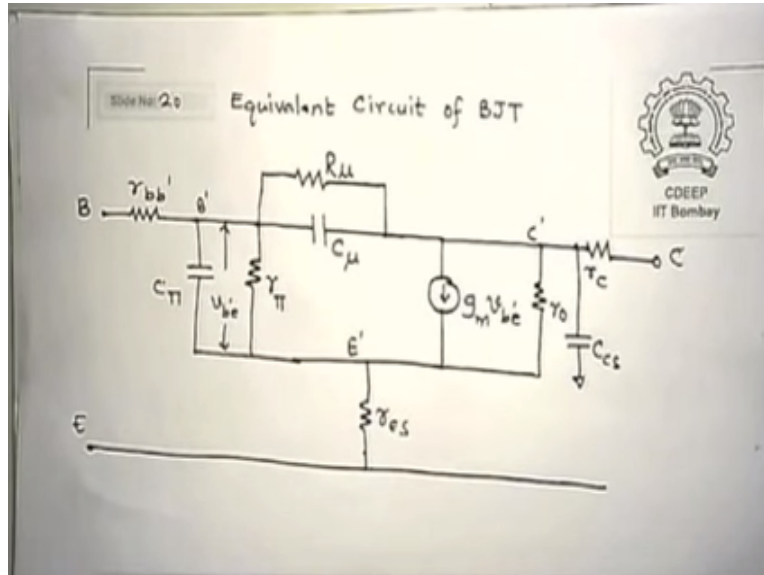


Analog Circuits
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Lecture – 04
BJT Small Signal Model

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We have discussed last time we show the circuit this is the equivalent circuit of a bipolar junction transistor in a common emitter configuration. Shown this is the base resistance called base spreading resistance or maybe dash this is the C_{π} is the capacitance associated with value given last time which is between base and emitter. Please remember there are 2 capacitances here those C_{π} is only shown there are 2 capacitance between base and emitter.

Which are the 2 in 1 because of the junction capacitance of the base emitter junction and the other is diffusion capacitance. Right now it is showing steeper as if it takes care of both but otherwise we must find whichever is dominant the sum total is what is going to come in this parallel combination and there is a resistance associated called qI_B/KT .

Which is R_{π} then there is a junction between base and collector which has a capacitance of reverse bias capacitance of C_{μ} which has shunted by a high huge resistance in the reverse bias

of a diode which is r_{μ} there is a resistance called spreading resistance to emitter because of the path it takes longer distance to travel to the collectors from emitter to real emitter is called r_{es} .

Then there is the current source this is the major feature of bipolar transistor if you have a V_B at the input the output current is $g_m v_{be}$ which is larger current than the input current which enters of the base and since this current will be larger then we gain output current by input current then there is the output resistance r_0 which is essentially the slope of ICBC characteristics with us and discussed.

Now there is a small capacitor or small resistance associated with the collector region itself which is R_C and there is a capacitor between substrate and the collector, which is called C_{TS} so this is the circuit last time we showed and we also derived it all the component it quickly will get into some of the features or some of the numbers.

So that we will get an idea of what of the kind of numbers let us say I am working on biasing okay so the word bias is very important I keep saying earlier also if you are the characteristics of it on this term we are redraw it if I have very this capacitor a collector current versus V_{CB} drawn a different V_B or I_B values okay this is I_B 0, 1, 2, 3, 4 and what did we say this is a DC current versus DC voltage.

So what we say that if I have fixed my V_C that is if I wait on this curve it is alright now shown and P_N have a small resistance R here then the current flowing here is I_C and this V_{CE} is essentially $V_{CC} - I_C R_C$ now so one can see from here depending on the value of R_L and depending on the choice of I_C I make I can draw this line itself on this graph and this light this is V_{CC} .

This is I_{CC} bar a maximum will discuss this with in more detail this is called load line this is called load line I think you have been disc already known but a given bias current let us say I_B to this value we see what we will use is called the and the current associated with this let us call it I_C bias V_C bias.

So if I fixed my VC bias I for a given IB I get a fixed ICDC value of electric current this is called DC bias okay we will do a little more detail I just want to use those values so I am now said this is called the operating point this is called the operating point and we are all the time worried last time I said choice of my IC is essentially going to decide all my parameters if you recollect our formula IC term is appearing Q_{IC}/KT gm.

So IC is therefore the major biasing capital IC means DC value or what is the output we are looking small signal values but the biasing is DC is that correct why signal is DC, which decides all small signal parameters for this subject so having shown you this we did loss and something like this.

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Let me quickly show you not really calculate anything typical I am biasing a carafe such an amplifier can be shown as IC of one minimum i bias the reverse bias voltage to 3 volts VCS I use it five volt I mean these are arbitrary values do not get the DS are the actual values will have to evaluate for given data given to us right now take some money typical value for junction capacitance key j_0 for the junction emitter capacitance C_{pi} .

What we were looking is 10 and what is this 0 stand for 0 bias with the bias change, yes this value will also change okay what is this $\pi_0 e$ this is the built-in voltage of base emitter junction okay this is 0.9 volts what is the value of that $kt/q \ln n_a n_d / n_i^2$ we are done this physics last year this is at any parameter which is you know because it feels a step Junction it is half it is exponential it in one third and so on and so forth right now.

I hum it half similarly I calculate the junction capacitance of the base collector which is around 10 femto farad's similarly for base collector Junction the sorry base collector Junction the built in voltage is 0.5 volt and HRC or the collector is here generally base emitter junction can be made it is step junction where our base collector Junction is normally because of the process we do can be generally exponential or linearly graded, but having given.

Whatever we can choose any of the values specified if it is a linear everywhere we will put 1/3 of Euripides other someone must specify what each are I should use for a given junction, you find

similarly variable between collector and subscribe the capacitance at 0 bias is 20 the built-in voltage is 0.65 fold and corresponding ETA is 1/3.

So these are the values associated with the capacitances now there are other values, which will be specified for BJT it is called beta 0 this is essentially same as AC beta n when the input signal is much smaller than 26 millivolt then we can say beta AC same as beta DC, otherwise you will have to specify we are not working at close to much less than 26 millivolt.

So for a large signal analysis do not use beta 0 and beta DC same, but for a small signal analysis this number is good enough that is 200 then we say typically based on the time is 10 picoseconds and hourly voltage can be 2200 volts this is just a little number 20 volt what does that mean if it is less what is that it means, which is the value which will become smaller anyone if only waited is smaller what does that mean.

