

Audio System Engineering
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Lecture - 23
Microphone Sensitivity

Now, in this you have heard about the different kinds of microphone, they are directivity pattern, they are frequency response and they are sensitivity. Now, in this lectures, we details investigate what you mean by sensitivity of a microphones, how the microphones sensitivity is desired or defined or how to measure you can say how determine and then we will discuss about what will happen if the microphone is connected to the pre amplifier and in which condition it will be deliver the maximum power.

(Refer Slide Time: 00:59)

**1.2.3 Electronic Industries Association (EIA)
sensitivity, 0dB = EIA standard SE-105**

Reminder	
1 bar = 1.00×10^5 Pa	1 Atm = 1.031250×10^5 Pa
10μ bar = 1Pa	1 Atm \cong 1 bar
10μ bar = 10 dyne/cm ²	20μ Pa = 0dB SPL
$1\text{Pa} (10 \mu \text{ bar}) = 20 \log \frac{1\text{Pa}}{20 \mu \text{Pa}}$	= $20 \times 4.69897 \text{dB} = 93.979 \text{dB}$
	= 94dB SPL
$20 \mu \text{Pa} = 0\text{dB SPL} = \text{Threshold of hearing at } 1 \text{ KHz}$	

And what is the electronically standard sensitivity defined by electronic association in electronic industries association EIA.

(Refer Slide Time: 01:04)

1. Microphone Sensitivity

1.1 Definition – may be defined as the output voltage/power of a microphone corresponding to a given input sound pressure level


- it is often expressed in dB referred to a particular voltage / power corresponding to a specified SPL.

1.2 Sensitivity Expressions

Microphone sensitivity may be expressed in any one of the following ways.

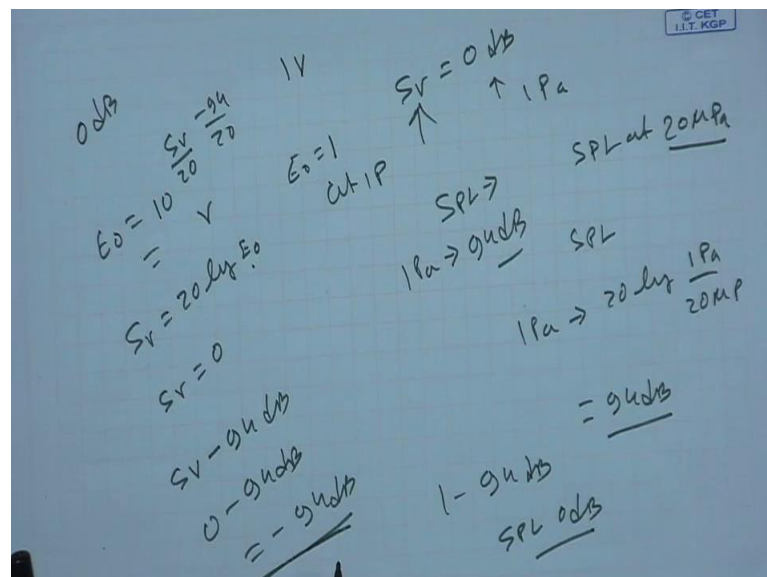
1.2.1 Open-circuit voltage, 0dB = 1V/Pa = 1V/10 μ bar.

1.2.1 Max power output, 0dB = 1mW/Pa = 1m μ bar.



So, as per the EIA definition, the sensitivity of the microphone is defined as that how the voltage produced by the microphone for a given 1 Pascal sound pressure is called 0 dB voltage sensitivity of the microphone.

(Refer Slide Time: 01:13)



What are the meaning of that that suppose this is the my microphone, I will say the sensitivity of the microphone is 0 dB, if I expose this microphone to 1 Pascal sound pressure and if it produces 1 volt output at open circuit condition. So, open circuit voltage 0 dB means, so sensitivity is 0 dB of the microphone means if I produce a 1

Pascal sound pressure at open circuit condition of the microphone, if it produces 1 volt outputs then I call sensitivity of the microphone is 0 dB. Similarly, power, it may be voltage sensitivity, it may be power sensitivity. What is the power sensitivity maximum power output of a microphone we will said 0 dB or 0 dB power output of the microphone is defined as if the microphone is expose to a 1 Pascal sound pressure, if it deliver 1 milli watt power, then we said the power sensitivity of the microphone is 0 dB.

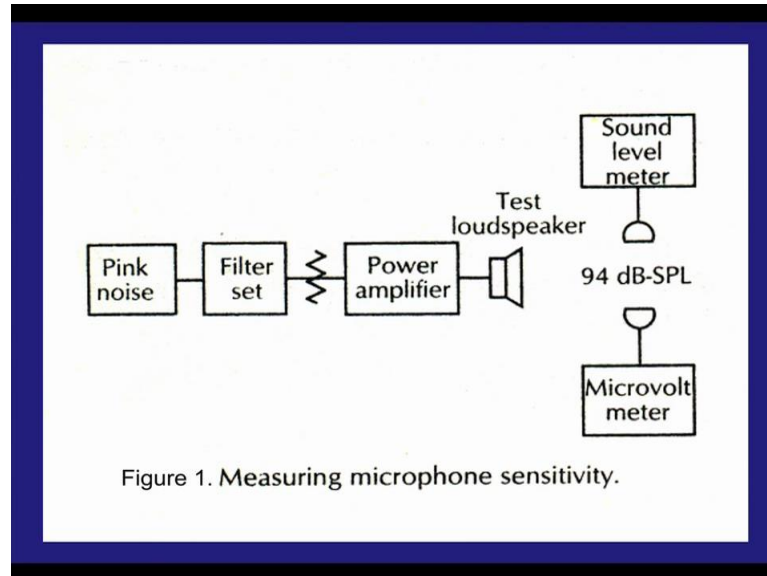
So, in the specification of the microphones, both can be written or one can be written. The voltage sensitivity of the microphone 1 Pascal pressure 1 volt; power sensitivity of the microphones 1 milli watt power 1 Pascal pressure, now, if I say this is one Pascal pressure is 0 dB, if the sensitivity of the microphone is 0 dB, then if it produces by 1 Pascal pressure. Now, if I say if I connect this microphone in or if I expose this microphone in a threshold of hearing SPL, SPL at threshold of hearing which is 20 micro Pascal in air threshold of hearing 20 micro Pascal in the refer as 1. Then how much voltage or what should be the sensitivity of that microphone at that pressure or I can say what should be the voltage output of the microphones in dB.

