

$v_0 = V_m \sin \omega t$ for output voltage for α to β and $v_0 = 0$ for $\omega t = 0$ to α for this condition and for this negative half cycle that is β to 2π .

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Single Phase Fully Controlled Converter (Cont...)

Load Current Expression

When the thyristor is triggered at a delay angle of $\alpha > \gamma$, the eqn. for the circuit can be written as

$$V_m \sin \omega t = i_o \times R + L \left(\frac{di_o}{dt} \right) + E; \alpha \leq \omega t \leq \beta$$

The general expression for the output load current can be written as

$$i_o = \frac{V_m}{Z} \sin(\omega t - \phi) - \frac{E}{R} + A e^{-\frac{t}{\tau}}$$

Where

$$Z = \sqrt{R^2 + (\omega L)^2} = \text{Load Impedance.}$$

$$\phi = \tan^{-1} \left(\frac{\omega L}{R} \right) = \text{Load impedance angle.}$$

$$\tau = \frac{L}{R} = \text{Load circuit time constant.}$$

The general expression for the o/p current can

be written as
$$i_o = \frac{V_m}{Z} \sin(\omega t - \phi) - \frac{E}{R} + A e^{-\frac{t}{\tau}}$$

So we can actually find it out the conditions and we can write that actually differential equations to find it out the load current and its profiling it has been shown in the wave form. When the Thyristor is triggered at an delay angle of α , α is more than λ then equations of the circuits can we give as $V_m \sin \omega t = iR + L \frac{di}{dt} + E$ for this duration. Now in general expressions for the output.

So we can write that actually can solve this differential equation and i can find it out that that load current we will have $\frac{V_m}{Z} \sin \omega t - \phi$ we have discussed ϕ in previous class where actually ϕ is actually this one $\tan \phi = \frac{\omega L}{R}$ so $\frac{E}{R} +$ this term $A e^{-\frac{t}{\tau}}$ but τ is an electrical time constant of the system. So this is the Z value Z is given by this thing and $\tan \phi$ is actually $\frac{\omega L}{R}$.

Similarly, the τ time constant is $\frac{L}{R}$ the load circuit constant and general expression for this thing if we substitute then we will have actually this value.

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Single Phase Fully Controlled Converter (Cont...)

To find the value of the constant

'A' apply the initial conditions at $\omega t = \alpha$, load current $i_o = 0$, Equating the general expression for the load current to zero at $\omega t = \alpha$, we get

$$i_o = 0 = \frac{V_m}{Z} \sin(\alpha - \phi) - \frac{E}{R} + A e^{-\frac{R}{L} \omega t}$$

We obtain the value of constant 'A' as

$$A = \left[\frac{E}{R} - \frac{V_m}{Z} \sin(\alpha - \phi) \right] e^{\frac{R}{L} \alpha}$$

Substituting the value of the constant 'A' in the expression for the load current; we get the complete expression for the output load current as

$$i_o = \frac{V_m}{Z} \sin(\omega t - \phi) - \frac{E}{R} + \left[\frac{E}{R} - \frac{V_m}{Z} \sin(\alpha - \phi) \right] e^{-\frac{R}{L}(\omega t - \alpha)}$$

Then what you can do we got to find out the value of A that is unknown. So we got to find A which we have done in and that was rectified also. So by initial conditions so when current is 0 for this A if we actually apply the initial condition when $\omega t = \alpha$ then load current $i_o = 0$ so if we can equate it $i_o = 0 = \frac{V_m}{Z} \sin \alpha - \phi - \frac{E}{R} + A e^{-\frac{R}{L} \alpha}$ from there we can get an expressions of A and that will have a component of e to the power.

So it is a varying component you can see that you know it is constant and there after a sinusoidal component and it is varied via actually an exponential component so here -sin is missing. So substituting this value A and we can have an expressions actually the load current so load current will take this format. So $\frac{V_m}{Z} \sin \omega t - \phi - \frac{E}{R} + \left[\frac{E}{R} - \frac{V_m}{Z} \sin \alpha - \phi \right] e^{-\frac{R}{L}(\omega t - \alpha)}$.

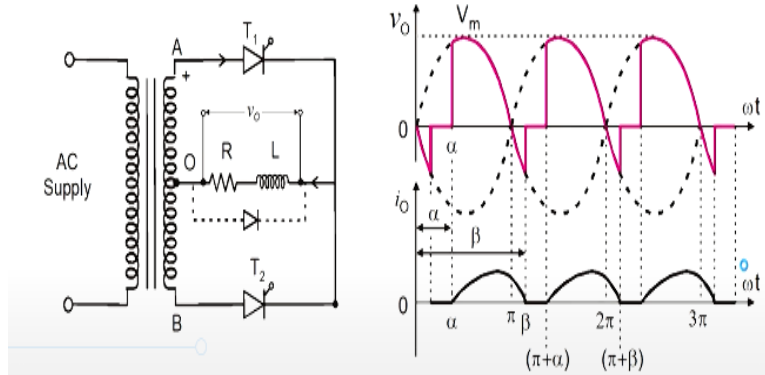
So from this equation this term this sinusoidal component can be 0 if you trigger $\alpha = \phi$. So ultimately then the sinusoidal component will come out you will have a sinusoidal component plus a decaying component. This will be a decaying component.

