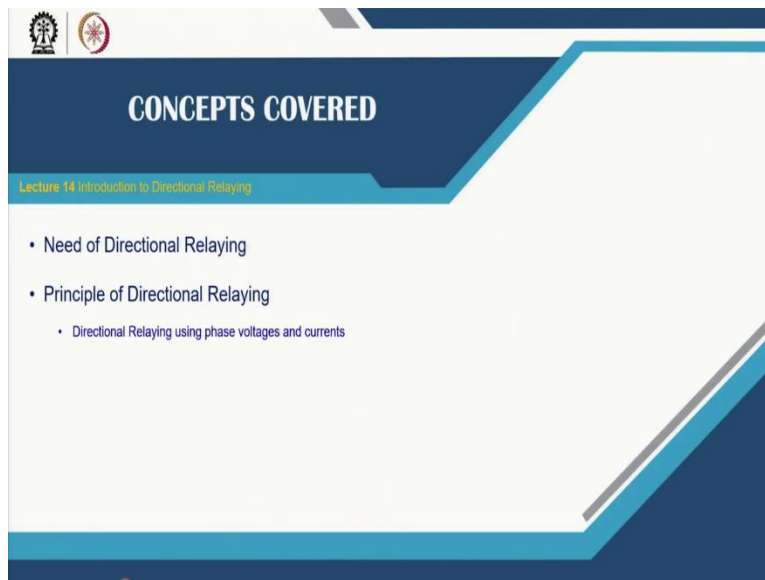


**Power System Protection**  
**Professor A K Pradhan**  
**Department of Electrical Engineering**  
**Indian Institute of Technology, Kharagpur**  
**Lecture 14**  
**Introduction to Directional Relaying**

Welcome to NPTEL Power System Protection course. In module four, we will talk on directional relaying.

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In this lecture we will see how directional relaying is being applied in different protection schemes. The basic protection philosophy for directional relaying and there are different ways to address the directional relaying perspective. We will go one by one. Today we will talk about the phase quantity-based direction relaying principle.

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Requirement of Directional Relaying

A Single-phase system

For a fault at  $F_1$

Current (kA)

Time (s)

Fault inception

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Requirement of Directional Relaying

A Single-phase system

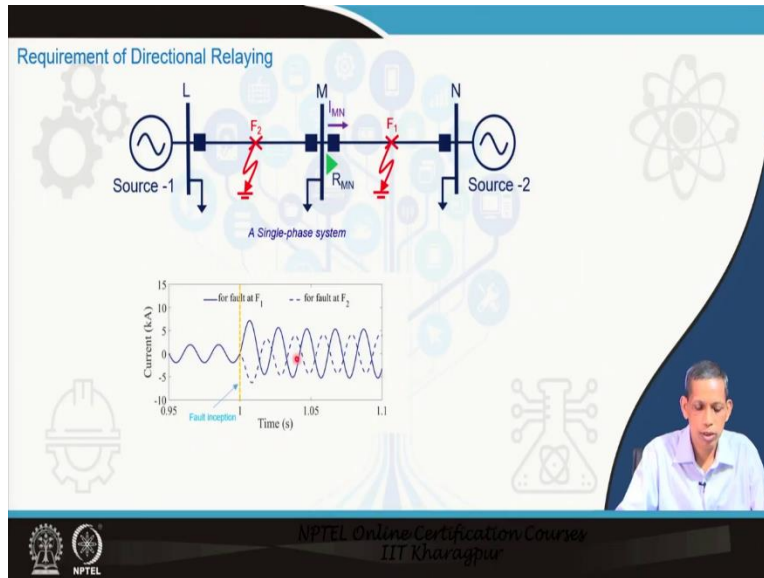
For a fault at  $F_2$

Current (kA)

Time (s)

Fault inception

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Before going to the directional relaying, we will see the need of directional relaying. How does it help in protection schemes? So, if we see this simple system. Now, as compared to earlier cases, we have sources at both the sides, so this is no more radial. So, power can flow from left to right or right to left, we can think about a tie-line connection at transmission level also.

But first, consider a single-phase system for understanding. We will extend this idea to generic three phase system. Let us consider a fault happens to be there at  $F_1$  positions between M and N line. So, at that time, current will flow from source one like this and also current flows from source two to the fault point like this. So, this current as you know becomes also very high and at that time, the objective of the protection scheme is that the breaker at this and breaker at these at the end must be open.

So, the fault is clear from both the ends otherwise current will flow and that is not desirable. Now one may say that we will trip this breaker here from this side also that means that the load at this also will be hampered. So, from selectivity point of view, part  $F_1$  fault here, we essentially say that the breaker at M bus, this breaker and this breaker should trip, that is the desirable things for the protection scheme.

However, in case of a failure of the breaker at this point, the backup against that breaker here should operate. Now, on this perspective you can say that if the relay for the corresponding breaker at this point designated at  $R_{MN}$ , the current during this fault as seen by the relay for a fault at 1s

inception then the current becomes like this and the current becomes higher following through a transient decaying DC component and so.