Now output resistance will be smaller output resistance will be smaller and that is what we are not looking into we want outputs infinite current source shunted by infinite resistance now it may shunt it really by some number so just distribute rather given an army voltage you are actually given something more than what we think it is giving you our zero value immediately from this a slope.

Therefore VA/IC is the r_0 of the transfers are given the given bias then the other resistance is given to us is our DB called base spreading resistance typically of 100 to ohm the collector my collector cap our resistance is higher than a meter device ami emitter is having a dope n plus collector is lightly doped in conductivity 4 and+ is much higher than collector region and therefore resistance wise is the opposite.

Similarly we have a value of R_{μ} which is the junction capacitance which is 10 beta 0 R_0 beta is much higher 100 r_0 is in kilo ohms tubing hounds therefore army will be order of mega ohms and above so it is almost open circuit across see me what is I am saying I repeat in most cases this resistance may be neglected why typically this value may be much higher than the short at the given frequency whatever scheme offers as the impedance.

Let set offers 10 ohms you are shunting 10 ohms by 1 mega ohm so how much is that can reduce 10 ohm may be 9.998 so how do I care whether it is a mega ohm sitting there or not sitting there is that clear in most cases arm you may not be useful and the tool, but if you draw a circuit if you are given a value do find what is it and use it in circuit book of a circuit it does not matter.

If you have a parallel combination will make a parallel comment that clear, but otherwise in general armies are not even because it is normally much higher than of operation is that clear, but when the omegas are much smaller and seem in omega smaller yes nation the army as well and then you will have to find what is the equivalent value that clear, so this is something as a circuit we must appreciate values, which will go whenever we like to do things.

We can evaluate the other parameters for example I say C_{je} is normally taken as twice that of c_{j0} why this is called empirical calculations you just double the value of C_{j0} given to you 10 / is it okay 20 come to forgot the c_{μ} at a given bias 3 volt bias it is 10 upon $1=3T$ upon built-in voltage 0.5 to the power one-third it may give you a value of 5.6, so we can calculate the CV value at a given bias please remember these values have to be calculated for a given DC devices.

Similarly we can calculate the collector capacitors with the substrate which is essentially twenty femtofarad divided by $1+5$ for the voltage given to you upon 0.65 which is built in voltage for collectors all subscription junction one-third this gives you a value of 10.5 femtofarad's and if I calculate therefore the major small signal parameter for me.

Then it is QIC/KT 10 to power - 3 divided by volt okay 38 milliamps forward one can always say it is as well but this is a common practice in analog circuit not to use the unit of Siemens okay modes what is the reason is as I say we always have values which is current by current by voltage by current voltage by voltage so we keep specifying the actual in itself emulator and do not B/VV/II/V.

We write exactly as the units we see on the denominator and numerator exactly that is the terminology if you use many pigments in world or minimums nothing the mouse is perfectly justified but as it convention that what you use.

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5. $C_{be} = g_m \tau_B = 38 \times 10^{-3} \times 10 \times 10^{-12}$
 $= 0.38 \text{ pf}$

6. $C_{\pi} = C_{be} + C_{jc} = 0.38 \text{ pf} + 0.02 \text{ pf} = 0.4 \text{ pf}$

7. $r_{\pi} = \frac{\beta_0}{g_m} = \frac{100}{38 \text{ mA/V}} = 2.6 \text{ k}\Omega$

8. $r_o = \frac{V_A}{I_c} = \frac{20}{1 \times 10^{-3}} = 20 \text{ k}\Omega$

9. $r_{\mu} = 10 \beta_0 r_o = 10 \times 100 \times 20 \text{ k}\Omega = 20 \text{ M}\Omega$

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So I can also calculate the base emitter C_{be} , which is very important g_m times τ_B g_m is given to you τ_B is given to you so it is 0.38 Pico fair please remember this value is so high point so if some capacitance is larger is it across.

The base emitter Junction is it more important or it is not more important smaller capacitance unimportant or larger capacitance unimportant please think of it $1 \text{ upon } J \text{ Omega } C$ is the resistance of or impedance offered across if C is much higher then it will actually shunt the input voltage or it is that correct please remember these values may decided then how much real signal is entering the base before actually the amplification can be seen.

So these values are not trivial but it also depends on the Omega term if Omega is larger or Omega is smaller these impedance may change so sometimes it may be dominant sometimes they may not be dominant and that is exactly what we are trying to say that means the response of an amplifier or a circuit is also a function of frequency is that correct and that is most important for us.

What is the frequency response this is all that is doing is for to finally get a frequency response okay we can calculate therefore the net C_{pi} as $C_{be} + C_{je}$, which is 0.38 pF just be calculated so it is roughly 0.4 pF is the t_{pi} value is that correct C_{pi} is 0.4 pF by similar expressions which we already told you it is r_{pi} , which is β_0/g_m and that β_0 is 100 g_m is 38 million per volt so it is around 26 kilo which is not a very small value please remember α is 26 clones is it good or bad is do.

You believe the resistance across base emitter should be higher or lower if our r_{pi} a cross is very low what will it do it will short-circuit every input signal okay so I really input impedance should be infinite I should allow all the input voltage to go okay but how much is that therefore we will reduce our r_{pi} upon our r_{pi} plus other couple resistances will decide how much is actual V_B main availability is that clear to you.

so that is most important what values you are operon please remember our r_{pi} as something to be β_0 as well as g_m which is a function of collector current and collector current is our biasing current is that correct so bias is also going to decide my our r_{pi} bias is also going to decide my g_m bias to some extent also decide because can calculate our μ which is typically ohm so you can see this value can always they get as far as shunting across Houston.

But if you keep it and solve nothing goes wrong numerically automatically that value will take care of itself is that correct so ideally need not neglect terms but and then engineering you must remember which term should be used and mission should not be use.

Why we want to because we are the smartest guys and we like to do calculations maybe by what we call back up the envelope what is this what I use even a small paper I should be able to tell you roughly how much is this okay to do this you must guess correctly, which values I can equal a base or smallest I can get okay this will develop because this is the first guess I must do and I actually implement the circuit on a board on a chip design when I do a actual silicon chip implementations.

So this first evaluations can be done by just finding okay this is too large this is it so this a frequency this I can neglect also gain is so much this will follow these values are your first cases in all designs and all analysis therefore you must roughly know these are values because when you finally evaluate this should not be far away from these values this is your check okay how much is that okay you have got 100 mega in your actual gasps something.