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Single Phase Fully Controlled Converter (Cont...)

Single Phase Full Wave Controlled Rectifier Using a Center Tapped Transformer

Discontinuous Load Current Operation without FWD for $\pi < \beta < (\pi + \alpha)$



Now let us take a next class that is a basically full control converter with a central tapped topology. So midpoint is available because you have in that configuration negative cycle is totally omitted so for this in conversion ratio is very poor and you also have a high degree of actually ripples. So for this we prefer actually full control mode of operations so but problem is there if we use a transformer we require the central time transformer.

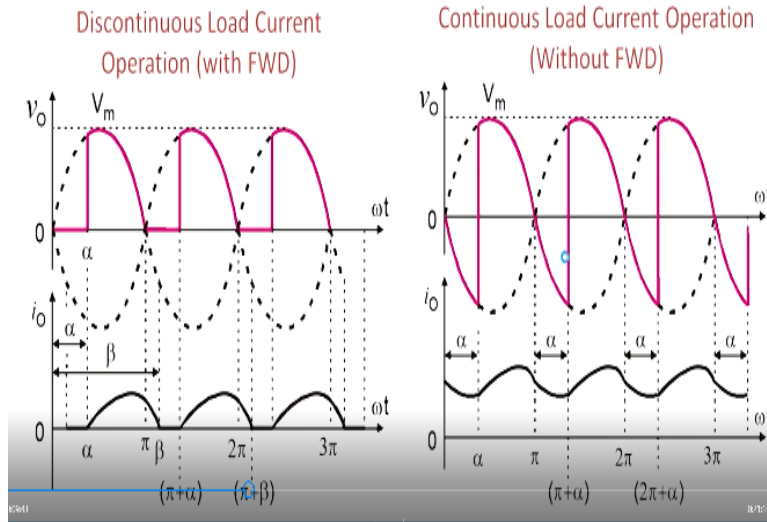
So same condition arises so let us consider that for RL load first. So we have a continuous and a discontinuous operation of the load current once we have a this is the current you can see that it is a discontinuous mode of conduction the red line shows that this is basically the voltage output available across this load and this is the freewheel it is optional whether it is connected or not. It generally comes through the switch may be.

So this wave form this half wave form shows that this continuous load current central tap full controller converters for triggering angle alpha for without any free wheel diode. So diode is basically not been placed into the circuit so far this is what will happen so a negative voltage will come that gives rise to the ripples or more DC and then after it will trigger an angle alpha then it will conduct so stored energy will mix this thyristor to conduct even in the negative cycle.

So you get this profile so all the energy is shared during this time so far this is and then we are no voltage is across is available and same way it will continue.

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Single Phase Fully Controlled Converter (Cont...)



If we have discontinuous conduction with that free wheel diode, then you know this negative part get truncated there is no negative part. So what happened you know actually till load voltage will be positive and DC component will be more. So what happened then there after actually at this point actually Thyristors will be reverse bias due to the diode and free wheel diode come into that picture and current will free wheel through this path.

This is the free wheel direction till actually energy is stored into the inductor is dissipated that is for the duration π to β and if the load current is quite high then you may have a continuous conduction mode and in this case you can see that actually current still follows alpha thereafter what happened since Thyristors is conducting you will be actually this is without free wheel so for this you get a huge part of the negative voltage.

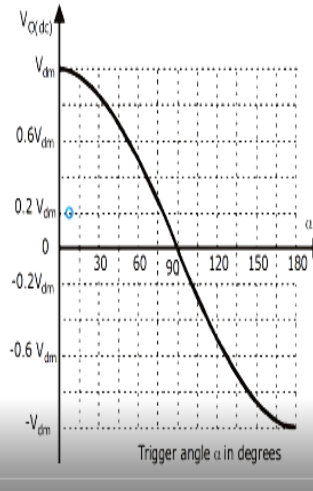
Then actually Thyristor will be triggered at an angle alpha so forward voltage you will get across the load then what happens is Thyristor is actually in a forward conduction mode due to the high current ultimately it will deliver negative load voltage so similarly it will continue. So negative load voltage can be truncated with the use of the freewheeling diode.

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Single Phase Fully Controlled Converter (Cont...)