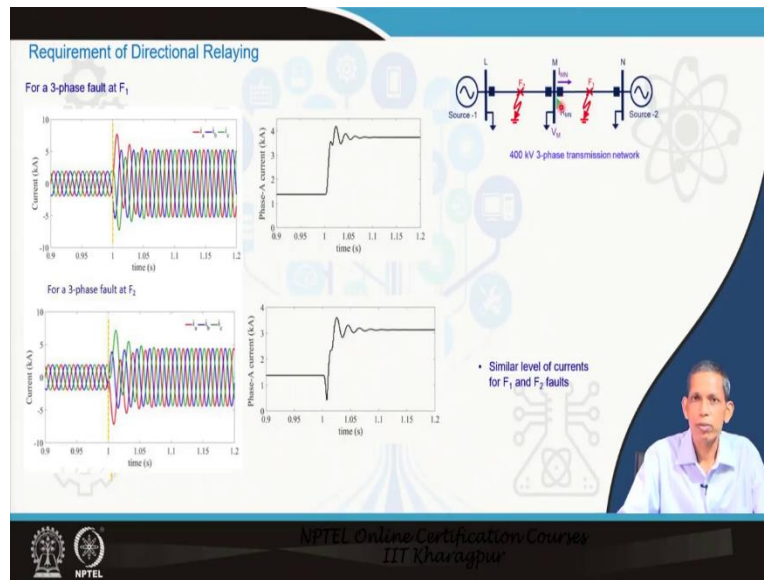
So, this is what for the single-phase system or fault at  $F_1$  the current which will be observed by the relay at bus M, the  $R_{MN}$  relay which is being assigned we can say that for this breaker. Now, let us come to this another fault, fault at  $F_2$  in line MN in the same single phase system, now current flows to this fault  $F_2$  like this from left hand source and from the right hand source. At this point the desirable thing is that the breaker, this one and this one should be open.

Now, how does this relay at M, same relay what we have earlier discussed, how does it see, so now the current which will be seen, you see here now flows from right to left for this relay and that is what is shown here, that the current now changes in different way for a fault  $F_2$  as compared to  $F_1$ . So, this is what you can say that for the two fault cases, one in  $F_1$  this side and one in  $F_2$ .

Now, if you mark this to consideration, assuming that you can say that the corresponding both the faults happen at the same fault inception point 1s here. This is some simulated data for understanding purpose. So then if you plot the two currents, fault currents become like this, the solid line for the  $F_1$  fault and the dotted line for the  $F_2$  fault and both the currents are observed by the relay  $R_{MN}$ .

So, we observe that you can say that for  $R_{MN}$  for  $F_2$  fault the current become reverse as compared to for the fault for  $F_1$ . That is what if you see these two currents that there is a phase separation between two currents  $F_1$  fault and  $F_2$  fault. This is what we observe from this simulation plots for the two currents.

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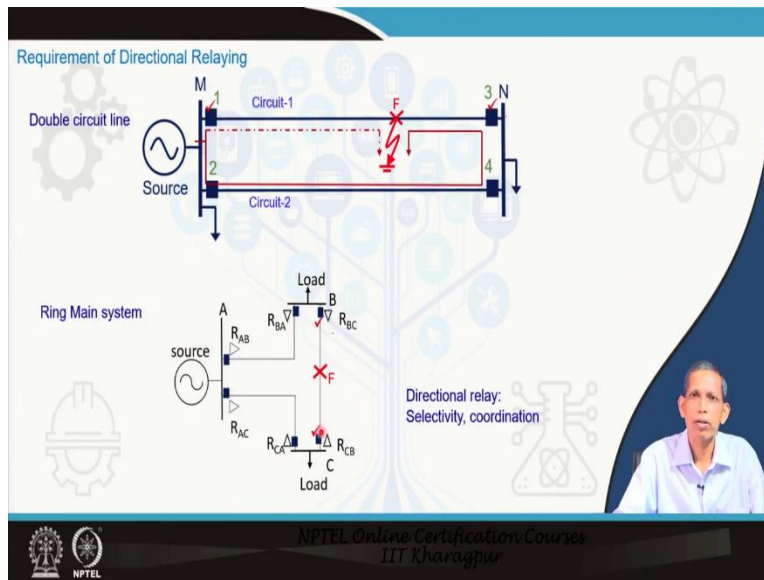


Now, we can extend this idea to the three-phase system. So, this is 400 kV three phase transmission network, part of the big network, and this interconnection one, so source one and source two, similar to what we have discussed earlier in the single-phase case. There are two faults  $F_1$  and  $F_2$  and we are observing the  $R_{MN}$  relay.

So, if we see that same, the corresponding fault we can say that is being created at 1s and then we see that the corresponding three phase faults are there at  $F_1$  and  $F_2$  site and we see you can say that the corresponding current magnitude for both the faults to be very high. So, what we say from the earlier discussion that in both cases for  $F_1$  fault  $F_2$  fault, whether it is single phase or three phase the current magnitude becomes significant. Therefore, the relay  $R_{MN}$  only trip this breaker in case of  $F_1$  not for in case of  $F_2$  from selectivity point of view. The relay  $R_{MN}$  cannot distinguish from magnitude of fault current. So, we have learnt till now, discrimination of faults in different sections using current over current principle.

Now, what you see that the overall current is full of limitations here that this relay has to discriminate whether the fault is this side or the fault in this side simply a fault in  $F_1$  direction or in  $F_2$  direction. Accordingly, this has to trip or not to tip the corresponding breaker. So, for that we conclude from this discussion that only current magnitude based over current relay cannot distinguish that, and that is what we like to say that for such discrimination directional relaying is required, direction what we mean here is that direction of fault.

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Let us see you can say that how these corresponding directional relaying is beneficial in discriminating practical systems. Consider a double circuit line and the source, substation side is this and the double circuit line and it is feeding to different loads for further section. So, we have four breakers here, the region behind then the fault happens to be there in any of the line let us say circuit one at F. So, this breaker 1 and this breaker 3 should open, so these lines will be out, the other lines still remain functional so that some of the loads here can still be supplied.

So, that is what the benefit of reliability from that perspective, we say that the breaker 1 and breaker 3 should be open for fault F in the circuit one. Now, see what happens during the fault condition. So, for fault F from this source, current flows like this and another path of current is from here to here. So, what you observed because this is a fault condition the current magnitude will be significantly high.