You made a mistake definitely is that clear so first evaluation should be what we call back up the envelope calculation well are being very small we can be able to do right calculations there this is engineer how much to do well is very crucial in the noise and we are making this word design and design again the reason is at the end of the day you are not going to do analysis in your career you will have to design something for others.

If you are paid for it obviously will be paid for it and since you are an again you will be designing to know where good design you must do good analysis first because you should know what implements when I implement what influences not okay and therefore my design as direct connection to what the analysis I have learnt this course will strictly follow more analysis but why are we doing this analysis because then if I have to design.

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The image shows a handwritten slide titled "BJT (Continued)" with a logo for "CDEEP IIT Bombay" in the top right corner. The text on the slide reads: "Figure of Merit of Transistor", " f_T is called Figure of Merit which is also Common Emitter Current Gain falls to 'Unity' as frequency reaches f_T .", and "We define". Below the text is a simple circuit diagram of a common-emitter BJT amplifier. The input current is labeled i_i and the output current is labeled i_o . To the right of the diagram, the current gain is defined as $\beta(j\omega) = \frac{i_o(j\omega)}{i_i(j\omega)}$.

I must know all of it before hand okay that is the way we think we should do one of the major parameters which all of you our last time I told all of you is the figure of Merit of a BJT it is also

called f_t sometimes it is called Ω_T what is $\omega = 2\pi f$ is Ω , $\Omega = \omega$ so if you some books Ω_T it is same as f_t because 2π is a fixed number okay.

So normally either Ω or f is the value specified to you if it is frequency or it is in radians depends on what value people specify now what is the definition is defined as it is the common emitter current gain when it falls to unity is that point clear f_t means I am varying the frequency fallen I am this kind of a circuit and I want to find at what value the beta which is collector current by the base current force to what value unity but why we want to find this value.

What does that why it is called figure of Merit beyond this f_t what will happen I_C/I_B will be less than 1 so now why are we doing an amplifier which has you gained okay so that is the maximum frequency of operation which you can use in a circuit but you should not use f_t you should typically use $1/10$ of f_t in your analysis because in your designs because f_t is the point at which gain has fallen to 1.

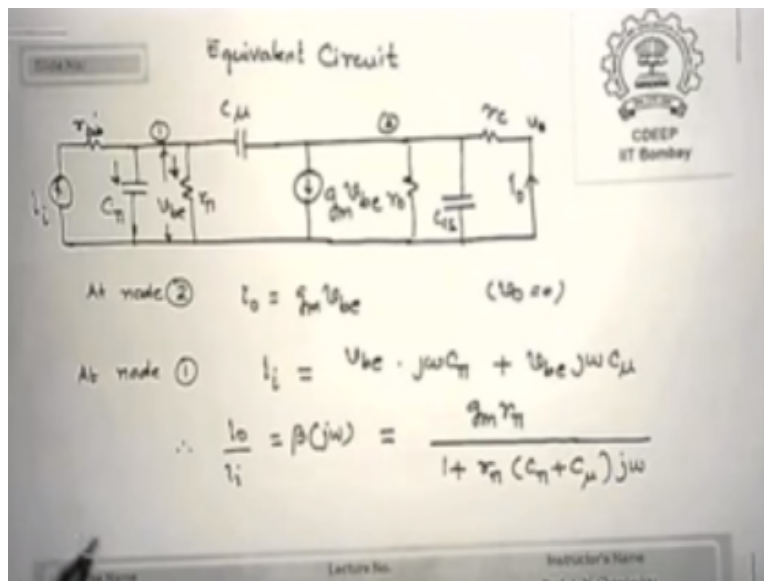
So that limit I want to know where is the gain going to 1 and beyond that I will not actually operate any time and that is why it is called figure of merit how do I calculate this or either evaluate I already said it is going to be common emitter current gain and falls to unity so I say okay I short circuit the output what does that mean I make V_{00} , but the current is not 0 please seek collector current is still flowing in a circuit.

Which I declare is i_{e0} my input current is i_b , which is nothing but the base current both are AC currents both are AC current DC biasing is taken care okay then beta $\beta(\omega)$ is defined as i_o/i_i I_C/I_B and that is a function of frequencies input signal is varying with frequency current disfunctional I am actually increasing the frequency.

Let us see we are at what frequency this term beta $\beta(\omega)$ becomes unity and that frequency will define as f_t okay, we are on unity current game if I have a resistance there, there are 2 parts of the currents that means the actual transistor current is now shared between the resistance and the collector current the collector external current will be done divided by the resistance $v/r + g_m$ times that I am interested in f_t of transistor not the circuit.

So I want to remove that resistor is that correct that means I must put only currents going at the output fish as if V_0 a shop by after we will come back to it if you saw write a small signal equivalent to get I buy something you will have to make the other term equal to 0 okay network analysis a 1 li 1 plus something to make other terms you know only then you can get this ratio is that I will do that in a necessity in real life this is just to give you the measurement.

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So this is equivalent circuit is that here this is my equivalent circuit this is my IIR by right now neglect our DB also I may neglect our μ , I may declare the leave this IR es also a neglected actually you can forget about our CS well if you wish by making output shorting I made V_0 but the i_0 is flowing inside and how much is i_0 therefore and there this node 2 GN.

Maybe is that correct now something I made a mushy in this my assumption is not much current is flowing across C_{μ} okay but that an assumption which is not very bad as of now will show you later it may not be as good an assumption ok, so $r_o g_m$ times V_B this is the current only current flowing in this circuit okay because V_0 is 0 so no current in r_o is that correct no current in r_o no current here so only this current source is same as the collector current.

If you see the input current I_i you can say $v_v \times j\omega C_{\pi}$ is one current here, where one current is flowing here and one current is flowing here is that okay last people I am is divided

into clumps one through C pi other through our pi again assumption is very little current is flowing in you okay if that is to be taken care little complications will arise more accuracy can be built but as an engineering that is going to up.

So if I write ours equal to $v_{be} j \omega c_{\pi} + v_{bc} j \omega c_{\mu}$ this darf i I made a mistake plus v_{be}/r_{π} and if I collect a $0/AI$ from these 2 equal node equations I can get a $0/IR$ is $g_m r_{\pi}$ upon $1 + r_{\pi} c_{\pi} j \omega + C_{\mu} j \omega$ into 0 is that term here I got III got a 0 and then took the ratio of i_0/I I and that what is the way I define that output current which is collector current I is the base current the ratio is beta.