- By plotting $V_{O(dc)}$ versus α , we obtain the control characteristic of a single phase full wave controlled rectifier with RL load for continuous load current operation without FWD

Trigger angle α in degrees	$V_{O(dc)}$	Remarks
0	$V_{dm} = \left(\frac{2V_m}{\pi}\right)$	Maximum dc output voltage $V_{O(max)} = V_{dm} = \left(\frac{2V_m}{\pi}\right)$
30°	$0.866 V_{dm}$	
60°	$0.5 V_{dm}$	
90°	$0 V_{dm}$	
120°	$-0.5 V_{dm}$	
150°	$-0.866 V_{dm}$	
180°	$-V_{dm} = -\left(\frac{2V_m}{\pi}\right)$	



Now let us see there is a characteristics of this actually single phase fully control converter. So we will plot VDC versus alpha. So you can see that you can get a maximum value of VDC that is $2 V_m/\pi$ that is add $\alpha = 0$ so control characteristics of a single and we assume that actually load current is continuous for this reason and without the free wheel diode that is this wave form so then what will happen you will find that at a 90 degree.

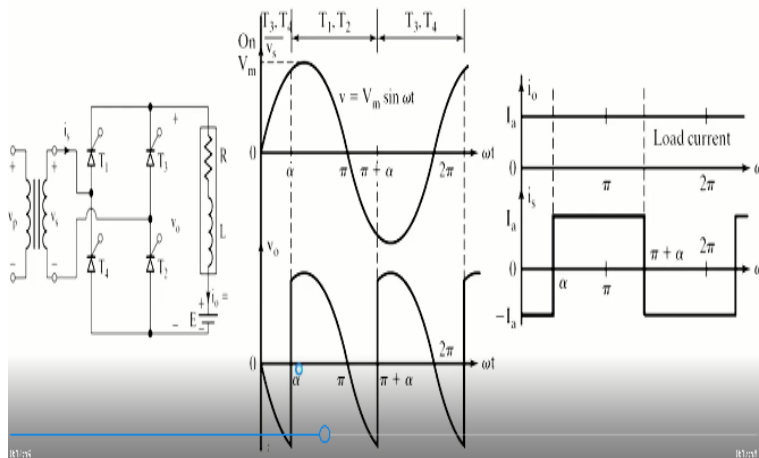
So this voltage deliver to the load is 0 thereafter if you increase this alpha beyond 90 degree then nearly a conversion operation. So it will be a bipolar so you can convert AC to DC as well as you can reconvert it into DC to AC. So actually so that load itself will actually then supply back the power to the source this is this kind of application is possible in case of the regeneration. So 90 to 0 if it is actually 120 degree then you can see that this $-V_{dm}$.

So on as 180 degree is the totally the inversion or inverter operation.

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Single Phase Fully Controlled Converter (Cont...)

Single Phase Fully Controlled Bridge Converter (Constant Load Current)



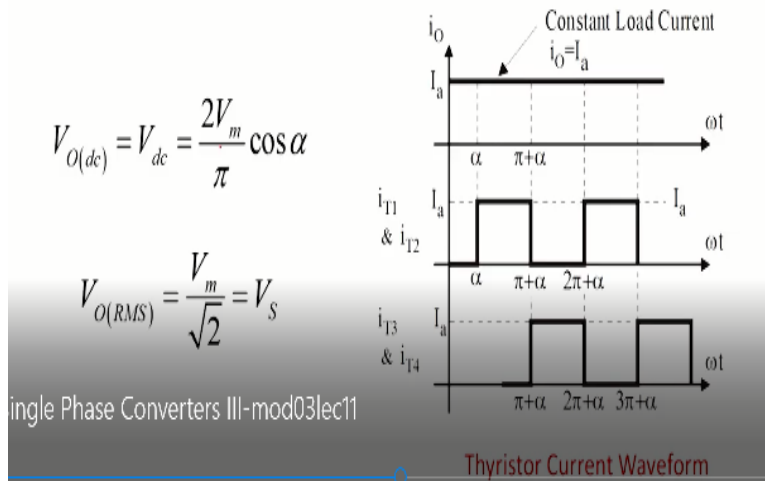
So let us consider that RME load with bridge configuration where actually we can bypass this central term transformer and also actually you may not require transformer if it is directly fed from the source. So now in forward half cycle we shall put this Thyristor in such a way that Thyristor T1 T2 will conduct and we assume that actually load current is actually continuous and constant that when it has got a very high level of inductance.

Generally, this can be approximated when $\omega L/R$ ratio is around 10. So time constant is around 10 second so for the period of actually 20 milli second it can be assumed to be actually constant. So it has been triggered at an angle α so before that the pair of Thyristors in negative half cycle was conducting and you are getting a negative voltage. Thereafter and same thing is applicable so since load current is continuous.