So, I say S_v is equal to the nothing but $20 \log \frac{E_0}{20 \mu\text{Pa}}$ the voltage produces at the output of the open circuit condition of the microphone. Now, if I say if E_0 is equal to 1 volt at 1 Pascal pressure then S_v is equal to 0. Now, if I say some microphone places in a sound pressure level SPL, where it is just threshold of hearing then what is the sound pressure what the dB in 1 Pascal. So, 1 Pascal is equal to $20 \log \frac{1 \text{ Pascal}}{20 \mu\text{Pa}}$. So, 1 Pascal SPL 1 Pascal SPL if I expressed in dB what the dB it is almost 94 dB, because it is 20 into 10 to the minus 3, if you calculate that mathematics it will come almost 94 dB. If it is 94 dB, so one Pascal sound pressure in dB, it is 94 dB. Now, in one Pascal it produces is 0 voltage, if I expose in minus 94 dB is the threshold of hearing (Refer Time: 05:19) Pascal. So, one Pascal is 94 dB that means, if I expose the microphone in SPL 0 dB that means, as threshold of hearing. So, pressure is drop by 94 dB.

So, S_v minus 94 dB, so it is 0 minus 94 dB is equal to nothing but a minus 94 dB. So, same microphone is the same bit of the microphone is 0 dB then the microphone sensitivity at threshold of hearing assume is nothing, but a minus 94 dB. So, how much voltage it will be produces if it is one volt E_0 is one volt means 0 dB. So, I can say that E_0 is nothing but what is E_0 is 10 to the power S_v by 20. Now, S_v is minus 94 divided

by 20 into the 10 to the power. So, I can get that voltage, I will get output of the microphone.

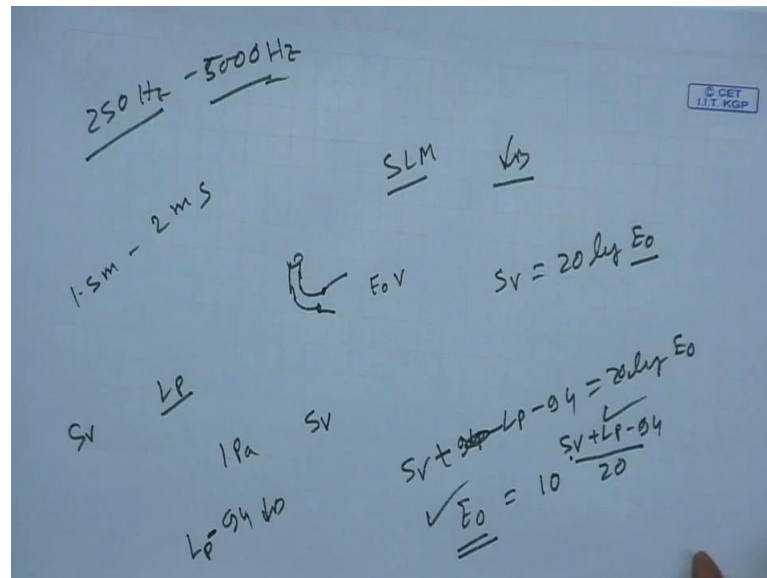
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Now how do you measure that microphone sensitivity? So, microphone sensitivity is measured in a condition, what are the condition let us see the see the setup this is the setup. What is the setup I required a pink noise source, which is electrical signal, source and passed through a filter, go to a power amplifier, which amplifies that signal and connected to loudspeaker, a loudspeaker produces the sound. Let explain one by one why the pink noise source suppose I want to test these microphone what is required I to expose these microphone in a sound pressure level. Now, you know the sensitivity of the microphone is frequency dependent, but for a particular frequency range, I can make that microphone frequency independent that we discussed in past lecture.

So, now, if I expose this microphone in a particular sound field, so I would produces that sound field by some loudspeaker, so that is why this is the loudspeaker. And to produces the sound I required a power amplifier and power amplifier required desired acoustic signal. What is the desired acoustic signal, I generate the desired acoustic signal of a particular frequency range by this filter, at input of the filter is a pink noise source that means, all I applied input to the filter all frequency with the same power same amplitude power amplitude then passed through a filter for a particular band.

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If I said my filter 250 hertz to 5 kilohertz which generally hertz in microphone 5 kilohertz then the acoustic signal produces for the loudspeaker is nothing but a acoustic signal of the frequency 250 hertz to 5 kilohertz. So, this filter hertz upper cut of frequency 5 kilohertz lower cut of frequency 250 hertz. Then this sound is propagated in the air, let there is no disturbance of the environment, there is nothing no disturbance of the environment and this pure pressure field this is no pre field it is no there is no reverberation version, it is not pre field, it is not I can say it is not reverent field. So, it is pure pressure field. If it is pure pressure field then what will happen once the sound is propagated the inverse power square law will be applied, the pressure will be dropped. Now, after certain distance let us 1.5 meters from the loudspeaker 1.5 meter to 2 meters from the loudspeaker, I could take sound level meter.

What is sound level meter? SLM- sound level meter measure the sound pressure level in d b; that means, respective threshold of hearing it dB it is measure. So, what is one Pascal should be reading 94 dB respective threshold of hearing. So, if it is I put the sound level meter and I increase the gain of the amplifier till the reading of the meters is not 94 dB; once the meter reading is 94 dB I fix the gain, and I have continuously sound is produces at 94 dB SPL at this point.

So, now I reach the 94 dB SPL, once I reach 94 dB SPL, I remove the sound level meter and put the test microphone there. So, I put the microphone there, let this is the

microphone and two end two electrical end of the microphone connected to a micro volt meter which is micro volt meter. So, the reading of the microphone meter, if it is E_0 volt then what is the sensitivity of the microphone, so 1 Pascal pressure produces voltage is the 0 dB. So, I can say S_v is equal to $20 \log E_0$ (Refer Time: 10:58), so that way sensitivity of the microphone is measure I can measure the sensitivity of the microphone.

Now, let one condition that I have taken a microphone in here and the data set the microphone sensitivity written is S_v . Now, instead of 94 of SPL, lets I measure this pen the sound pressure level is L_p . Now, if I expose this microphone in a L_p sound pressure level how much electrical voltage should it produces in the two end, understand. So, I said that at 1 Pascal sound pressure if it is S_v that means, 1 Pascal means 94 dB sound pressures. So, if it is L_p in dB, so if it is respect to 1 Pascal sound pressure effective L_p is L_p minus 94 dB, because at least 94 dB, it is S_v . So, at L_p it should be L_p minus 94 d b. So, output in dB sensitivity of the microphone at L_p is S_v minus 94 or in v plus L_p minus 94. This will be $20 \log E_0$, the output produces by the microphone $20 \log E_0$, I can say E_0 is nothing but 10 to the power S_v plus L_p minus 94 divided by 20 ok or not see that I am not going to slide.

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- The open-circuit voltage output of the microphone when exposed to some other acoustic level L_p is calculated from

$$E_0 = 10^{\left(\frac{S_v + L_p - 94}{20}\right)} \dots (2)$$

[$20 \log E_0 = S_v + L_p - 94$]

Example: If a given microphone tested under the condition shown in Fig. 1, produced an open circuit voltage $E_0 = 0.001$, then from equn. (1) we calculate

$$S_v = 20 \log (0.001) \text{ dB}$$

$$= - 60 \text{ dB}$$

Contd.