Since both currents are functions of frequency so is the beta is a function of frequency so I have a beaker $j \omega$ I $g_m r_{\pi} / (1 + r_{\pi} c_{\pi} j \omega + C_{\mu} j \omega)$ if you are familiar with Laplace transforms I hope so we may start using s instead of $J \Omega$ but I thought initially maybe I will show you later on maybe will not use $z \Omega$ term you start using s normally as everyone of us have been familiar just for the few days.

You may continue your ω then we will never use the Ω term and maybe add an meaning we will put $s=0$, so yes the current going through this is the conductance multiplied by voltage g_m this is g_m this current how could I have taken care in this current also now in this case all that I have no current on this side but this current I have taken so there are 3 currents flowing here one through this please remember what is voltage here zero $v=0$.

I assume zero so I can find this current which is $V_{be} \times J \Omega C_{\mu}$ this current because this voltage is going to zero so I calculate this current I calculate this current I calculate this current is that okay so that is what I already said RC as far as since there is no other term there is a RKI said drop right now that is what I said you know that is what I started neglect our key desire right now.

We are not worried about, so this is clear is that last people is it clear to you, how day what did I do I calculate currents here I calculate current here and took the ratio and that ratio we know is beta $J \Omega$ is that okay so we move for that and we say if I do this, so okay maybe we can

keep it here so now to make this $\beta J \Omega$ equal to 1 what is the condition it will get to me let us put at okay maybe we will put a next slide at $\Omega = \Omega_T$ we say $\beta J \Omega$ is 1.

Now we can say in normal cases since Ω_T is very high much higher frequencies in numerical numbers if this term is stronger than 1 if I take square of this plus 1 square or under root of this magnitude why this term will start please remember our party pass you mean - Ω^2 plus for this one is much smaller compared to this number and if I do so then I write our $\Phi_C \Phi + \mu \Omega E$ is then Ω_T is $g_m r_{\pi}$.

If you wish to keep one I had no objection if you wish you can keep this one and then write one further it does not matter but then there is a 1 upon term come so right now I do not want to complicate so I will just write $r_{\pi} C_{\pi} + \text{view a what is } g_m r_{\pi} \text{ what a } g_m r_{\pi} B \tau_0 \text{ what is } \beta / r_{\pi} g_m \text{ political certificate came you are right so } \Omega_T \text{ is what } g_m \text{ upon } C_{\pi} \text{ and see what is } g_m K T / q \text{ sorry I am Wilson } q I_C / K T / C_{\pi}$.

So are you now getting a point that when I see becomes constant what is the r from where I fix my I see I just showed you by seeing if I fix my bias, I fixed my eyes, if I fix my I_C ima fix my C bias μ and G_M together all 3 of them are fixed by me so this Ω_T then becomes the figure of Merit is that current what is the definition I set for it whenever β falls to 1 $\beta J \Omega$ Falls to 1 that is the frequency at which transistor will no more give you current gains and if there is no current gain.

There is no question of I times our output if you put the voltage will be less than input voltage, so even there will not be any voltage so if I am not getting an amplifier I am not getting in amplifier and any amplification and why do I do it okay for this statement we may qualify later it is not really necessary that the amplifier should have again less than should not have gain less than one you may not call that you will say so many TVs it does not matter for me with the gain is less than one in some case it will show you.

Why we say so is very relevant for us as of now we say amplifier should again larger than one then we will call amplification that correct so Ω_T is therefore what it is called figure of

Merit and this is technology constraint because please remember the values are C_{pi} assume you are decided by the doping in base emitter junctions and base collector Junction the lifetimes there I assume the based on the time I should accept the capital IC part, which is external to me the rest parameters are internal to a transistor.

So they decide what gm/CI am going to get this normally in one word they say gm/CC in so what gm/CL now you are understood what did I say so why it is called figure of merit because it decides the maximum frequency of operation calling an amplifier circuit as an amplifier is that clear can you get me a unity gain amplifier unit again is not this oh sorry when the beta becomes starts falling.

So what is this expression which I just showed you this expression if I plot on a frequency scale what do you what will you like the beta times Omega if I plot what will happen you start looking at this expressions if only is much smaller is that correct if Omega is much smaller this term will be smaller than one because $C_{pi} C_{Mu}$ femto farad's and something comes our pi is that correct.

So at higher frequency this term will start dominating but for lower frequency one will start dominating so how much is the gain at very low frequencies $gm r_{pi}$ which is β_0 so at low frequencies gain roughly is because 0 as you start increasing the frequency what will happen the denominator terms will become higher and higher and beta will start becoming lower and it will fall it will start falling in a log scale.

If you plot this will start falling at this point actually it will go by asymptotes but this frequency when the beta falls by 3 DB or $1/\sqrt{2}$ of this beta be $\beta_0/\sqrt{2}$ 3 DB down okay this value is called beta sorry Omega beta what is this value called Omega beta this frequency how do I calculate from here you can calculate find the 3 DB means $1/\sqrt{2}$ put this is equal to $\sqrt{2}$ and whatever value.

You will get is called Omega beta it is $\beta_0/\sqrt{2}$ is that correct $\beta_0/\sqrt{2}$ this Omega beta what is that significance of Omega beta and this value Omega T how can they be related anyone,

okay you do this and find this $\Omega_{\beta} \times \beta_0$ is essentially Ω_T is that correct essentially ω_T .

So what is the Ω_{β} value you can immediately this is of course not exact like this so how do I calculate Ω_{β} otherwise I calculate Ω_T which is $\frac{g_m}{2C_2 \pi C_n}$ and then just divided by β_0 and I get my Ω_{β} and what is this value I should use for anyone what is the β why I am interested in Ω_{β} because it is here up to this frequency your amplifier has a reasonable gains available is that correct.

If you go beyond Ω_{β} of this β will start following still gain but it will start falling is that clear at Ω_T no further gains okay so now can you say that not even 10 times how much I should have a Ω_{β} roughly will be β will be 100 or 200, so Ω_{β} will be 100 or 200 of Ω_T Ω_T maybe let us say hundred mega a 1 gigahertz or something or 10 gigahertz the operating frequency is that right.