So effect of the vacuum is may not be the same so there after Thyristor is triggered at an angle α it could conduct till α to $\pi + \alpha$. So 180 degree thereafter again T3 and T4 will come into that picture. So it is quite easy to analysis since load current we have assume this kind of fashion. So the source current will also have a square wave and we can do the Fourier series analysis all the odd harmonic will be present for the order symmetry.

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Single Phase Fully Controlled Converter (Cont...)



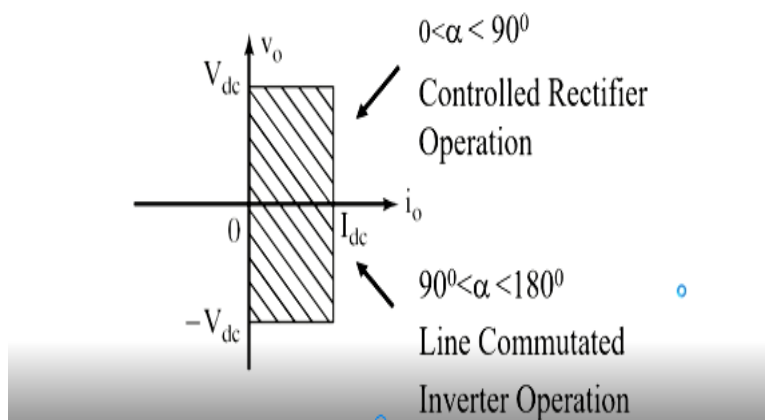
And thus we can calculate what is the amount of the actually Vdc and RMS and the corresponding current part of it. So Vdc actually $2 V_m / \pi \cos \alpha$ so we can derive that expression in place simply by integration. Same way actually the RMS output voltage will be $V_m / \sqrt{2}$ will be V_s and current to the Thyristor will be actually square wave. So this will be the current through across T1 and T2.

For the period of actually 360 degree similarly this will be the current for T3 and T4.

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Single Phase Fully Controlled Converter (Cont...)

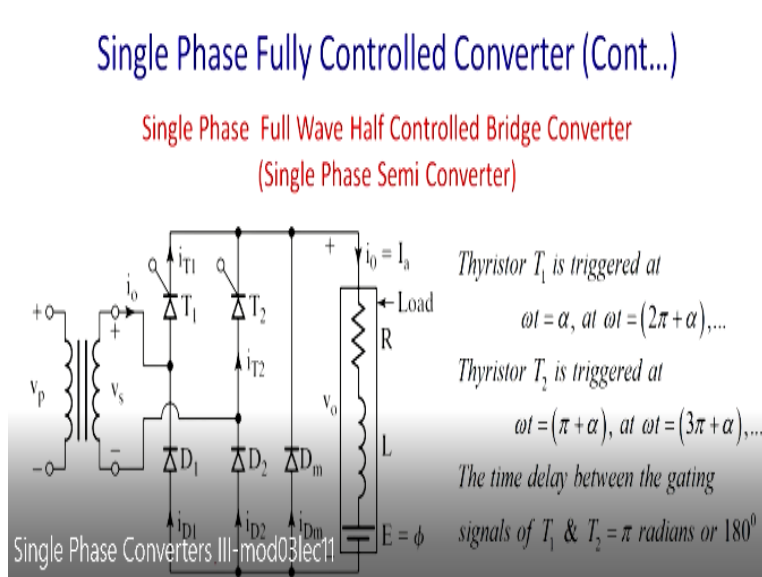
Two Quadrant Operation of a Single Phase Full Converter



Now here this is a 2 quadrant operation so you know while discussing switch we have described the quadrant operation here current is unidirectional. So current is always positive in the load but

voltage can be negative and positive depending on the triggering angle. So if alpha is actually more than 90 degree in this case then it will be an inversion operation and alpha is < 90 degree you get a controlled rectifier operation.

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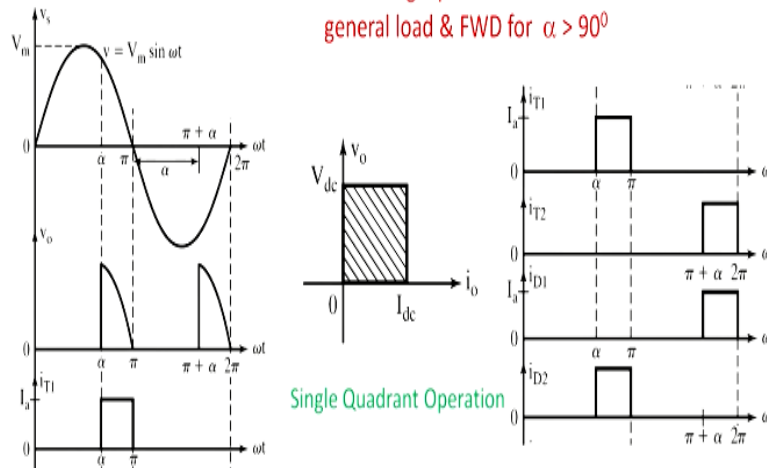
Now let us see the condition when there are three changes has been made this is called half control you can have a different combination of half control you can as asymmetrical or symmetrical configuration. So here you know upward to a Thyristor lower to a diode we can have another configuration where one leg is of thyristors and another leg is of diode. Then if you do that then we need not have to give a actually the freewheeling diode in that case.