Or similarly, if I said if the microphone I do not know the sensitivity of the microphone I put the microphone in L_p sound pressure level what should be the sensitivity of the microphone. Then sin that case I know E_0 I know L_p , I have to calculate S_v in dB or

other way if I know the sensitivity I know sensitivity then I have to calculate E_0 I can calculate E_0 very easily.

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If this microphone is now exposed to an acoustic input level of 100 dB, rather than 94 dB then the open-circuit output voltage would be

$$E_0 = 10^{\frac{-60 + 100 - 94}{20}} = 0.002V$$

Another way of looking at it is to think that the new SPL is $100 - 94 = 6$ dB higher. Therefore the new E_0 will be + 6 dB higher or double the previous E_0

Contd.

Now, let us look at this problem. A microphone if a microphone is now exposed to an acoustic level of 100 dB rather than 94 dB then the output circuit open circuit voltage should be E_0 should be L_p is 100 dB.

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$S_v = -60$
 $L_p = 100 \text{ dB}$
 $E_0 = 10^{\frac{-60 + 100 - 94}{20}}$
 $E_0 = 10^{\frac{40 - 94}{20}} = 10^{\frac{-54}{20}} \approx 0.002V$

So, it is if it is microphone is minus 60 dB sensitivity S_v is minus 60 dB exposes the microphone in a L_p sound pressure level which is 100 dB. So, minus 60 plus 100 minus

94 divided by 20 10 to the power that is E_0 is nothing but 10 to the power how much will come minus 60, so 10 to the power 40 minus 94 divided by 20 that is 10 to the power minus 4 5 divided by 20 this is equivalent to 0.002 volt.

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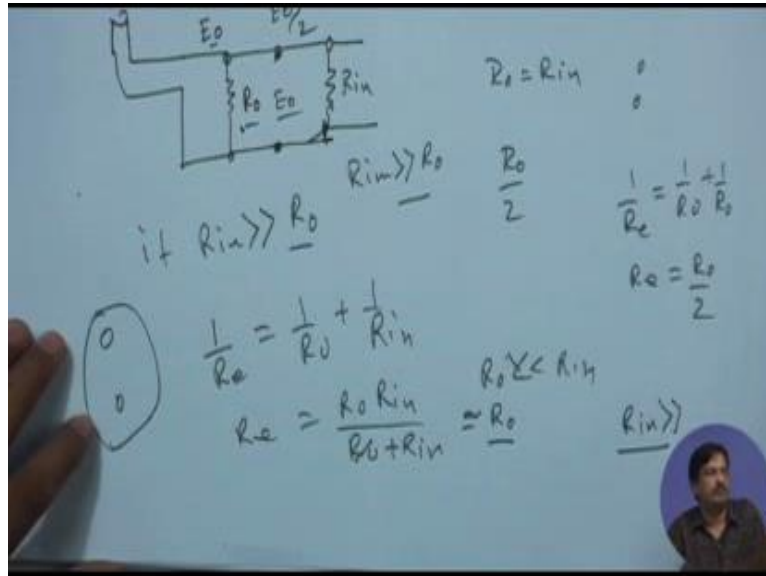
Now, we have to justify why we have take the sensitivity in open circuit voltage. We said that sensitivity is measured in term of open circuit voltage. Why I would justify why I take the open circuit voltage why not it is closed circuit when there microphone is connected to the amplifier that I would take the measure of the voltage.

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- Given E_0 (open-circuit voltage) and R_0 (resistive component of Z_0 , the output impedance) of a microphone, the voltage across the input terminals of the microphone preamplifier can be calculated if the R_{in} of the preamplifier is know.
- Usually R_0 is in the range of 150Ω to 250Ω and $R_{in} \geq 2k \Omega$. Therefore for all practical purpose E_0 is effectively the voltage at the input of the microphone preamplifier and the specified voltage represents the actual operating condition.
- If $R_{in} \geq 10 R_0$ then small variations in R_0 does not alter final voltages significantly.

So, why it is, now if you see if microphone I take I am not getting the slide, let us understand that things.

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Suppose this is a microphone and these are the two vertical terminal two electrical terminals. So, if the microphone is connected to like this is the preamplifier two terminal, if the microphone is connected to the preamplifier then what will happen there will be a output resistance of the microphone will be could acoustic parallel of the input. It is the R_{in} is the input resistance of the preamplifier R_0 is the resist compound of the microphone. If I say the R_0 , if I connect this microphone with the amplifier in this condition then if it is microphone is produces the E_0 voltage then once R_0 is equal to R_{in} , what will happen the effective resistance between two this terminal will come R_0 by 2. Same resistance in parallel it is reduces by half that is one equalize 1 by R_e is equal to 1 by R_0 plus 1 plus R_0 , it is nothing but R_e is nothing but R_0 by 2.

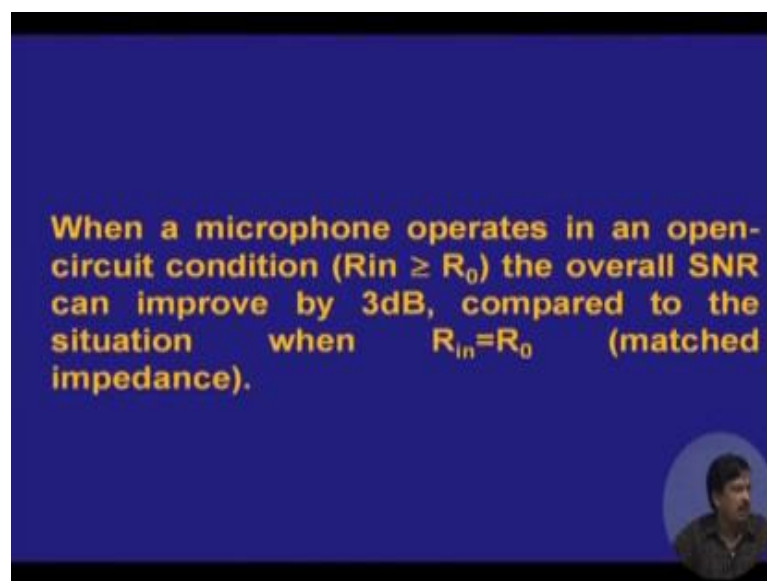
Once the resistance is dropped then the E_0 will be E_0 by 2. But if R_{in} is much, much greater than R_0 that means, that if R_{in} very high then 1 by R_e is nothing but 1 by R_0 plus 1 by R_{in} . So, R_e is nothing but a $R_0 R_{in}$ divided R_0 plus R_{in} . Now, if R_0 is much, much less than R_{in} than I can neglect this R_0 equivalently it will come to R_0 values. So, if it is R_0 then the acoustic this terminal the voltage will be E_0 in case of R_{in} is much, much greater than R_0 . So, I do not want when I measure the sensitivity once

I load it then the voltage is dropped. So, what I want I measure the voltage emission micro volt meter.