What is Ω_{β} called the maximum operating frequency is Ω_{β} for us is that current please remember I can certainly go beyond Ω_{β} as well till up to what Ω_T but I am assuming and I know when I am designing that my β is following, but I am taking care by other parameters the lift of the gains okay by g_m for abandonment which worker but I know I have some advantage of increasing the frequency but beyond our Ω_T .

Of course I will not use it but preferably I will only use my transistor in range from 0 to Ω_{β} this is called my operating frequency maximum operating frequency that is what this number is known must be known to us I will evaluate Ω_T divided by my β_0 value and say okay this is the uppermost frequency okay is that clear to you therefore this is how the analog circuit bipolar circuits actually gets limited both on frequencies as well as gains because if you want to make gain larger or g_m larger.

Should I increase, I want larger and larger to get larger gains what should I increase I see what is the problem if I increase I_C okay your one is worse key that I_C may be so high that device saturate let us say it does not even now then what will it increase something else you are to some

extent yes but there is a major worry starts if the collector current or the current in the circuit start rising device V times I what is it power so the I showed you yesterday first slide power in my major worry.

So power dissipation will start anion saying and once power dissipation okay what increases temperature increases all my parameters of device are a function of T okay so they keep changing beta changes are β everything will change with temperature and now as they change and you will find very interesting some of the parameters have positive coefficients, so they may further boost I_C , we further boost.

I see so what will happen it may actually burn or what we call thermal runaway device may actually burn that clear for even if what she said is correct first a device may enter saturation but let us say it is a gauge it does not enter even then your circuit may actually fail it then is that clear this is the reason why we say there are limitations of everything which we were here is that otherwise on a normal mode many things can be tried.

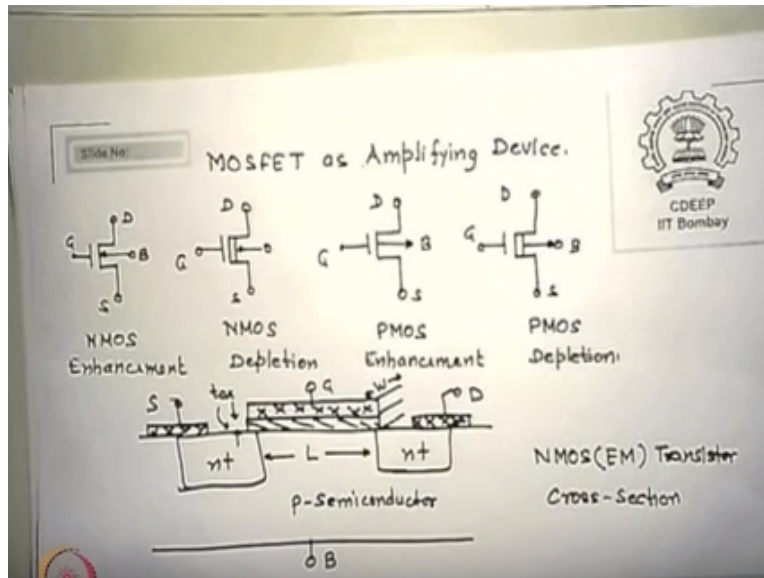
What do we do like a you open any computer or any other system there is a huge fan on the backside of the system okay so it keeps cooling so any desktop system I can keep a good coolant cooling system and I will never allow temperature to rise but on a chip which is our major worry when I actually make a chip there is no panel because it is a package inside there is no fan inside okay, so this chip will burn irrespective what you do is that clear to you and therefore in designs we must worry about the limitation and limitations come from the theory of the transistors.

Which we are this is that current so why all that so far we are doing to show you because we wanted to convince you that why we are getting limited otherwise in why not work everywhere whatever value has attitude usually something will come but it may not be useful as far as circuit circuits so this is a generic must know where we are bounds match but on a lower bound upper bound we must work within the bounds okay.

Let us do something more okay the major device of course as I say why I keep teaching my bipolar because it though every book will start with bipolar so I do not want to take you away

immediately from them but the first amplifier which we are going to design will not be bipolar we will first do MOS design and then say okay.

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Equal and bipolar okay so now within the next technology of address or next device of interest which is based on MOSFET here is the N channel MOSFET maybe if there are four possible MOSFET, we may use one is n loss announcement mood please see a symbol this is a cross section of N channel enhancement mode transistor how many terminal MOSFETs have poor please remember MOSFET is a 4 terminal device actually.

So is the bipolar I show you substrate is the foot there also in circuits actual terminals are 4, but the normally substrates are grounded with the other grounds and therefore you see you will always have for tonight donor of course you can connect this bus this substrate, as well as source common then it will also become 3 terminal device, please I have figures and channel enhancement mode transistor and MOS.

The second is n channel depletion mode MOSFET and complementary to them is p-channel enhancement mode and p channel depletion modes plus symbol these are just shown you to you whatever symbols I am going to use in my course I just thought I should show you my circuit symbols in the case of enhancement mode and channel the verse arrow is inside this array is inside this is the symbol for N Mo's enhancement mode that okay.

N channel enhancement mode the substrate terminal arrow gets inside that is my symbol by contrast basis is a complimentary P channel transistors the error is oppose it coming out towards substrate B is called bulk or subscript B is called bulk other name is also substrate, so the arrow in P channel is out arrow in n channel is in there are 3 terminals otherwise gate drain and source for each of them and fourth is the bulk.

Now what is depletion transistor you are how have they discussed okay if the channel exists pre-exists before the gate voltage is applied then there is already a current flowing between source and drain independent of gate voltage essentially.

What we are saying is the following, I do not if you are drawn this is standard you can see in any book including the book which I happen to know quarter for that if you do not by your choice any of the book you buy is fine. If you use library books fantastic absolutely no problems.

So if I plot okay and channel n mas this is the third one is a normal and mass enhancement mode I am drawing what is called as what characteristics this IDS- IDs is at what point very good someone has had transferred drain source current is the output current V_J at the input and if it is called input to output transfer okay so it is transfer characteristics you can see at zero bias V_G s no current that start increasing - channel will start appearing at certain voltage.

We call terminal voltage or threshold voltage current will start rising sufficiently efficient electrons will remain available in and channel their P substrate and channel this voltage is called threshold voltage where current starts substantial it is higher and channel negative V_T has some advantage this is called depletion transistors what is it trying to show you in depletion even at 0-

There is a current flowing and to shut it off I will have to apply a negative $V_T = -V_T$ value which will make this electrons which were sitting there must deplete they must go away and that is called negative threshold voltage - μ and the upper 2 are just the complementary of the only field at sign for p-channel or - ID as - V_{GS} - everything I put are shown on the fourth quadrant but that is shown essentially on the fourth quadrant okay.