Let us consider this configuration this configuration is called single phase fully controlled rectifier this is a single phase semi controlled converter rather so and it is fitting a RLE load. So it is $\omega t = \alpha$ it has been when triggered and we assume that load current is quite high and continuous so actually it will fit till $\omega t = 2\pi + \alpha$ thyristor T_2 is triggered and an angle $2\pi + \alpha$ and $3\pi + \alpha$. So accordingly this time delay between T_1 and T_2 is going to be the 180 degree.

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Single Phase Fully Controlled Converter (Cont...)

Waveforms of single phase semi-converter with general load & FWD for $\alpha > 90^\circ$

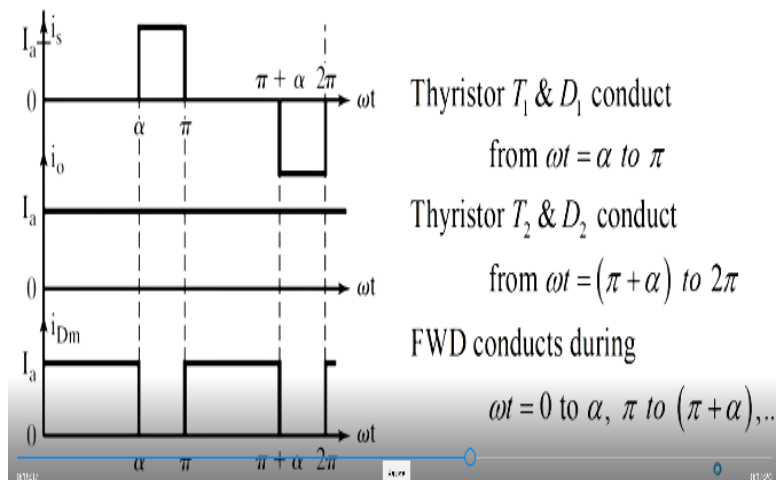


So see then wave form of voltage you will get so you have triggered here this is your angle. So ultimately you will get a voltage like this and please see that you know since the diode into the pictures. So negative voltage it is not possible to have because diode will conduct and free wheel truncate this actually the negative voltage and thus this part is been actually omitted so you only get the first quadrant operation that is actually the rectifications or the converter operation.

Same way current through this thyristor is T1 and T2 and this is a D1 and D2 so on and this is a single quadrant operation.

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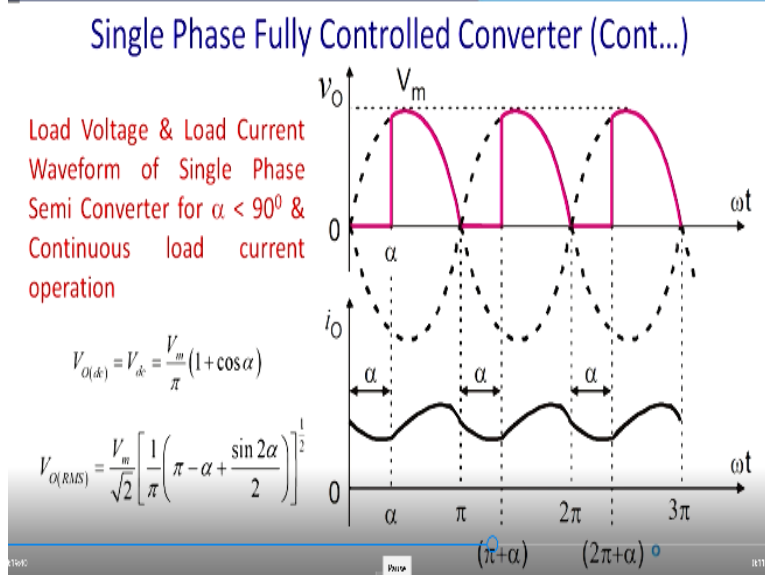
Single Phase Fully Controlled Converter (Cont...)



Now actually this is I_a this is a source current and it will be conducting for a very small interval of time α to 2π there after $\pi + \alpha$ to 2π in negative half. But since the value of the inductance is so high that you get a constant actually the load current and similarly you can find that rest of the current is flowing through the free wheel diode. Current through a free wheel diode will be very high and this is the amount of the current flowing to the free wheel diode.

So thus T1 and D1 conducts for this duration for α to π T2 D2 conducts for a period $\pi + \alpha$ to 2π and for ωt_0 to α that free wheel diode conducts again π to $2\pi + \alpha$ free wheel diode conducts.