Therefore, relay at one, relay at two, relay at four and relay at three all will see large amount of current, so over current relay will see there is high level of current and it is go for decision depending upon the coordination but what you need in this case that for this fault only one and three should trip, not two and four. So, to resolve that, we can use your directional principle, we will have a directional relaying at bus three. So, what will happen here if in addition to over current relay, if you put a directional relay here then if we see here the normal flow of current direction for the relay at three is this but now whenever a fault happens to be in circuit one, the current

direction is reversed. So, that is what a discriminating function perspective to know the direction of current, and that gives you the direction of fault. Furthermore, if we put a directional relay here, then that gets discriminated that the fault is in the line section or not. Thereby we can say that we can have a coordination at our current level between one and three. So, relay at bus three can trip fast and then you can say that once three opens here the breaker then no current from this side. So, this circuit does not have any current, and this current still may be flowing at a later time coordinated with three, this can be open.

Therefore, we see that in such a situation for the double circuit line or parallel line for the selectivity point of view directional relaying is a requirement. Now come to Ring main system, which we have already discussed in over current coordination, same system we have considered. So, we see you can say that there are different breakers. Now let us consider you can say a fault in this line B to C.

So, what will happen that current will flow from this side and also current will flow from this side but the objective from the protection perspective is that the breaker at here and breaker at here should open, not the any other breaker. That is the primary protection level. Therefore, relay at this and relay at this must see this fault. Note that all the relays should trip the breakers they will observe large amount of current. So, their overcurrent will trip and that is not desirable. So, only requirement is that relay at here and relay at here should be there and this discrimination can be achieved using directional principle. So, we will see you can say that more details. How we can you can say use the different directional principles to employ different nodes, different points for satisfying the different protection needs.

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The slide is titled "Applications of Directional Relaying" and is part of an NPTEL Online Certification Course from IIT Kharagpur. It features a background with a stylized tree of icons representing various engineering and technology fields. The text on the slide is as follows:

**Applications of Directional Relaying**

**In distribution and transmission systems**

- With overcurrent relay
- High speed transmission protection
- To supervise distance elements
- Used for earth fault protection when selectivity is required

67 - AC Directional Overcurrent Relay  
67G - Ground Directional Overcurrent  
67P - Phase Directional Overcurrent

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Directional applications are quite wide. This is being widely used for the distribution and transmission system protections, supplementing overcurrent relay, high speed transmission protection at high voltage level to supervise distance relaying, will see more details on the distance relay, also used for earth fault protection when selectivity is required that also we will see along with the transformer protection and so.

The common IEEE standard numbers for the directional overcurrent relay in an alternating current system is 67, ground directional overcurrent relay is 67G and phase based directional overcurrent is 67P. They are to these 67 directional overcurrent relays that are other variance also we will see that later on.



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The slide, titled "Principle of Directional Relaying", explains the concept based on the angle between phase voltages and currents. It states that transmission lines are predominantly inductive. Two bullet points describe fault conditions: for forward line faults ( $F_1$ ), current  $I$  lags voltage  $V$  by the fault loop impedance angle  $\phi$ ; for reverse faults on the adjacent line ( $F_2$ ),  $I$  leads  $V$  by approximately  $180^\circ$  minus the fault loop impedance angle  $\phi$ .

The diagram shows a three-phase system with Source-1 at bus L and Source-2 at bus N. A relay  $R_{MN}$  is located at bus M. Faults  $F_1$  and  $F_2$  are indicated on the lines between L-M and M-N respectively. A phasor diagram at bus M shows the polarizing voltage  $V_M$  as a reference vector. For a forward fault ( $F_1$ ), the fault current  $I_{MF1}$  lags  $V_M$  by angle  $\phi$ . For a reverse fault ( $F_2$ ), the fault current  $I_{MF2}$  leads  $V_M$  by angle  $\phi$ .

A graph shows the current  $I$  (A) versus Time (s) for faults at  $F_1$  (solid line) and  $F_2$  (dashed line). The  $F_1$  current lags the  $F_2$  current.

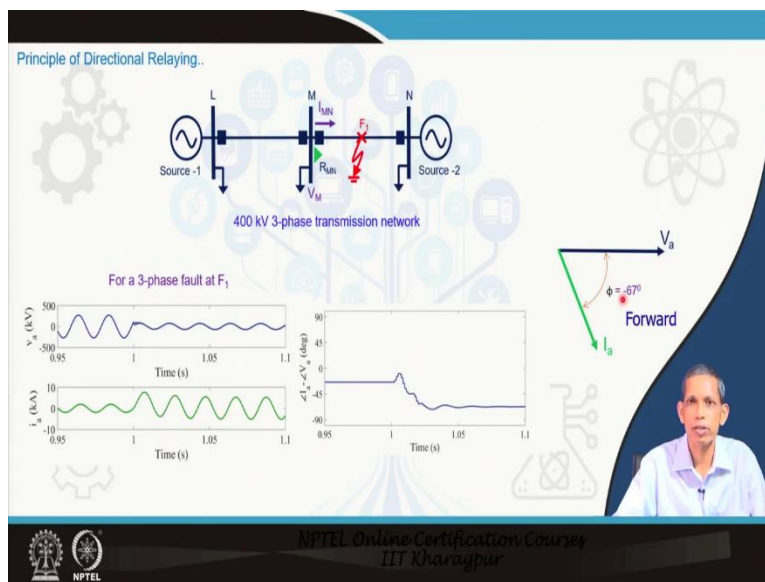
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Now, we go to the principle one by one. So first we will go to we can say phase quantity based directional relaying principle. So, we know we can say that transmission lines are predominantly inductive  $R / X$  ratio is low and the angle impedance angle is pretty substantially high,  $80^\circ$  and above and so. Now, see this system we can say that as we have already seen, source-1 and source-2 we have already known that for these relays, for fault at  $F_1$  and fault at  $F_2$  the corresponding current patterns becomes like this. So, we like to know now how this corresponding relay at this will be able to discriminate whether the fault is  $F_1$  side or  $F_2$  side. That discrimination is nothing but here a two class problem for this is to be achieved using the voltage and the current signals available at the relay point. So, to achieve this let us see you can say that how we can go with that so first as I had mentioned we will go with phase quantity based approach and then we will extend this idea for other options also. So, we see here you can say that at  $V_M$  at the bus M,  $V_M$  that is reference, a fault happens to be in  $F_1$  so current from left to right, this impedance path is highly inductive.