These are 2 of our fourth quadrant these 2 are the first quadrants is that okay these first 2 are on the fourth quadrant second 2 are the first quadrant curves what is V_T value we said we say in a transistor whenever inversion channel comes we say that voltage of - we define as turn-on voltage or a threshold voltage or not only circuit people call the device we always called threshold.

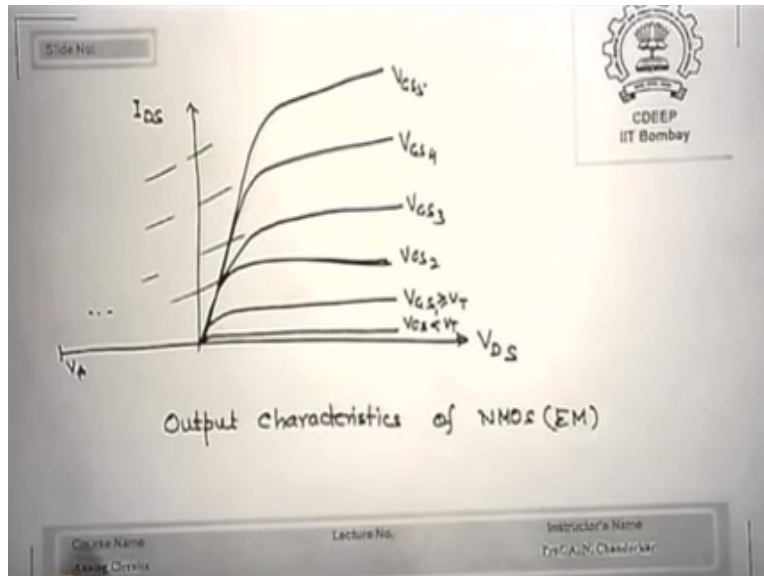
So the threshold voltage by theory which will not use now but just to show you for both N channel p channel common formulas in specified 5 s what is finance load function difference between metal gate, as well as the semiconductor r-5 what is NI or in d/9 therefore + or- both signs in and I will b or anyone I will be now the P channel device a ND y NI will be - because potential a bar is to get your load is positive opposite happens in both sides okay.

Please remember E/Q is V, but a sine QR the - sign is that correct Q as a - sign and therefore potential energy rise plus means potential negative energy going down means potential positive band diagrams for up deep yeah okay this QOX is the fixed charges in the oxide normally unless we do some radiation or something we force it to become lower or - otherwise QOX term is always positive.

So this always is negative what is C_{OX} value essentially capacitance of oxide is ϵ_{OX}/T_R this is oxide capacitance per unit area gate area and plus - QBVHQNA depletion layer charge - NAXD or QMD x T is that correct so that is + - is that correct -NA XD will be - Q and EXT will be plus but this sign is - outside so - QNA XT will become positive because of the outer - sign and + K and exp will become - - sign so what is it trying to show you V_T can be known to us from the device side.

I have no control once given me a transistor my V_T are given to me I am this bothered what is 5ms what are fixed charges why they are operating by band diagram goes like this or goes like this help to them so we will now onwards may not use these expressions but just to give an idea that from where they were appearing.

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Now typical output characteristics of a bipolar mass transistor is of this I_D s versus V_{GS} at different - values are plotted here whenever - is less than V_T there is no inversion channel but there is a small current what is it because of - is less than V_T so now in version channel firstly this segment itself is not correct why do I say because the definition of inversion was given when the wind band bending is equal to 2 times the fire but between five and 2 pi f the inversion was existing so one reason was but I showing it even went to p.

I they still current going on from where if you see the bodies quickly and that is very into circuits also now these are 2 diodes even if gate is not controlling any charge here these 2 diodes are reverse biased diodes reverse bias diode will constitute reverse bias currents this is the leakage current junction leakage current which is independent of what oxide does or does not is that clear to you these are diode reverse bias currents so leakage currents are always present independent of now what is the first slice.

I show you that is becoming now major worry since we are scaling, scaling, scaling, we are losing everything the currents in these are increasing this saturation currents are increasing normally because the doping is amusing see these currents are increasing and on currents I cannot increase because size will increase and I am reducing the size.

So what is happening I told you one bad thing about our good thing for you that the recent MOBA is people say keep it on because the off current is much larger than the off current, so get the battery, drain, environment draw energy so bad, okay so in this region which in a digital way use very often, what is this region V_G 's less than V_T or zero roughly off state of the transistor okay.

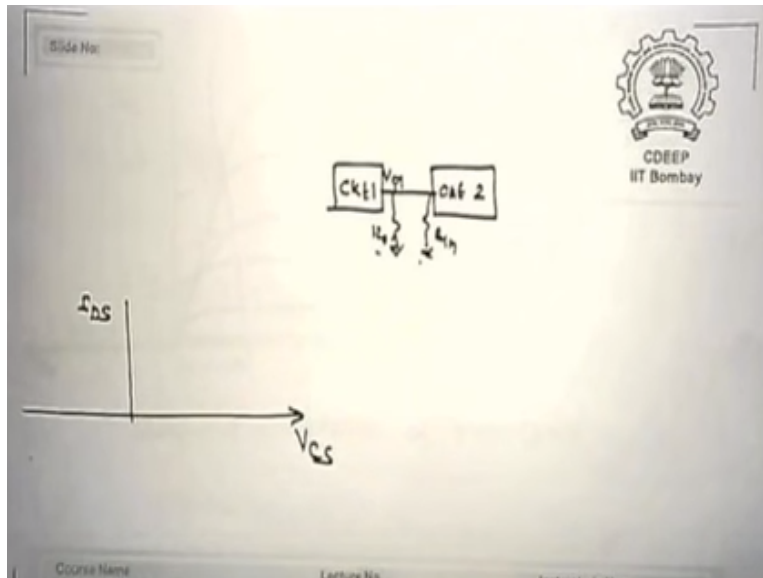
We say 0 current, but it is not zero at some finite small current then we say if I will start increasing V_G further beyond V_T inversion channel will exist and current - will start each has one characteristics now this essentially means if I increase - I am going to increase ideas but show is if you see at this region at least in this region.