So, I want the input voltage input resistance of the micro volt meter should be sufficiently large, so that once I connect the micro volt meter that develop voltage should not be dropped. If R_{in} is sufficiently high what is meaning of that R_{in} sufficiently high that is nothing but open circuit voltage that means, as if there is no load acoustic two terminal of the microphone. So, load is only R_0 the output resistance of the R_0 . So, there is no extra load is added on that R_0 , so that is why we take them meter took them take the reading of the sensitivity at open coil or we can say data define the sensitivity in term of open circuit voltage.

Generally, if you see usually R_0 value for a microphone is 150 ohms to 250 ohms and we take R_{in} in which is 10 times greater than the R_0 . So, if it is 250 ohms, it will be 2.5 kilo ohms greater than 2.5 kilo ohms. So, it take 10 times if it is 10 times large then almost the voltage R_0 does not change if I connect to the preamplifier or micro volt meter that is why we say the sensitivity of the microphone has to be measure in term of open circuit condition. It is not practically, not open circuit, so when you measure the open circuit voltage the input impedance of the measure instrument should be very high.

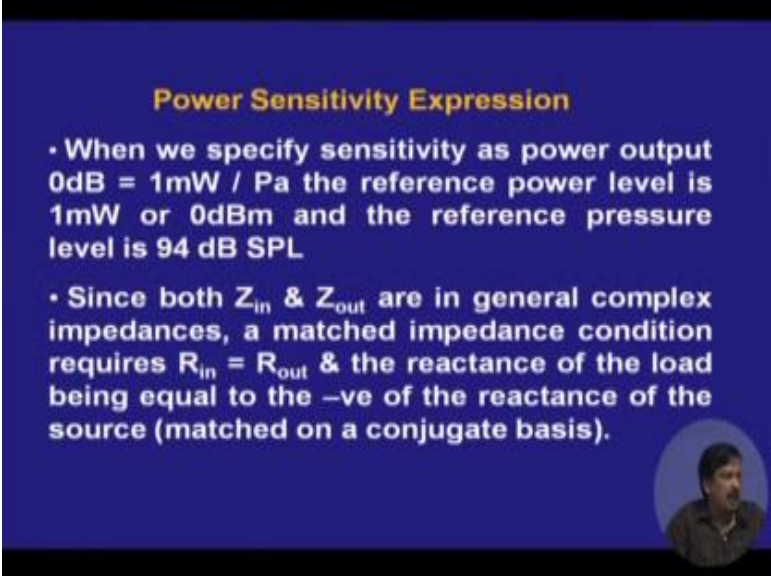
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Then there is another condition is come. While a microphone is operates in open circuit condition, the overall SNR can be improve by 3 dB compared to the situation when it is

connected in impedance matched condition that why I will ensure few slides ensure these issues.

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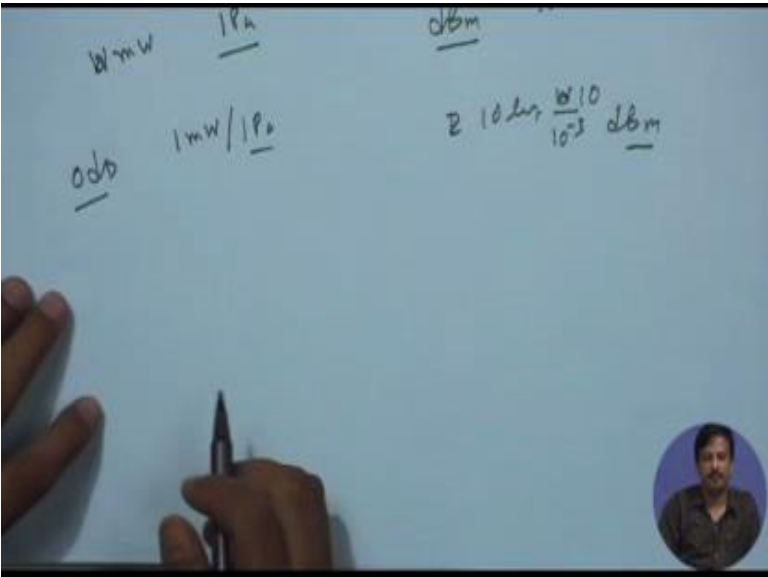


Power Sensitivity Expression

- When we specify sensitivity as power output $0\text{dB} = 1\text{mW} / \text{Pa}$ the reference power level is 1mW or 0dBm and the reference pressure level is 94 dB SPL
- Since both Z_{in} & Z_{out} are in general complex impedances, a matched impedance condition requires $R_{\text{in}} = R_{\text{out}}$ & the reactance of the load being equal to the $-ve$ of the reactance of the source (matched on a conjugate basis).

Another issues is there, bring the voltage sensitivity issue and there is a power sensitivity issue.

(Refer Slide Time: 19:58)



Handwritten notes on a whiteboard:

- 0dB
- $1\text{mW} / 1\text{Pa}$
- 0dBm
- 20dB
- $\frac{10}{10^3} \text{ dBm}$

What is the power sensitivity of the microphone? We define in the power sensitivity the power sensitivity of the microphone is power deliver by the microphone in milli watt

will compare in 1 Pascal pressure. So, what I say if I expose a microphone in 1 Pascal pressure, the amount of power deliver by the microphone in milli watt will be the power sensitivity of the microphone. So, it is 0 dB, it is not dB, if it is milli watt then it will go dBm power using dBm. So, we already discussed what is dBm, it is nothing but a 10 log power divided by 10 to the power minus 3 in power milli watt with respect to milli watt. If it is power expect to if it is microphone produces 10 watt then it is 10 watt divided by 10 to the power minus 3 that dBm. So, power using dBm ratio of the power using dB m, so 0 dB sensitivity of the power sensitivity 0 dB that means, 1 milli watt produced by 1 Pascal. Now, we will go for the watt part, how the microphone will deliver the power how the microphone will deliver the power.