Therefore, the current you can say that flowing through these, this relay  $I_{MN}$  for fault  $F_1$ ,  $I_{MF1}$  at  $F_1$  will be lagging to this voltage at this relay bus and that is what the lagging current is. Now, this is the solid line current we talk about. Now, in case of  $F_2$  fault, same relay will now see a current flowing from right source to the fault point. Therefore, the relay can see the reversal of current with respect to the earlier case.

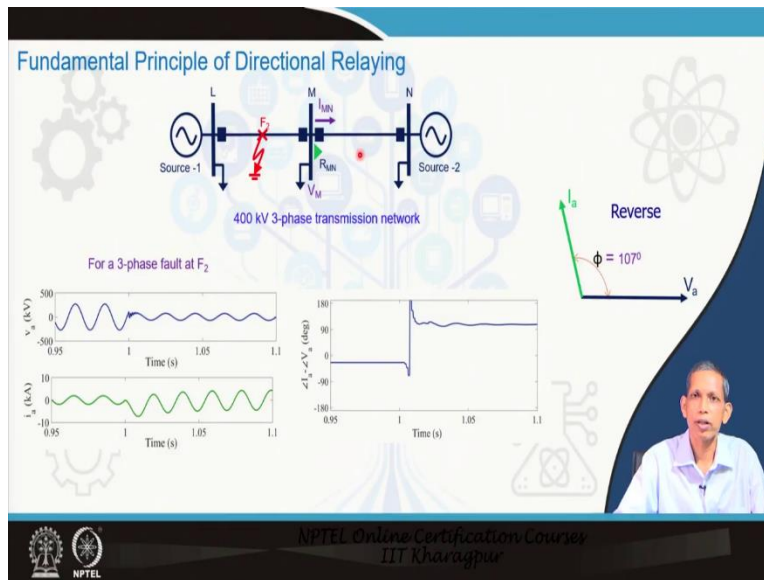
So, that is what a reversal of current we are noticing with the dotted line. Therefore, the reversal of current for  $F_2$  becomes this  $I_{MF2}$ , and that is what with respect to  $V_M$ , this will be a leading current. This implies that the relay at here can discriminate this  $F_1$  fault and  $F_2$  fault using the phase current and the phase voltage and the associated angle. In case of  $F_1$  the forward fault we call it as forward fault, forward looking relay for this line protection of MN. For this forward fault the corresponding current lags the voltage by certain angle and in case of reverse fault that is  $F_2$  side fault the corresponding current noticed by this relay leads the voltage. That is what the conclusion we have from this slide.

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Now, going to a three-phase system if we see this corresponding three phase fault, so all faults are involved. So, this is  $V_a$  voltage signal. This is the current signal compute the phasors then you get the corresponding angle between current and voltage, angle of current minus angle of voltage because you are taking voltage as reference  $V_a$  where only concern now about the phase A voltage and current because we are trying to discriminate this direction of fault using phase voltage and phase current. So, with  $V_a$  as reference at bus M, the current here lags for this  $F_1$  fault so the current here lags and for this situation if we see the corresponding current obtained you can say is  $67^\circ$ . So, angle of  $I_a$  minus angle of  $V_a$  that comes out to be minus  $67^\circ$  that is what the  $\phi$  angle.

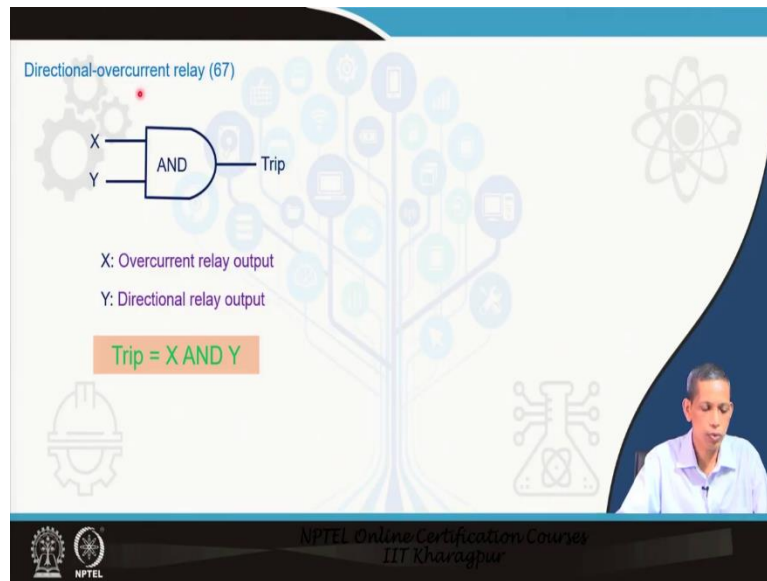
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Now, when you go to  $F_2$  fault for the same 400 kV system, fault now is in reverse direction so current flows from here to here. That is what notice from this current pattern with respect to this  $V_a$ , at bus M for this relay. So, the angle of  $I_a$  minus angle of  $V_a$  that it comes positive now as you have already seen. So, we have already done  $V_a$  the phasor, the phase fault is at bus M and the  $I_a$  is leading and the angle comes out to be  $107^\circ$  and this  $\phi$  is a positive value. So, this is the reverse fault for this relay and that angle comes out to be positive.