Those slopes are not very much but there is a finite slope that if I increase V_G current still increase marginally but if you see this region for every - if I increase V_G current increases linearly roughly linear so what is this region called linear region of a MOS transistor what is this region calling transistor because characteristics roughly looks to be saturated this is called saturated region.

These names are opposite in the case of bipolar in the case of bipolar this region we called as saturated because they are both junctions became forward bias okay the maximum collector current was made available so there this region we called saturated in the we call this region as such is that clear slight definite why the definition came the first difference you should realize between bipolar transistor and a mass transit what is the input of a MOS transistor.

We say all the time - that is voltage driven what is the input in the case of bipolar current input base current so it is a current driven circuit eyes, why so the first worries are in the case of bipolar obviously you will find the input impedance will be lower, is that correct because there is a current flowing so V/I since I will be larger of resistance at the input will be always smaller Q_{IB}/KT , which is HIB as we call or KT/Q_{IV} .

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Where what do we really want larger input resistance can you tell me, why I am saying so from the circuit point of view I have one circuit here circuit, one circuit one and I am connecting this 2 circuit 2 now it has some input impedance and it has some output impedance is these 2 value something to play again if this value is infinite let us say R_n then this device will not be loaded or this will not share currents from here.

Otherwise what will happen these 2 transistors will parallel and this value will start influencing the output of the first stage itself if this resistance is finite in 0 or small then these 2 will become smaller and V_0 will be then function of second circuit which do not designer will like occur I do not know what where I am going to connect.

So how do I decide for the first block what I am going to connect next so ideally my R_n would be infinite I also on my order to be as small as possible as P_{in} is a serious resistance because I do not want large currents to flow there okay now if that is so happen the decision is how to control auto and R_O and R_n MOSFET has the biggest advantage what is are in to see a MOS transistor.

What is between this between gate and transistor oxide large resistance large resistance is that become hundreds of mega ohms which means its input impedance is extremely high so MOSFET circuits are better because they can be directly connected now. Heath of bipolar mica is k-beach may do new k-, book by Dunlap Auriga Muskoka Bolton buffer.

I will have to match resistance on this side and also there is a then if you are one huge box boy fight will occur then if there is a huge wrestler and a smaller wrestler they cannot fight, CMOS size format but they both are saved so buffer is a very important circuit in all bipolar circuit it is not bad import at not saying that not important that important in the case of Boston not that it is not required not they will never use buffer will open anytime.

But, in general what is the advantage of bipolar over mass and what is the disadvantage of that bipolars are larger gm ICS are always larger than ideas for given voltages collector currents will be larger compared to the drain currents is that correct what does that mean for the same voltage operations GM will be larger for bipolar and J will be smaller for most understood.

So what will be the voltage gain from same currents and same voltages bipolars will give higher gains than MOSFETs what is the disadvantage is giving it is consuming larger power its input impedance is low is that correct whereas in the case of MOSFET is input in finances very large and closer to infinity and currents being smaller what is it going consume power much lower power is that correct.

So you must know when to use bipolar and then so larger gm k4k advantage over Omega, beta higher high to fall be gone over to Omega t be higher over so higher bandwidth can also be attained by bipolars compared to MA I do not say that mass does not is not coming closer to bipolar but intrinsically one sees bipolar have a larger power larger bandwidth and larger gains.

Whereas most on the stirs have larger lower bandwidth lower gains and lower power but then we will continue to use everything lower these days because power is our major criteria everywhere ethical mobile laptops H voltage hand rail system and they will start draining power in the next seconds that clear so we are looking for low power so that is why I say most ancestors are preferred blocks compared to this.

So this is not only reason we were looking for digital which is much better in the case of in case of mass than in bipolar and therefore will prefer MOSFETs as a universal device that universal

device but if I want specific circuits which has a higher bandwidth higher gain then I will look for bipolars I will look for bipolar and therefore bipolar circuits though the only six percent of the world semiconductor IC market has only 6 percent bipolars 94 percent and I am told long soon it may be 98 percent will be MOS and only 2% with bipolar.

So maybe after verse I may not be teaching but you will not teach bipolar at all, your opinion okay, so having told you that this is our math characteristics we must operate we were in this region, which is our saturation region what is the saturation region and what will happen in linear mode we will say in a linear mode V_{GS} has direct relationship with I_D so it said resistive circuit okay.

I would now prefer that this current may remain roughly constant part given V_G V_{GS} or varying V_{GS} only should change with I_D what does that mean external voltages should not influence too much of the output current only the input should change okay, I_D output should be seen so I will prefer to work only this if I extrapolate these which unfortunately this length is not good enough for me.

If I extrapolate this as I did in my poll where they will meet at a point which is not really early voltage in stricter sense what is invested to sense because this early effect is not seen in MOSFET really is that correct but we say as if they are same so we say V_A , which is early voltage for the case of MOSFET also by same logic what will be the R_0 for most undisturbed V_A by I guess okay will be the R_0 so given the biasing I_D s given the early voltage.

I know my output resistance is that correct V_A by ideally remembered at this point for example if I buy US V_A plus this much I must add but I do not know why I tell you because we reading will be how much 3 world 1.5 volt 1.8 volts how much will be this 100 volts T volts so $50+1$ point 5 divided by so much biomass 50 by this and 51 by this will not give you much a difference and therefore we say V_{naught} many do not write this Plus this divided by this we just write V_A by ideas in reality.

This must be added this must be either, but numerically 100 may one would add by the same number will not matter okay, you are done this theory I just give the expression for you and then when the transistor in linear mode what doing my linear mode just now actually this mode what is the me what do you mean by linear mode in transistor.

When the channel exists between source and drain throughout okay some symbols may be quickly seen there sorry I think we just repeat between source and drain we have a channel length L the third dimension there is no duster here, but okay maybe this you can see this is your source this is your drain this is your channel length but this is 3 dimensional device.

This is your width okay so this width is shown on the third dimensions my definitions is I always have this exists XY and set this is how I define so along the third axis are the width along the y axis I are the length and I have the best along XX this is how we define in our device theory so I have a fixed width of the device fixed channel length of the device then this oxide thickness t_{ox} is also fixed by the process people.

So capacitance of this is also fixed ϵ_{ox} by T of what is K_{ox} dielectric constant of oxide is how much silicon guy $12C/9$ okay, already if you are numerically for constructive but 3.9 okay what is ϵ_0 value 8 point a queer very good 8.854×10^{-14} , please remember an in this course will not require in device.