(Refer Slide Time: 21:27)

Handwritten notes on a whiteboard:

$$E_0 = 20 \log Sv$$

$$E_0 = 10 \log \frac{Sv}{10^{-3}}$$

$$E_0^2 = 10 \log \frac{Sv^2}{10^{-6}}$$

$$AIP = \frac{E_0^2}{4 \cdot R_0} = \frac{10^5 Sv^2}{4 \cdot R_0}$$

$$\frac{AIP}{10^{-3}} = \frac{1}{10^{-3}} \cdot \frac{10^5 Sv^2}{4 \cdot R_0}$$

$$= \frac{10^3 \cdot 10^5 Sv^2}{4 \cdot R_0}$$

Labels: $L_{AIP} \Rightarrow dBm$, $L_{AIP} = 10 \log \left(\frac{AIP}{10^{-3}} \right)$

So, let us start with phase page, I have a microphone, and the two electrical terminals it is here and it is connected to a preamplifier, let using the preamplifier and would connected. So, output impedance of the microphone is R_0 and input impedance of the preamplifier is R_{in} . So, if E_0 is voltage sensitivity of the microphone, E_0 voltages is produces by the microphone then this E_0 will be loaded here. Now, if you see when R_0 is equal to R_{in} impedance match condition then E_0 will drop by half.

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- Let AIP = Available Input Power that a microphone with an output resistance R_0 can deliver across the input of the preamplifier.


$\therefore E_0$ = Open circuit voltage of the microphone

$$AIP = \frac{E_0}{2} \times \frac{E_0}{2R_0} = \frac{E_0^2}{4R_0} \dots\dots (3)$$

$S_v = 20 \log E_0$

$$\text{or } (E_0)^2 = 10^{\frac{S_v}{20} \times 2} = 10^{\frac{S_v}{10}} \dots\dots (4)$$

Substituting (4) in (3)

$$AIP = \left(\frac{1}{4}\right) \left(10^{\frac{S_v}{10}}\right) \left(\frac{1}{R_0}\right) \dots\dots (5)$$


So, power sensitivity is defined by AIP - available input power AIP. When I expressed in dB we said L AIP available input power level, L means level; once it is level then AIP express in dBm - available input power level, AIP is defined as in dBm. So, if this is the condition when R_0 is equal to R in how much power will deliver by microphone to the amplifier to the pre amplifier. So, E_0 is open circuit voltage. So, once it is R_0 is equal to R in then E_0 will be drop by half, voltage acoustic this two terminal is E_0 by half. So, available input power if I say AIP not level, I said available input power, if it is level then it will be dBm. Available input power is E_0 by two voltage into power is nothing, but V into I what is $I E_0$ by 2 into 1 by half R_0 V into I d by R is the I . So, it is nothing but a E_0 square by $4 R_0$.

Now, what is E_0 s v if the voltage is S_v then $20 \log E_0$ is s v. So, if it $20 \log E_0$ s v then E_0 is nothing but a 10 to the power S_v divided by 20. So, what is E_0 square is nothing but 10 to the power S_v by 10 is 20 to 10. So, I can write it is nothing but a 10 to the power S_v by 10 divided by $4 R_0$. Now if I take available input power is 10 to the power S_v by 10 divided by $4 R_0$, if it is microphone is connected in impedance match condition.

Now, the L AIP when I said that L level of available input power or power sensitivity of to determine the power sensitivity of the microphone or L IP what I would take I would take milli watt because I said dBm is nothing but watt divided by 10 to the power minus

3. So, I have to divided AIP by 10 to the power minus 3 is equal to 1 by 10 to the power minus 3 into 10 to the power S v by 10 divided by 4 R 0. So, it is nothing but a 10 to the power 3 by 4 into 10 into S v by 10 into 1 by R 0. So, what is L AIP level is nothing but a 10 log power divided by 10 to the power minus 3. So, this I have known this part I have known 10 by this part I have known. I would then multiply log and 10. So, if I say take the logging of both side of this equation what will come.

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$$\begin{aligned}
 LAIP &= 10 \log \frac{AIP}{10^{-3}} = \log 10^3 + \log \frac{1}{4} + \log 10^{\frac{Sv}{10}} + \log \frac{1}{R_0} \\
 &= 10 \left[3 - 0.6 + \frac{Sv}{10} - \log R_0 \right] \\
 &= 30 - 6 + Sv - 10 \log R_0 \text{ dBm} \\
 &= 24 + Sv - 10 \log R_0 \text{ dBm} \\
 R_0 &= 200 \Omega \\
 Sv &= -60 \text{ dB} \\
 LAIP &= 24 - 60 - 10 \log 200 \text{ dB} \\
 &= 24 - 60 - 23 \text{ dB} \\
 &= -59 \text{ dB}
 \end{aligned}$$

Take the logging both side of this equation. So, log of AIP divided by 10 to the power minus 3 is equal to log of 10 to the power 3 plus log of 1 by 4 minus 4 sorry plus log of 1 by 4 plus log of 10 to the power S v by 10 plus log of 1 by R 0. So, I can write log of 10 to the power 3 is 3 plus log of 1 by 4 is nothing but a minus 0.6 plus is nothing but a S v by 10 and it is nothing but a minus log of R 0. Now if I multiply by 10 both side then I get L AIP available input power L AIP. So, L AIP is equal to 10 log of AIP divided by 10 to the power minus 3 in dBm. So, it is nothing but a 30 minus 6 plus S v minus 10 log R 0 dBm. So, it is nothing but a 24 plus S v minus 10 log R 0 dBm.

Now, if I say the res output R 0 of the microphone is 200 ohms and S v of the microphone is minus 60 dB then what should be the L AIP. So, L AIP is nothing but a 24 minus 60 minus 10 log 200 dB m. So, it is nothing but if I said what is the value often log 200 this nothing but 23. So, it is 24 minus 60 minus 23 dBm. So, it is nothing, but a minus 59dB. So, L AIP you can calculate it.

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$$= S_v - 10 \log R_0 + 24 \dots\dots (10)$$

For example a microphone has $R_0 = 200 \Omega$ & $S_v = -60 \text{ dB}$

Then $L_{AIP} = (-60 - 10 \log 200 + 24) \text{ dBm}$

$= (-60 - 23 + 24) \text{ dB m}$

$= -59 \text{ dB m/Pa}$

1.6 EIA Sensitivity Expression

The power sensitivity of a microphone may be referenced to 0dB SPL ($20 \mu \text{ Pa}$, threshold of hearing), instead of 94 dB (1 Pa). Since the SPL is lower by 94 dB, the L_{AIP} of equn (10) will be lower by 94dBm.

If we denote this power sensitivity as G_{AIP}

Similarly, if I say GAIP EIA is the specification of power sensitivity in G AIP is written as G AIP. What is the G AIP, G AIP is nothing but a power sensitivity with respect to SPL, sound pressure level references sound pressure level, which is nothing but a just respect 20 micro Pascal.

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$G_{AIP} \rightarrow \text{SPL } 20 \mu \text{ Pa} \quad 0 \text{ dB}$

$G_{AIP} = L_{AIP} - 94$

$= 24 + S_v - 10 \log R_0 - 94$

$= S_v - 70 - 10 \log R_0$

100 SPL (GAIP)

GAIP

So, instead of 1 Pascal, if I said 20 micro Pascal then the 94 dB is the difference. So, I can write G AIP is nothing but L AIP minus 94 dB. So, if I know L AIP. So, what is L AIP is 24 plus S v minus 10 log R 0 minus 94. So, this is nothing but a S v minus 70

minus $10 \log R_0$. So, why I express in G_{AIP} because if I express it since the SPL is lower by 94 dB the L_{AIP} equation 10 will become lower by 94 dB. And we denote power sensitivity G_{AIP} because when you measured microphone if you know the microphone g_{AIP} in some SPL lets SPL the G_{AIP} in L 1 SPL will be just suspect the difference of the power pressure level.