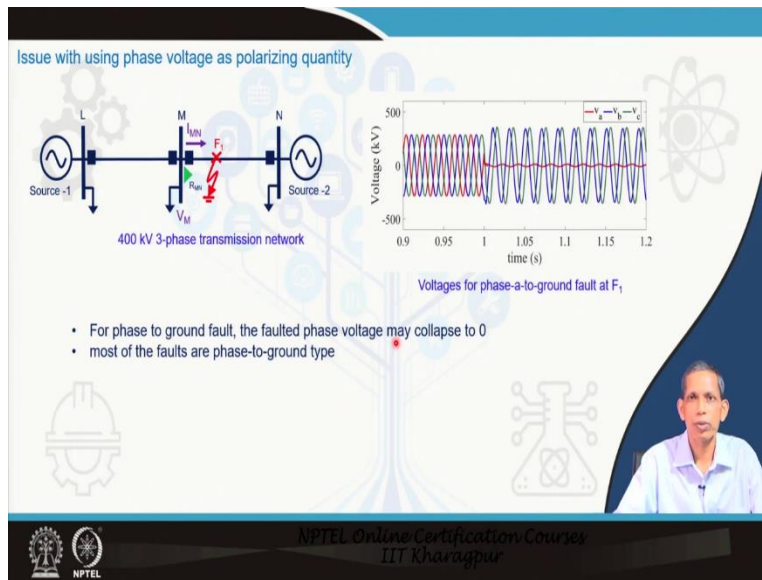
The way we have computed here can be different options also for that perspective. The angle we have computed it angle of  $I_a$  minus angle of  $V_a$  whichever phase is involved with fault. Take that current phasor angle of that current phasor minus angle of that phase voltage will be indicative of the direction of fault. If that angle comes out to be positive, we say the fault is in reverse side for the relay. If that angle comes out to be negative, then we call the fault to be forward fault.

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These kinds of principles in directional relaying is being widely used with overcurrent relays as I mentioned and that is designated by IEEE standard number 67. What is being done in directional overcurrent relay principle that the decision by the overcurrent and the decision by the directional we have a AND circuit and by and operation that we decide whether to trip the corresponding breaker or not. That is been that the trip decision is the decision by the X, the overcurrent and and the decision by the directional relaying. So that is what we talk about directional overcurrent relay while using in distribution and at transmission level.

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However, this phase voltage and phase current based relaying principle has certain problem. Let us observe this. So, for this three phase fault  $F_1$  in this transmission system, if the faults comes out to be very closer to this one and this source is strong and this line is not long, then phase voltage here collapses and that may substantially having a lower value. That is what we observe here as compared to other phase voltages, the corresponding voltage is significantly low because of the fault being closer to the relay bus.

In that case the corresponding voltage being substantially low because of the other uncertainties and all these things. If phasor will not be reliable and therefore this corresponding associated angle of the phase voltage  $V_a$  and angle of  $V_a$  cannot be consider for reliable directional relaying principle. We know that most of the faults are line to ground faults. So, as already mentioned phase voltage and phase current can be used for directional relaying. If you use the corresponding phase voltage, for a line to ground fault the corresponding voltage may be substantially low and there may not be a reliable option for that one.

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Solution: Quadrature Voltage directional elements

- To resolve the low voltage issue, quadrature voltages (i.e.,  $V_{bc}$  vs.  $I_a$ ) are commonly used.

90°- phase directional elements

Phase	Operating Quantity ( $I_{op}$ )	Polarizing quantity ( $V_{pol}$ )
A	$I_a$	$V_{bc}$
B	$I_b$	$V_{ca}$
C	$I_c$	$V_{ab}$

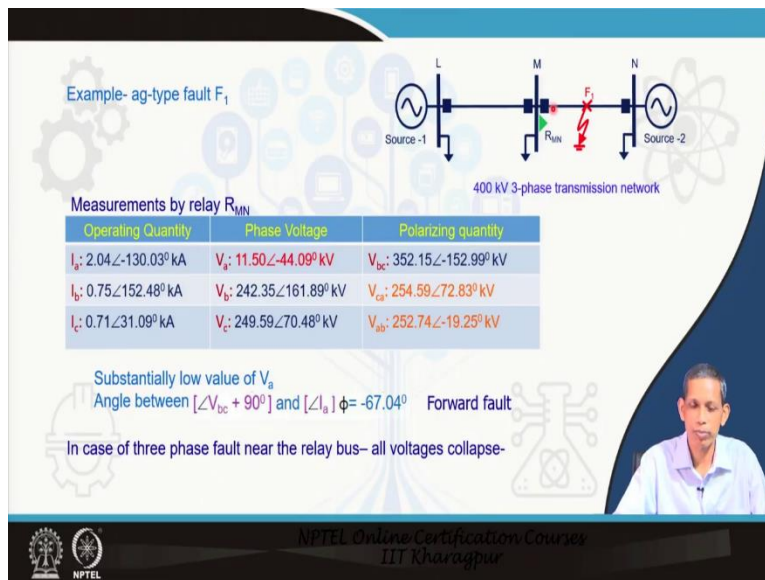
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In that scenario, we have alternatives so for that what we do is that we use the quadrature voltage directional element. What do you mean quadrature here that because most of the faults are line to ground faults say AG fault phase A to ground fault. Then instead of taking  $V_a$  the  $b$  phase and  $c$  phase voltages are sound phases now. So, we can take  $V_{bc}$ , then we can get a more reliable we can say that directional relaying solution. So, what to do that to avoid that low voltage situation, the common practice is that for a phase  $a$  fault the corresponding operating quantities is  $I_a$  and polarizing quantity becomes  $V_{bc}$  instead of  $V_a$ . For  $b$  it is  $I_b$  current and  $V_{ca}$  not  $V_b$ .