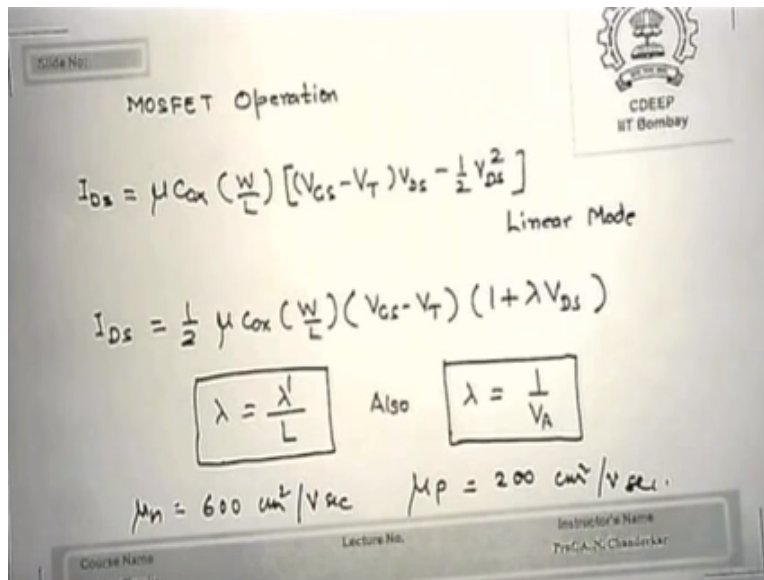
If I am teaching I insist that you use CJ system and not systems because there is huge problems in microns conversion to meters down so here of course within units so channel length channel width oxide capacitance ease are the specific given by transistor people I do not care what the values they specify once given to me I will use this so I had derived this expression by a simple theory $\mu \cos W/L \rightarrow VT$.

What is okay let me show again if I apply gate voltage with reference to source, which is grounded with reference to B , which is grounded and I apply V_{GS} at the drain this is V_{GS} across Y V_{GS} is across x -axis is that field effect layer to you field effect is near to you BG s is along X

direction if creating a electric field along this direction current is along this direction the current transport on a lateral plane is governed by field across all orthogonal to it.

Therefore, it was called field effect would be the field which is controlling the ids along the lateral line that is why it was named field effect is that correct so since this is going to control IC mu is the mobility of the carriers so should I use N channel device or a p-channel Device's and channel device because beyond is much larger than movie.

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How much is larger how much of this mu and channel or p channel can you tell me the ratio but how much is mu in the on the stairs and how much is moving the best of mu and you can get in a mosque instead of 600 centimeter square per volt second how much mu, n is the best of the value you can get 600 centimeter square volt second and mu P as he said is not even best of it is 200 centimeter square volt second so what does that mean.

Why this is not 1350 or 1300 and this is not 500, but the electron mobility is essentially in 1300 or 1350 sometimes even 1500 possible the whole mobility in silicon is just 500 okay why this number is so small, it is called surface mobility there is a oxide surface sitting on the top, a lot of recombination going on there okay.

So these are much smaller so these numbers should not be used at 1300 and 500 as in the case of bipolar because there is a bulk transport here it is surface transport okay please look at these numbers carefully so can you think this value V_T what is it essentially tells if V_G exceeds V_T then only inversion starts is that correct so this value in circuits we define this value V_T is called over voltage what is it called over would be okay this is very important some books I do not know any other book may be called V_{Xs} is that correct why it is called XSR/V_T .

When you go you need an current age available to you and therefore it is called over voltage or excess voltage now in the linear mode please remember the condition, which we are applied essentially each V_T is greater than V_G is that correct, why this condition is valid because at the drain end - please look at the drain end voltage this is this is V_G .

So what is the difference at the drain end of the difference this voltage V_G if I want inversion to appear at the edge what should be this greater than V_T , which means V_T should be greater than V_G so for inversion channel to go till drain V_T must exceed V_G that is the point where when we say it is a linear because if V_D is smaller this term can be neglected.

So I get I_D s proportional to V_G this is constant V_0 is constant I_D s is proportional to V_G therefore it is called linear mode of operation since V_G is smaller than, but as you come closer this linear relationship is not linear it starts bending partly because square term starts coming into picture however if the condition is such that $V_T < V_G$ there will not be any channel at the drain end and larger the V_G first the channel may not exist here when $V_T = V_G$ $V_T = V_G$ no channel here okay.

If V_G - we case still smaller than V_G even here it will be $0 < V_T$ here, so channel will become saturated or pinch of it and the pinch point will start shifting towards source as V_D starts increasing is that correct that means the effective channel length is not L , but it is something L the depletion layer which is a function of this doping and this bias how much is V_D will decide the depletion larger the depletion larger will be depletion layer and smaller will be L effective what is the importance of this word.

I am saying if you see this expression if L becomes $L_{\text{effective}}$ and smaller then what does that mean ideas will increase or decrease increase because L is decreasing, L affecting decreasing means are increasing exactly what you saw in the characteristics slope if media starts increasing the depletion layer will start dancing L will become smaller and there will be a increase of current with VGS as well is that clear to you is that clear.

That is why the slope is appearing for you okay therefore the slope is appearing for me so first we said in the saturation normally we say it should be independent of VGS, so normal currents what do we write this should have been over normal sorry if I would have been if ideal saturation would exist I say I_D s will be half MOS W/LVT square okay.

Such but now just now i said that if VGS increases and if a tube actually changes okay and therefore that if it can be taken care by additional term which is $1+\lambda$ with VGS, which is λ is the saturation factor λ is saturation factor and it is defined by in actual this λ dash/L what if this also means large as a channel length λ will be higher or smaller this is a parameter this is technology parameter, which is fixed for a given transistor.

So larger the channel length smaller is λ smaller in λ here is good or bad, you look at it if λ is smaller this will be independent of VGS is that correct what does mean R_0 is how much if what is our I_{D0} Delta I_D of by Delta media see if they does not change with VGS our I_{D0} is infinite ideal is that correct.

So I would prefer channel lengths to be higher and higher and higher such that λ is smaller such that λ VGS can become smaller, but this means channel length larger if I do what will happen to actual ideas value decrease ways we will see GML aesthetically so one advantage I bought please remember I am saying GM decreases if I increase channel length. However if I define R_0 which is nothing but related to λ so is that correct so what is R_0 is higher when λ is smaller which means channel length is higher larger.

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