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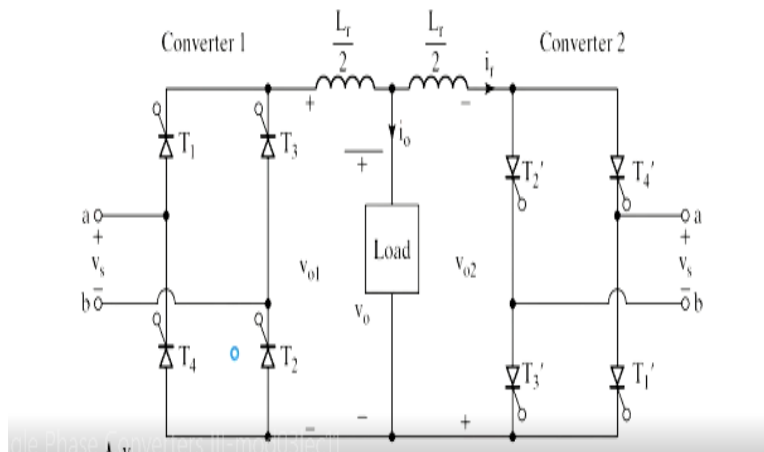
So this is the wave form of it the pink line actually shows the load voltages and from there we can derive the equation of the load voltage that is actually VDC that when we integrate over it is a very simple thing you will get $V_m/\pi (1 + \cos \alpha)$. So you can put any value of the $\cos \alpha$ you can find that actually even if you put $\cos \alpha = -1$ (180 degree) this value will be 0. So you will have a single quadrant operation.

Same way we can actually find it out the RMS value by actually integrating over it so you get $V_m/\sqrt{2} \left[\frac{1}{\pi} (\pi - \alpha + \sin 2\alpha/2) \right]^{\frac{1}{2}}$ so you can expect that in voltage there will be some oscillation of the double frequency. So due to that double frequency oscillation will come. So if

you divide by R definitely you will get the I RMS and if you divide it by R you get the I DC which is assumed to be cost and this comes square root kind of a thing.

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Single Phase Dual Converter

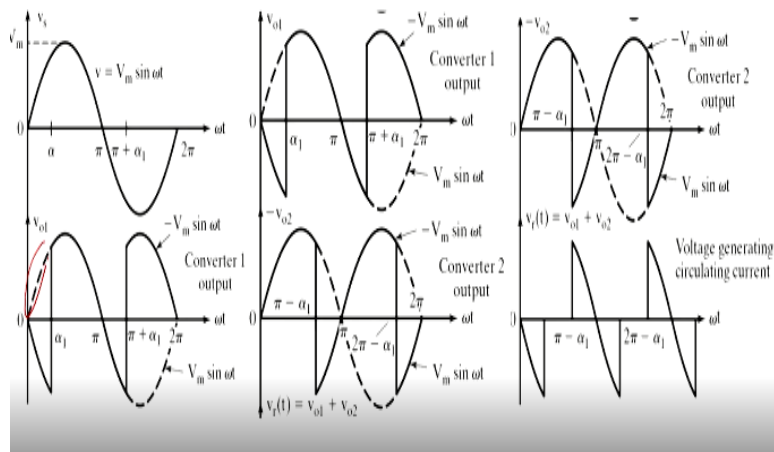


And mind it since it is a square wave so average and the RMS value should be same okay now let us come to the single phase dual converter. So it is a 4 quadrant operation so this Thyristors is a full control converter so thus it can operate + - actually 0 to 90 degree as a mode of converter and 90 to 180 degree as a mode of the inverter. Same way what you see that polarity of this actually Thyristor is reversed.

So what this is and it will be - alpha and since that there can be this pole voltage may have a instantaneous difference of the voltages. So due to that you require to actually put a blocking current blocking inductor so that it can block the instantaneous voltages between these two pole voltages. So what happened in first mode let us assume that you know.

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Single Phase Dual Converter (Cont...)



This is the input voltage and essentially you have chopped out this voltage and since it is a full control operation you will get this kind of wave form and similarly you feed the same voltage and if you trigger the logic of triggering of the dual converter is that if you trigger that one converter and an alpha another converter required to trigger at $\pi - \alpha$. So you have triggered $\pi - \alpha$ so essentially you will get actually this part of the voltages.

So essentially what you will get at the output voltage is $v_1 + v_2$. So this will be the voltages across the load and unfortunately due to that there will be a circulating current flowing like this when there is no cancellation of the instantaneous voltages. To block that instantaneous voltages, we have put an inductor.

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Single Phase Dual Converter (Cont...)