For  $c$  phase it is this  $I_c$  current and  $V_{ab}$  not the  $V_c$ . I told you that most of the faults being line to ground faults we can overcome the problem of significantly small voltage for close in fault which are very close to the relay bus. In that case if you see this phasor diagram, so this is  $V_a$  line, this is  $V_b$  line and this is  $V_c$  line,  $120^\circ$  apart. Now let us say this is AG fault so  $V_a$  becomes smaller and the corresponding  $I_a$  current become significant and that will be lagging to  $V_a$  this is a forward fault case you have already seen in the circuit. So, this corresponding  $\phi$  this is a lagging current. In this case, if you see this is  $V_b$  and  $V_c$  they remain intact. Therefore, you can say that the corresponding  $V_{bc}$  become this plot here you can say that at this point origin then this becomes  $V_{bc}$  become this. So, we see that now that this  $I_a$  and  $V_b$ ,  $V_c$  then take this position like this. When we realize what the, we can say that do if they suitably translate this you can say that  $V_{bc}$  to the again bring back this  $V_{bc}$  to this  $V_a$  reference for that you can say that  $90^\circ$  you can say that to the angle of  $V_{bc}$ .

Then the corresponding reference we can say that voltage becomes in line with  $V_a$  and then similar we can say that positive value of  $\phi$ , negative value of  $\phi$  the concept which we have used for that reverse and forward fault can be applied. So, this for that once again I am telling that one of the way relay many relays do is that once you compute the  $\angle V_{bc}$  add the corresponding angle you can say of the  $\angle V_{bc} + 90^\circ$ . Then again you can say that bring back the corresponding reference to the same reference as  $V_a$  and there we can say that you can apply this leading, lagging concept of this current which will decide you can say that the direction of the fault. We will see different examples for these kind of applications also.

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Now, let us you can say that come to the same 400 kV three phase systems and we have a forward fault  $F_1$  and then this we are observing this relay which is assigned for this breaker. This is a forward fault and we are observing for this relay 400 kV transmission system. Now, let us say that for a fault this is the set of currents observed by the relay and set of voltages which is measured by the relay. So, if we see this current 2.04, 0.75, 0.71, so this clearly shows that this is a phase to ground fault and if we see this corresponding phasor become substantially low as compared to  $b$  and  $c$ . So, now the relay will make a judgment to this is acceptable for deciding on the relay or not, simple phase angle of  $V_a$  and  $I_a$  or it has to go for the polarizing quantity using what is that component that is  $V_{bc}$ .

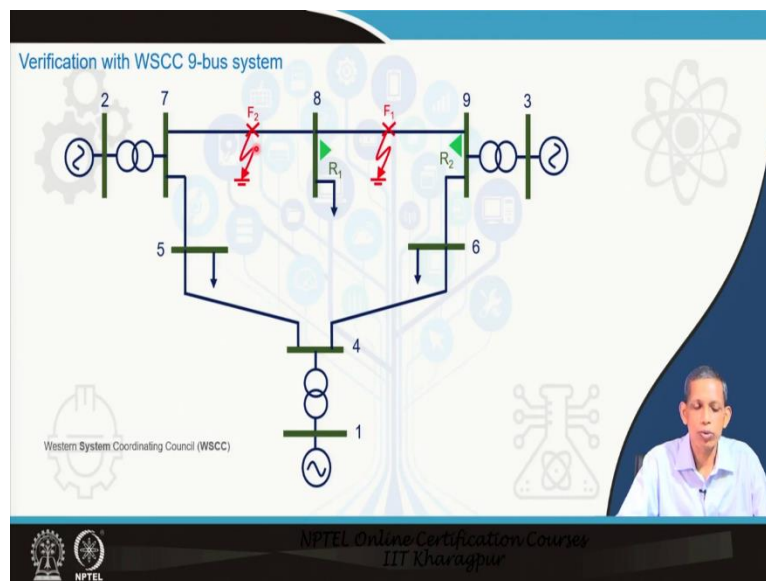


Because this is phasor current, the fault is  $ag$  type phase  $a$  to ground fault. Therefore, what we say here that if the corresponding relay rejects that this is not acceptable then will be using  $V_{bc}$ , this is better option. So, then in that case what you do is that these  $V_{bc}$  whatever angle we have, we can say that you make a  $90^\circ$  with that and then you can say that you compare with  $I_a$  to compute the  $\phi$ .

So, the  $\phi$  angle is nothing but you can say that angle of  $I_a$  minus angle of this combinations then you get the angle to be  $-67.04^\circ$  and this angle is negative indicating this is a forward fault which is confirms to our simulation for  $F_1$  fault. So, this sequence that we see that in case of  $a$  phase voltage is low significantly so the better option we can say that is quadrature component can be used.

So that is why we can say that this is very common. The instant of  $V_c$  in phase component of voltage the relay is generally take the option of quadrature component because most of the faults are line to ground faults. But still there is problem that in case of three phase fault this in case the closed by to this bus M that all the phase voltages may collapse, what is the solution. So, we will look into those kind of issues also later.