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For a microphone with $S_v = -60$ dB, $R_0 = 200\Omega$


$$G_{AIP} = L_{AIP} - 94 = S_v - 10 \log R_0 + 24 - 94 = S_v - 10 \log R_0 - 70$$

$$= (-60 - 23 - 70) \text{ dBm}$$

$$= -159 \text{ dBm. at the threshold of hearing.}$$

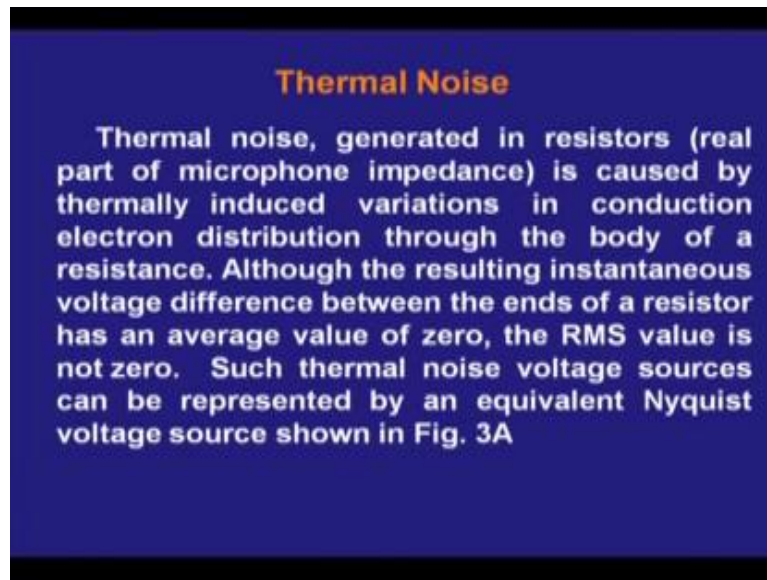
The advantage of this form of specification is that the power level supplied by a given microphone is obtained by simply adding the G_{AIP} to the SPL at the microphones position. (as it is referenced to 0dB SPL).

In the EIA rating system R_0 is replaced by R_{MR} , where R_{MR} is the EIA centre value of the nominal impedance r_n shown below.



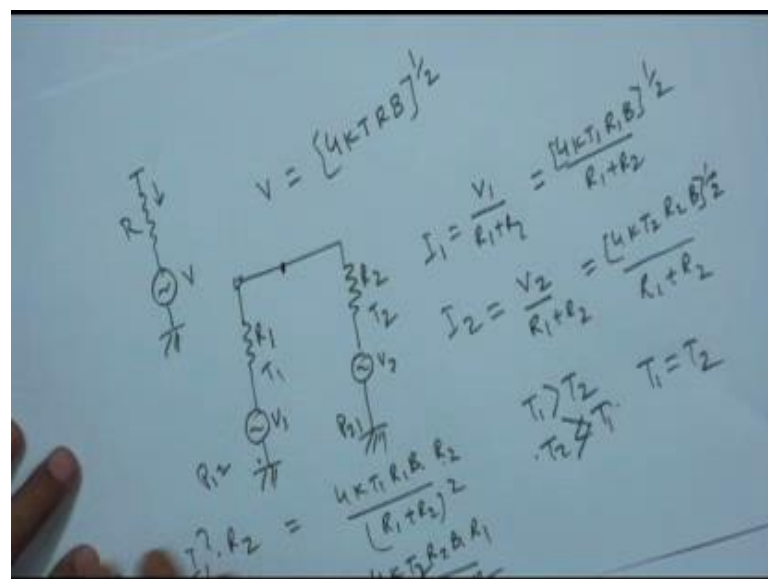
Suppose in 100 dB SPL if G_{AIP} is given or G_{AIP} given if the microphone G_{AIP} know what should the G_{AIP} 100 dB SPL I would just simply subtract that difference. So, it is 94 dB. So, it is 100 dB that is why all are expressed the power sensitivity in G_{AIP} .

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Now, I come to the next condition while the microphone is connected then if the microphone why that is the questions that is the question which I have raised here. When a microphone operate in an open circuit condition the overall SNR can be improved by 3 dB compared to the situation when R_{in} and R_0 . Now, if a microphone connected to a preamplifier, there will be a thermal noise. Any microphone if it is connected to the preamplifier there will be a thermal noise. What is thermal noise?

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Since, the microphone if it is resistance suppose I have a resistance if I flow a current to the resistance then a thermal noise will be produces. Average value of the thermal noise cross the resistance may be 0, but the RMS value is not 0.

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$V = (4KTRB)^{1/2} \dots\dots (1)$
 Where V = RMS value of the noise voltage
 K = Boltzmanns constant = 1.38×10^{-23} J/K
 T = Absolute temp (K)
 R = Resistance in Ω
 B = is the observation bandwidth in Hz

Fig 3 B depicts a situation when two Resistors are connected in parallel as would be case when a microphone is connected to the input of a preamplifier.

Contd.

So, thermal noise of the resistance can be expressed resistance through and Nyquist voltage source let V , and resistance is R . Then the expression of the thermal noise V is nothing but $4 K T R B$ to the power half, this is the formula. What is K ? K is the Boltzmann's constant. What is T ? Temperature in Kelvin; what is R ? R is the resistance, What is b is the bandwidth. If you see this slide, V is the RMS value of the noise voltage, Boltzmann's constant, absolute temperature resistance, b is the bandwidth. So, the signal bandwidth is also effect on the how much voltage will be produces.

Now consider the case of the microphone. So, a microphone let us microphone has R_1 output resistance and Nyquist voltage source V_1 of the thermal noise. Similarly, input resistance of the pre amplifier has R_2 and has a Nyquist voltage source V_2 for the thermal noise this is the condition. So, the thermal noise contributing to the amplifier if V_2 is not present lets v_2 is not present then the thermal noise the current flowing to the circuits it is nothing but a V_1 divided by R_1 plus R_2 when the V_2 is sorted.

Similarly, if I say this is I_1 current flowing. What is I_2 is nothing but a V_2 by R_1 plus R_2 . What is V_1 if it if temperature of this resistance T_1 and temperature of this resistance T_2 then V_1 is nothing but a $4 T_1 R_1 b$ divided by R_1 plus R_2 root over?