The average dc output voltage of converter 1 is

$$V_{d1} = \frac{2V_m}{\pi} \cos \alpha_1$$

The average dc output voltage of converter 2 is

$$V_{d2} = \frac{2V_m}{\pi} \cos \alpha_2$$

In the dual converter operation one converter is operated as a controlled rectifier with $\alpha < 90^\circ$ & the second converter is operated as a line commutated inverter in the inversion mode with $\alpha > 90^\circ$

$$\frac{2V_m}{\pi} \cos \alpha_1 = \frac{-2V_m}{\pi} \cos \alpha_2 = \frac{2V_m}{\pi} (-\cos \alpha_2)$$

$$\therefore \cos \alpha_1 = -\cos \alpha_2$$

or

$$\cos \alpha_2 = -\cos \alpha_1 = \cos(\pi - \alpha_1)$$

$$\therefore \alpha_2 = (\pi - \alpha_1) \text{ or}$$

$$(\alpha_1 + \alpha_2) = \pi \text{ radians}$$

Which gives

$$\alpha_2 = (\pi - \alpha_1)$$

$$\therefore V_{d1} = -V_{d2}$$

So let us do some analysis so of course since it is the full control converter for first converter in left hand side it is this value will be this average voltage or the Vdc 1 will be $2V_m/\pi \cos \alpha_1$ similarly output voltage of the second converter V dc 2 that will be $2V_m/\pi \cos \alpha_2$. The dual converter operates one in a converters operating under the controlled rectifier another actually was triggering angle is < 90 degree.

Another is basically it has to be more than 90 degree and we hold this equation further if it is trigger an alpha another is triggered 180 degree $-\alpha$ so Vdc1 should be $=-V_{dc}/2$ so if you can equate this two equations ultimately you find that basically $\alpha_2 = \pi - \alpha_1$. So this is the constraint so $\alpha_1 + \alpha_2$ should be $=\pi$ so for this is in this mode of operation has been continued. So dual converter can we operated it in two different modes of operations.

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Single Phase Dual Converter (Cont...)

The Dual Converter can be operated in two different modes of operation

- Non-circulating current (circulating current free) mode of operation.
- Circulating current mode of operation.

Circulating Current Mode Of Operation

- In this mode, both the converters are switched ON and operated at the same time.
- The trigger angles α_1 and α_2 are adjusted such that $(\alpha_1 + \alpha_2) = 180^\circ$, $\alpha_2 = (180^\circ - \alpha_1)$.

Non-Circulating Current Mode of Operation

In this mode only one converter is operated at a time.

- When converter 1 is ON, $0 < \alpha_1 < 90^\circ$
- V_{dc} is positive and I_{dc} is positive.
- When converter 2 is ON, $0 < \alpha_2 < 90^\circ$
- V_{dc} is negative and I_{dc} is negative.

Definitely, so one is non-circulating current circulating current free mode of operation we can make the instantaneous for the same at all the time so that no sacrificing current flows and circulating current mode of operation. So in non-circulating current mode of operation this mode only actually possible in one instant mode is in this mode only one converter is operated one time.

So both converter are not operated so when converter 1 is on that means alpha 1 should be =0 to 90 degree and Vdc is positive and Idc is also positive and where converter 2 is on, it should be actually < 90 degree and Vdc is negative and this should be also negative. So then what happened since you are operating one converter at one time and thus there is no condition of flow of current.

But what happened then actually power delivering capabilities is decreasing in circulating mode what happened. In this mode, both the converter has switched on and operated at the same time and the triggering angle alpha 1 and alpha 2 are adjusted in a way alpha 1 and alpha 2 =180 degree or alpha 2= 180 degree-alpha 1. So when this mode is generally more preferred.

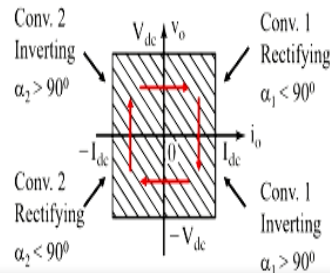
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Single Phase Dual Converter (Cont...)

Circulating Current Mode of Operation

- When $0 < \alpha_1 < 90^\circ$, converter 1 operates as a controlled rectifier and converter 2 operates as an inverter with $90^\circ < \alpha_2 < 180^\circ$. In this case V_{dc} and I_{dc} both are positive.
- When $90^\circ < \alpha_1 < 180^\circ$, converter 1 operates as an Inverter and converter 2 operated as a controlled rectifier by adjusting its trigger angle α_2 such that $0 < \alpha_2 < 90^\circ$. In this case V_{dc} and I_{dc} both are negative.

Four Quadrant Operation



So when alpha 1 is basically < 90 degrees converter one operates in a controlled rectifier and converter 2 operates in an inverted mode. And in this case V_{dc} and I_{dc} are both to the preferably assumed directions. When it is change when actually this condition is satisfied is alpha 1 is more than 90 degree and < 180 degree then converter 1 operates in the inverter mode and converter 2 operates in the rectifier mode.