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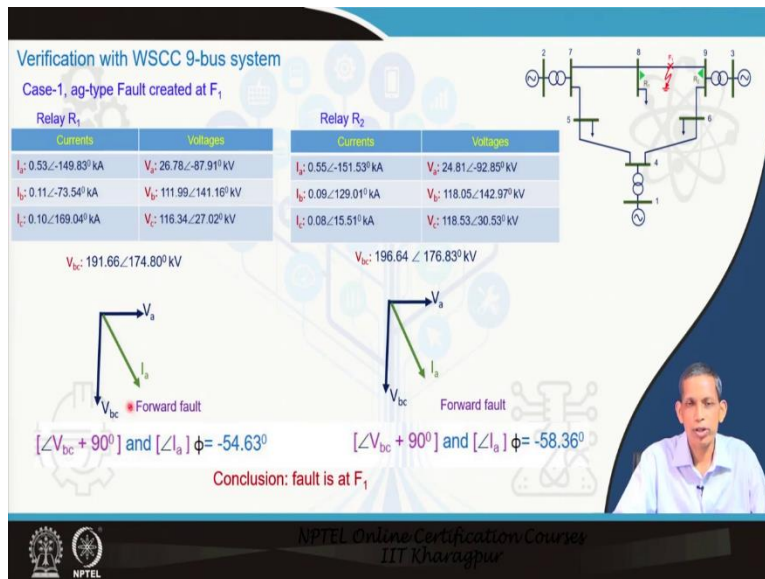
Now, let us we can say that whatever you have learn how to discriminate forward and reverse fault to obtain the direction of fault that is our directional relaying perspective which is being used in the different protection schemes. We will take a 9 bus WSCC system and we will check you can



say that in this system, how we can say that the corresponding quadrature voltage approach is reliable will check.

So, we will see you can say that see only this relay who takes care of breaker at here for the line section 8 -9 and also we can say that the other relay will check a R<sub>2</sub> at bus 9. So these two relay takes care this line, and how do they see this F<sub>1</sub> fault which is internal to this line and F<sub>2</sub> fault which is external to this line 8-9. So how do they see, now if you see this perspective as you understood, for R<sub>1</sub> this F<sub>1</sub> fault is a forward fault. For R<sub>2</sub> the F<sub>1</sub> fault is a forward fault, they take care of the corresponding breaker at this bus 9 and bus 8. For F<sub>2</sub> fault the relay at bus-9 R<sub>2</sub> will still see a forward direction but R<sub>1</sub> at bus 8 will see a reverse fault. So with this you can say that we will see how the corresponding relay will be able to distinguish this F<sub>1</sub> and F<sub>2</sub> fault as a forward or reverse fault.

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First case the fault is *ag* type phase a to ground called created at F<sub>1</sub> here, and now this relay R<sub>1</sub> and R<sub>2</sub> will have measurements for this fault. So, these are the set of measurements for R<sub>1</sub> current set I<sub>a</sub>, I<sub>b</sub>, I<sub>c</sub>, V<sub>a</sub>, V<sub>b</sub>, V<sub>c</sub>. Similarly, for R<sub>2</sub> we have current measurements and the voltage measurements from there we get the corresponding phasors using DFT, least square or so. Now, we see this perspective, if you see this phase *a* current is 0.53 kA phase B is 0.1 kA, phase C is 0.1 kA. This is phase *a* to ground fault. So, this clearly is being observed here.

The  $V_a$  is low, much lower than  $V_b$  and  $V_c$ . In this case also at bus 9 at relay  $R_2$  the corresponding  $a$  phase voltage is substantially low that is what you observe. So now we can apply the corresponding quadrature voltage approach. One can use also the phase voltage approach also.

So, now if you compute the  $V_{bc}$  because fault is in phase  $a$ , compute the  $V_{bc}$  so  $V_b - V_c$ . So then only you get you can say that you get  $191.66 \angle 178.80$  kV. So, these are all system level voltages without any sense also for our easy understanding. Similarly, for  $R_2$  for the same  $F_1$  fault, the  $V_{bc}$  is  $196.64 \angle 176.83$  kV that is  $V_b - V_c$ .

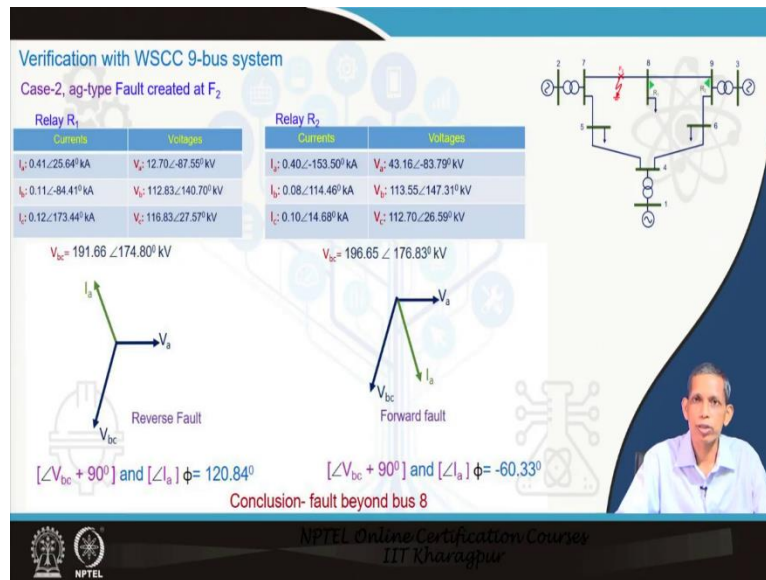
Now, what we do is that we see for these cases, if we take the  $V_a$  as the reference, I will take the  $V_a$  as reference -  $87.91^\circ$ . So, make it you can add that  $87.91^\circ$  in all the phasor quantity. So we shift it you can say that you rotate it anticlockwise, then we will get the corresponding  $V_a$  as reference. At that time so we will compensate for all you can say  $87.91^\circ$ . At that time the corresponding  $V_a$  takes the position of this, you see here respect to  $-87.91^\circ$  this is  $-149^\circ$  so this current is lagging to  $V_a$ . Now we get the  $V_{bc} 90^\circ$  to that as such  $V_{bc}$  will be  $90^\circ$  to lagging to this  $V_a$ .

So, this is  $V_{bc}$  position but as far or you can say that quadrature principle what do we follow if that angle of  $V_{bc}$  plus  $90^\circ$  that again  $V_{bc}$  is being shifted to this  $V_a$  reference and then we compare the corresponding  $I_a$  position. So, angle of  $I_a$  minus that shifted angle of  $V_{bc}$  will compare that and get the  $\phi$  and that comes out to be  $-54.63^\circ$ .