What is $V_{2,4} k T_2 R_2 B$ same bandwidth root over of half by $R_1 + R_2$. Now how many power suppose this source is not there. So, it is power P_1 and P_2 , noise for deliver from the microphone to pre amplifier there is P_1 and P_2 , noise power deliver by the preamplifier to the microphone is $P_{2,1}$.

So, what is $P_{1,2} I_1^2$ into R_2 , the current I_1 current will flowing through R_2 and that noise will be that that power will be deliver. So, it is nothing but I_1^2 into R_2 . So, what is the I_1^2 is nothing but a $4 k T_1 R_1 B$ into R_2 divided by $R_1 + R_2$ whole square. What is $P_{2,1}$ is nothing but a I_2^2 by R_1 , I_2^2 into R_1 . So, I_2 , what is I_2^2 $4 k T_2 R_2 B$ into R_1 divided by $R_1 + R_2$ whole square.

Now, if you see what is the difference between the two expressions; only differ by T_1 and T_2 . So, this is T_2, T_1 by T_2 . If T_1 is greater than T_2 then the power will be transformed for T_1 to T_2 . If it is T_2 is greater than T_1 then the power will be transformed for T_1, T_1 to sorry T_2 is greater than T_1 then the power will be transformed for T_2 to T_1 . Now, at the equilibrium condition will be happen when T_1 is equal to T_2 . Now I have to calculate what is the effective noise voltage acting in here. effective noise voltage is acting in here across this terminal effective noise voltage how do we calculate. The noise voltage across the power terminal can be calculated by super position of V_1 and V_2 super position.

(Refer Slide Time: 36:13)

The source with a lower T receives power from the other source. When $T_1 = T_2$ $P_{12} = P_{21}$ and equilibrium is established.

The noise voltage across the common terminals can be calculated by superposition. Voltage when both the source act simultaneously is obtain by appropriate combination. In this case it is quadratic sum rather linear sum as the two generator have completely random phase.

The appropriate voltage = V'

$$V' = \left[\left(\frac{V_1 R_2}{R_1 + R_2} \right)^2 + \left(\frac{V_2 R_1}{R_1 + R_2} \right)^2 \right]^{1/2} \dots (6)$$

$$= \left[\frac{4kBR_1 R_2 (T_1 R_2 + T_2 R_1)}{(R_1 + R_2)^2} \right]^{1/2} \dots (7)$$

So, voltage when both the source acts simultaneously. So, how do you get the super position first let V 2 is not there, I calculate the voltage, V 1 is not there I calculate the voltage then do the super position, but both the source simultaneously is on, then how do you obtain by appropriate combination. So, in this case, it should be quadratic sum rather than the linear sum, because I do not know the completely the generated source or completely in random space two source completely random space. So, I do not know whether it will be a linear super position. So, instead of take linear super position the effective voltage I can get by the quadratic super position. So, square of the voltage will be added up.

(Refer Slide Time: 37:29)

The image shows a handwritten derivation on a whiteboard. It starts with the equation for the total voltage V as the square root of the sum of squares of individual voltages: $V = \sqrt{(I_1 R_2)^2 + (I_2 R_1)^2}$. This is then expressed in terms of source voltages V_1 and V_2 as $V = \sqrt{\frac{V_1^2 R_2^2}{(R_1 + R_2)^2} + \frac{V_2^2 R_1^2}{(R_1 + R_2)^2}}$. The individual voltages are given as $V_1 = \sqrt{4kT_1 R_1 B}$ and $V_2 = \sqrt{4kT_2 R_2 B}$. Substituting these into the total voltage equation and simplifying, it leads to $V = \sqrt{\frac{4kT_1 R_1 R_2^2}{(R_1 + R_2)^2} + \frac{4kT_2 R_2 R_1^2}{(R_1 + R_2)^2}}$. A note $T_1 = T_2 = T$ is written. The final simplified result is $V = \sqrt{\frac{4kBR_1R_2T}{R_1 + R_2}}$.

So, quadratic super position of v will be the square of the voltage added up. So, it is nothing but a I_1 current while across the R_2 . So, $I_1 R_2$ is the voltage square plus I_2 current while across the R_1 whole square then take the root over quadratic voltage sum. So, what is I_1 is nothing but $V_1 R_2$ divided by R_1 plus R_2 V_1 square R_2 square divided by R_1 plus R_2 whole square. This is nothing but V_2 by $R_1 R_2$; this is V_2 square R_1 square R_1 plus R_2 whole square. So, what is V_1 v one is nothing but root over of $4kT_1 R_1 B$, and V_2 is nothing, but a root over of $4kT_2 R_2 B$.

So, I can put valid value then what will cut root over of V_1 is $4kT_1 R_1 B$ into R_2 square divided by R_1 plus R_2 whole square plus $4kT_2 R_2 B$ divided by R_1 by R_2 whole square into R_1 square. So, now, if I take it will be if I simplify it, it will be root

over of $4 k B R_1 R_2$ into T divided by $R_1 + R_2$ whole square. Now, if this is the case then if T_1 and T_2 is equal and equal to t then I can say this reduces to $4 k B R_1 R_2 T$ divided by $R_1 + R_2$ root to $R_1 + R_2$ root, OK or not.

(Refer Slide Time: 40:09)

Handwritten mathematical derivations on a blue background:

$$V = \sqrt{\frac{4kBR_1R_2T}{R_1+R_2}}$$

$$V' = \sqrt{4kBR_1T}$$

Annotations and further derivations:

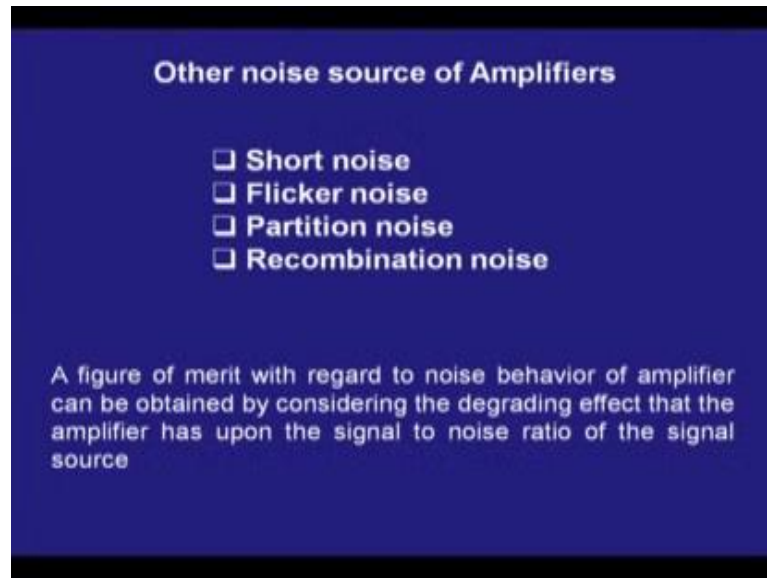
- $R_2 > R_1$
- $R_1 = R_2$
- $V = \sqrt{\frac{4kBR_1R_1T}{2R_1}}$
- $= \frac{1}{\sqrt{2}} V'$
- $\frac{E_0}{2} \Rightarrow 6dB$
- $3dB$ (circled)