And thus what happened we get a negative dc. After this we have a four quadrant operation so converter 1 is in rectify mode thereafter converter 1 is inverting mode this is 1 of this quadrant operation in this condition I_{dc} is positive. So this is a conversion this is actually we have described in case of the full control converter similarly we can make so converter 2 < 90 degree then what happened basically I_{dc} will be negative but V_{dc} will be positive.

And this is a third quadrant operation both V_{dc} and I_{dc} both will be negative where actually you are putting the converter to more than 90 degree.

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Single Phase Dual Converter (Cont...)

Expression for the Instantaneous Circulating Current

- v_{O1} = Instantaneous o/p voltage of converter 1.
- v_{O2} = Instantaneous o/p voltage of converter 2.
- The circulating current i_r can be determined by integrating the instantaneous voltage difference (which is the voltage drop across the circulating current reactor L_r), starting from $\omega t = (2\pi - \alpha_1)$.
- As the two average output voltages during the interval $\omega t = (\pi + \alpha_1)$ to $(2\pi - \alpha_1)$ are equal and opposite their contribution to the instantaneous circulating current i_r is zero.

$$i_r = \frac{1}{\omega L_r} \left[\int_{(2\pi - \alpha_1)}^{\omega t} v_r d(\omega t) \right]; \quad v_r = (v_{O1} - v_{O2})$$

As the o/p voltage v_{O2} is negative

$$v_r = (v_{O1} + v_{O2})$$

$$\therefore i_r = \frac{1}{\omega L_r} \left[\int_{(2\pi - \alpha_1)}^{\omega t} (v_{O1} + v_{O2}) d(\omega t) \right];$$

$$v_{O1} = -V_m \sin \omega t \text{ for } (2\pi - \alpha_1) \text{ to } \omega t$$

So let us understand the few aspects of it so let us assume that the instantaneous output voltage converter 1 is V_{O1} and Instantaneous output voltage of convert 2 is V_{O2} . And the circulating current are we required to calculate and we required to block their circulating current which may harm actually the Thyristor unnecessarily. Because it is not getting into the load circulating current i_r can be determined by integrating the instantaneous voltage difference.

Which is the drop across the circulating current along L_r so let us start at $\omega t = 2\pi - \alpha_1$ as the two average output voltage during this interval is $\omega t = \pi + \alpha_1$ and another is $2\pi - \alpha_1$ positive opposite to their contributions so you can put this limits so $i_r =$ this thing $2\pi - \alpha_1$ to ωt where actually V_r is this. So we can actually find it out the what should we the value of this circulating current. Substituting $v_{O1} = -v_m \sin \omega t$ or $2\pi - \alpha_1$.

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Single Phase Dual Converter (Cont...)

➤ The final expression will be

$$i_r = \frac{V_m}{\omega L_r} \left[\int_{(2\pi - \alpha_1)}^{\omega t} -\sin \omega t d(\omega t) - \int_{(2\pi - \alpha_1)}^{\omega t} \sin \omega t d(\omega t) \right]$$

$$i_r = \frac{2V_m}{\omega L_r} (\cos \omega t - \cos \alpha_1)$$

The instantaneous value of the circulating current depends on the delay angle.

For trigger angle (delay angle) $\alpha_1 = 0$,
the magnitude of circulating current becomes min.
when $\omega t = n\pi$, $n = 0, 2, 4, \dots$ & magnitude becomes
max. when $\omega t = n\pi$, $n = 1, 3, 5, \dots$
If the peak load current is I_p , one of the
converters that controls the power flow
may carry a peak current of

$$\left(I_p + \frac{4V_m}{\omega L_r} \right), \text{ where}$$

$$I_p = I_{t(\max)} = \frac{V_m}{R_t}$$

&

$$i_{t(\max)} = \frac{4V_m}{\omega L_r} = \text{max. circulating current}$$

So either substitute it and you get the results $i_r = \frac{2V_m}{\omega L_r} \cos \omega t - \cos \alpha_1$ so you can see one thing that you can actually make the circulating current 0 suitably controlling α_1 but it is not impossible most of the time. So for triggering angle $\alpha_1 = 0$ the magnitude of the circulating current becomes minimum 1 $\omega t = n\pi$. So magnitude become maximum and when $\omega t = n\pi$ actually for the odd harmonics.

The peak of the load current I_p one of the converters is actually giving you the current. So this is where the expressions of it so $I_p + \frac{4V_m}{\omega L_r}$ where $I_p = I_{L \max}$ that is $= \frac{V_m}{R_L}$ and that is I_r should be equal to this is the max peak value of the circulating current that is $\frac{4V_m}{\omega L_r}$. I continue you with the next class with the converter, we are looking forward to discuss more interesting detail about this converter. Thank you.