So, this shows that this minus angle so that this is a forward fault as observed by relay  $R_1$  for this  $F_1$ , which is correct. Now, you go to this  $R_2$  now.  $R_2$  at this  $V_{bc}$  to be this and you draw the phasors. It comes out to same so  $R_2$  the corresponding  $V_{bc}$  plus  $90^\circ$  whatever  $V_{bc}$  plus  $90^\circ$ , angle  $I_a$  we know -  $151.53^\circ$ .

So, angle of  $I_a$  minus angle of this shifted  $V_{bc}$  will give us  $\phi$  and that comes out to be  $-58.36^\circ$ , that this minus angle shows again this is forward fault. So for  $R_2$  also this is forward fault. So, the conclusion from these two we can say that  $R_1$  and  $R_2$  that both are forward and that means there is an internal fault and this also correctly identified by these two relays  $R_1$  and  $R_2$  using the quadrature voltage approach. We are able to identify the direction of fault properly. You can try also simple phase based approach.

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Now, I will go to the next with fault at F<sub>2</sub> as I already mentioned for fault at F<sub>2</sub> relay R<sub>2</sub> see forward direction what relay R<sub>1</sub> this is reverse direction. Let us see how they see through this calculation process. Relay R<sub>1</sub> has this set of current, these set of voltages. R<sub>2</sub> has this set of current and voltages.

So, current phase is high, current voltage in phase *a* is substantially low. Here also it is lower than *b* and *c*. You computed the V<sub>bc</sub> from V<sub>b</sub> - V<sub>c</sub> here, now I got the corresponding V<sub>bc</sub>, V<sub>a</sub> and I<sub>a</sub> position like this. And note that here for this case the I<sub>a</sub> takes a position like this if we compensate you can say the corresponding V<sub>a</sub> to be a reference - 87.55° add that 87.55° to all.

Then we will getting you can say that this I<sub>a</sub>, 87.55°, twenty five plus that. So, this gives you an angle like this. So this was that to with respect to V<sub>a</sub> this is leading, when you come to know that this concludes that there is a reverse fault. Similar conclusion also from V<sub>bc</sub>. V<sub>bc</sub> takes a position like this 90° so again it comes out to be V<sub>a</sub> reference with an angle of I<sub>a</sub>.

So therefore, you can say that the I<sub>a</sub> the corresponding φ happens to be 128.84°. If that is so, there is a positive angle, 128.84°. So, we conclude that this is a reverse fault. When you comes to R<sub>2</sub> and this set of measurements and then again V<sub>bc</sub> becomes this. So, angle of V<sub>bc</sub> plus 90° and then that we can say that the angle I<sub>a</sub>. So, angle of I<sub>a</sub> minus this angle you say φ is -60.33°, negative angle indicates forward fault. So, we see that for R<sub>2</sub> this is forward fault and for R<sub>1</sub> this is reverse fault and this is correct as we have already mentioned for the F<sub>2</sub> fault. Therefore, these two relays we

can say that are able to distinguish the corresponding fault in terms of the directionality successfully using the quadrature voltage component.

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Alternative principle- sequence components-  
Available Sequence Quantities for Different Faults:

Quantity	3-phase fault	LG fault	LL fault	LLG fault
$V_1$	Yes	Yes	Yes	Yes
$V_2$	No	Yes	Yes	Yes
$V_0$	No	Yes	No	Yes
$I_1$	Yes	Yes	Yes	Yes
$I_2$	No	Yes	Yes	Yes
$I_0$	No	Yes	No	Yes

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So, we see that quadrature voltage are simple phase voltages can be applied to that, but they have their own merits and demerits. There are alternative principles on sequence components based approach and so by different numerical relay. So, we will see you can say that, the how corresponding sequence components are able to distinguish the direction of the fault and how they can be applied in a better way for directional relay principle.

We will see more details on the next lecture, but have you can say see what happens there, the available sequence quantities for different faults. So, for three phase fault,  $V_1$  is present, for line to ground fault  $V_1$  is present, for line to line  $V_1$  is present, for three phase fault  $V_1$  is always present. Any measurements at any relay bus will give you the  $V_2$  is present for all faults except three phase.  $V_0$  is present only for you can say that fault involving ground LG and LLG. Similarly,  $I_1$  for all,  $I_2$  for unbalanced fault and  $I_0$  for you can say that fault involving ground.

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Sequence component based Directional Relaying:

Operating Quantity ( $I_{op}$ )	Polarizing quantity ( $V_{ref}$ )
$I_1$	$V_1$
$I_2$	$V_2$
$I_0$	$V_0$

- These quantities can be used to produce a single three-phase directional element and replace the three separate 90° connected phase directional elements.
- The total number of phase directional elements is reduced by one.
- Angle of  $Z_1$ ,  $Z_2$ , and  $Z_0$  as calculated from corresponding  $V/I$  to determine direction of fault

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With this scenario so the sequence component based directional relaying principle are being applied. So there you can say having operating quantity is  $I_1$  and polarizing quantity or reference quantity is  $V_1$ ,  $I_2$ ,  $V_2$ ,  $I_0$ ,  $V_0$ . These quantities can used to produce different relaying principles hopefully we will seek one by one. Because of the transformations from phase quantity to these sequence quantities, let us see for negative sequence. So, we are getting one pair only instead of  $V_a, V_b, V_c$ , and  $I_a, I_b, I_c$ . So that reduces the directionality computational perspective. Note that if  $V/I$  that is  $V_2/I_2, V_1/I_1$  so that gives an impedance from, so we can use the impedance form and the angle of the impedance is indicative of direction that we will see in more details in the next class. Thank you.