So, now I put the condition. Now, let the both the things or happen as the same temperature. Now, so voltage in that case the V is equal to root over of $4 k B R_1 R_2 T$ divided by $R_1 + R_2$. If R_2 is much, much greater than R_1 what the meaning the input impedance of the preamplifier is much, much greater than output impedance of the microphone, then v will be R_2 much, much greater than R_1 . So, I can this R_1 can be cancel. So, it is root over of $4 k B R_1$ into T . Now, if R_1 is equal to R_2 R_1 is equal to R_2 then v will be root over of $4 k B R_1 R_1$ into T divided by $2 R_1$. So, R_1, R_1 is cancel. So, it is nothing, but a 1 by root 2 into if it is V dash, 1 by root 2 into V dash.

So, if the impedance matches condition if it is impedance match condition then thermal noise voltage is reduces by 3 dB. At the same time, if it is impedance match condition then available input power is E_0 is by half. so it will be reduces by how much 6 dB. So, overall SNR come if the impedance match condition then I get 3 dB less thermal noise, but I lose 6 dB due to the impedance match available input power. So, ultimately gain 3 dB is here if it is not impedance if R_1 is greater than R_2 , I get 3 dB more noise power, but at least 6 dB down will be not there. So, I can say that in case of this case, so I can this statement I can said is true by the microphone operated in an open circuit condition,

now overall SNR can be improved by 3 dB compare to impedance match condition it is proved.

(Refer Slide Time: 42:42)



Now, suppose there is another situation you will heard over that when the microphone is connected to amplifier will consent about that all over the noise figure means microphone connected to the amplifier and output of the amplifier it produces noise that system call overall noise figure. So, I would calculate the overall noise figure. Instead of thermal noise there is another noise also short noise, flicker noise, partition noise all kinds of noise that may be a (Refer Time: 43:12) line this terminal noise all kind of noise will be there.

(Refer Slide Time: 43:18)

Source Signal to noise ratio (thermal noise)

$$SNR_s = \frac{V_s}{4kTR_s B} \quad R_m \gg R_s$$

$$SNR_A = \frac{V_o^2}{V_n^2}$$

$$V_o^2 = A^2 V_s^2$$

$$V_n^2 = 4kTR_s B + V_{nd}^2$$

$$SNR_A = \frac{V_o^2}{V_n^2} = \frac{A^2 V_s^2}{4kTR_s B + V_{nd}^2}$$

V_{nd}^2 is the mean square noise voltage at the amplifier output contributed by the amplifier

$$F = \frac{SNR_s}{SNR_A}$$

Now, let consider only thermal noise then, what is SNR S, what you mean by SNR S, SNR of the source.

(Refer Slide Time: 43:24)

Handwritten derivations on a whiteboard:

$$V_s = \frac{V_s}{4kTR_s B}$$

$$SNR_A = \frac{V_o^2}{V_n^2}$$

$$SNR_A = \frac{V_o^2}{V_n^2} = \frac{A^2 V_s^2}{4kTR_s B + V_{nd}^2}$$

$$F = \frac{SNR_s}{SNR_A}$$

$$NF = 10 \log F$$

$$= 10 \log \frac{SNR_s}{SNR_A}$$

$$= 10 \log SNR_s - 10 \log SNR_A$$

V_s is the source sensitivity of the source V_s and divided by the thermal noise $4kTR_s$ into B . T is the Kelvin temperature; R_s is the resistance of the microphone; B is the bandwidth of the microphone, this is the SNR_s . Now, in case of R_m is greater than R_s . Now what is SNR_A is nothing but V_o input power to power to amplifier output of the amplifiers whatever the input for. So, V_o square divided by V_n square. What is V_o

V_{os} is nothing but A^2 times signal square. So, if the gain of the amplifier is s then the output of the amplifier will be divided by the gain.

So, the power is nothing, but the square SNR, if it is power then it will be voltage square. So, square voltage square O_s square by V_1 square. What is V_{o1} square the total output power is nothing but this is output power for the signal output for the signal noise $4kTB$ $R_s B$, which is the thermal noise power plus $V_n A$ power, which is the noise for the amplifier noise produces by the amplifier. So, SNR_A is nothing but V_{os} square by V_{on} square is nothing but $A^2 v_s^2$ square divided by $4kTB R_s B$ plus $V_n A$ square. $V_n A$ is the mean square noise voltage at the amplifier output contributed by the amplifier. Now, what is the figure of merit f is called SNR_S by SNR_A .

(Refer Slide Time: 45:44)

The slide contains the following mathematical expressions:

$$V_{nd}^2 = A^2 V_{in}^2$$

$$V_{in}^2 = 4kTR_s B$$

$$F = \frac{A^2 4kTR_s B + A^2 4kTR_n B}{A^2 4kTR_s B} = \frac{R_s + R_n}{R_s}$$

Noise Figure of the amplifier

$$NF = 10 \log F = 10 \log \frac{SNR_s}{SNR_A} = 10 \log SNR_s - 10 \log SNR_A$$

So, I can write F is nothing but I know then $V_n A$ is nothing, but this one the minimum and I know that B minimum this one. So, I can write this expression like this way. So, noise figure of the amplifier is in all over the said the noise figure said the noise figure of the NF is nothing, but a $10 \log$ noise figure of the amplifier. So, what is the $10 \log f$ $10 \log SNR_S$ divided by SNR_A ? So, it is nothing but a $10 \log SNR_S$ minus $10 \log SNR_A$ or $10 \log SNR_S$ is nothing but a $10 \log SNR_S$ plus noise figure or $s n r a$ is nothing, but a $10 \log SNR_S$ minus NF . So, if I know the noise SNR_S microphone SNR microphone SNR if I know and if I know the noise figure I can calculate the amplifier SNR . . So, you can solve this problem.

(Refer Slide Time: 46:58)

Microphone specification and amplifier specification as in given below

Microphone specification	amplifier specification
$S_v = -60 \text{ dB}$	<i>Frequency respons</i>
$G_{AV} = -153 \text{ dB}$	20 Hz – 20 KHz
$R_0 = 200 \Omega$	NF = 5 dB
	$R_y = 200 \Omega$

If a talker produce 80dB near the microphone find out the signal to noise ratio at amplifier out put at 20° C

Let us I have problem, I have given a microphone and given an amplifier, amplifier specification. If talkers produce 80 dB near the microphone find out the signal to noise ratio at amplifier output 20 degree centigrade in dB, output at 20 degree centigrade in dB. So, use this equation and find out the amplifier output.

Thank you.