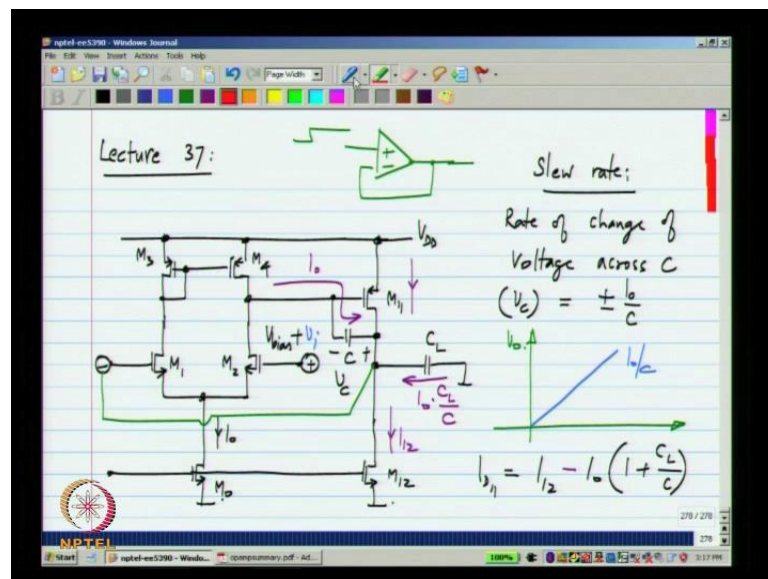


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**Lecture - 37**  
**Two Stage Opamp; Three Stage and Triple Cascade Opamps**

Hello and welcome to lecture 37 of analog integrated circuit design. We were discussing the 2 stage opamp. We have calculated the spot signal parameters, offset and noise. We also saw that offset was contributed by a mismatch between transistors in the first stage as well as the biasing condition of the second stage. If we make the current density in the second stage transistors equal to the current density in the load transistor for the first stage, the systematic offset can be avoided. Now, we will calculate the slew rate and signal ranges. That is input common mode range and output signals range of the 2 stage opamp.

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This is the second stage opamp, positive input, negative input and the output and this is integrated capacitor C. Now, we have to assume that there is some load here and the load will be connected between the output and ground. If it is the capacitor load; if it is a resistor load we will see later what to do with it. We will assume that there is only a capacitor load for now. That is why the tile current of the input stage is I naught.

The slew rate as usual is limited by the amount of current flowing into some capacitor which limits the rate of change of voltages inside the opamp. As before, if we test the Opamp, the unity gain configuration that is; I make this circuit and apply a step and look at maximum rate of change of the output voltage.

The input is  $V_{bias}$  plus some step  $V_i$ . Now, we know that for larger and larger values of  $V_i$  the incremental current in  $M_2$  is larger and larger for very small values of  $V_i$ . The total current here will be  $I_{naught}$  by 2 plus  $G_{m1}$  times  $V_i$ . As  $V_i$  increases the current in  $M_2$  is larger and larger, but the increment cannot go beyond  $I_{naught}$  by 2. That is the total current in  $M_2$  can only be  $I_{naught}$ . At that point 0 current will be flowing through  $M_1$  and all of that  $I_{naught}$  will flow from the integrated capacitor  $C$ . That will be equal to  $I_{naught}$  for large values of positive  $V_i$ .

Now, similarly for large values of negative  $V_i$ , that is large in negative. All of the current will flow through  $M_1$  and nothing will flow through  $M_2$  and there is a current  $I_{naught}$  that can go in that direction. So, what is the rate of change of the output voltage? First of all, rate of change of voltage across  $C$ , this voltage  $V_c$  that is equal to plus or minus  $I_{naught}$  by  $C$  assuming that the current  $I_{naught}$  will flow through the capacitor.

Now, what will be the output voltage? Remember, if you recall the representation of the 2 stage opamp at the level of transconductors, this is what we have.  $G_{m2}$ ,  $G_{m1}$ ,  $C$  and  $C_1$ . Now, the second stage will be the current controlled voltage source and it becomes a current controlled voltage source because the voltage at the negative input of  $G_{m2}$  is very small. If  $G_{m2}$  becomes very large, if the second stage has an ideal opamp, this voltage will be at 0. So, this voltage is approximately 0.

So,  $V_c$  is simply the output voltage itself.  $V_c$  equals  $V_{naught}$ . So, this is not simply the slew rate across the capacitor, but it is also the slew rate of the output. So, it looks like the slew rate is similar to what we were get in a single stage opamp, but we have to consider other things here. Let us say that  $V_{naught}$  which is  $V_c$  is changing at some rate.

$V_{naught}$  is changing at a rate of  $I_{naught}$  by  $C$ . What does it mean? It means that the voltage across  $C_1$  which is  $V_{naught}$  is also changing at this rate. So, the current to  $C_1$  is the slope of this voltage, times the capacitance. So, the current through  $C_1$  would be  $C_1$  times  $I_{naught}$  by  $C$ . Similarly, if the output voltage was reducing, if the output voltage

was growing, something like that, with the slope of the minus  $I_{\text{naught}}$  by  $C$ , there would be current in the other direction. Now, also of value  $C I$  times  $I_{\text{naught}}$  by  $C$ .

Now, let us examine these 2 cases separately. First, let me take the first case where current  $I_{\text{naught}}$  is drawn in this way. So, that means that the output is ramping up at positive  $I_{\text{naught}}$  by  $C$  and that means, that current of  $I_{\text{naught}}$  times  $C I$  by  $C$  is flowing through the load capacitor. What does it mean? It means through  $M_{11}$ , we need to have current equal to the current in  $M_{12}$  which is some bias current  $I_{12}$ , plus the current through  $C$ , plus the current through  $C I$  ok?

So, this is  $I_{12}$  plus  $I_{\text{naught}}$  times  $1$  plus  $C I$  by  $C$ .  $I_{d11}$  will be  $I_{12}$  plus  $I_{\text{naught}}$  of  $1$  plus  $C I$  by  $C$ . Is it possible to have this value? Yeah, because in quiescent condition the voltage here would be such that the current through  $M_1$  equals  $I_{12}$ . Now as  $V_i$  increases, this voltage reduces slightly and that the increases current in this. Now, total current is limited here by how far the voltage can go, but we will assume that it is not limited. So, the current in  $M_{11}$  can increase in positive direction ok?

So, in this direction, current in  $M_{11}$  can increase while it is  $I_{12}$  it can easily become this value by lowering of the gate voltage. Now, this may be a little confusing. Earlier while calculating output voltage, I assumed that the voltage at the gate of the  $M_{11}$  is hardly changing. So, this is just approximate calculation for current in  $M_{11}$  to increase.

The voltage here has to decrease, but just to be able to calculate output voltage we assume that this is fixed for calculating that output voltage. Now, while lowering the gate voltage of the  $M_{11}$  the current in  $m_{11}$  will increase. So, it is indeed possible to have this current in  $M_{11}$ . Let us see what happens in the other direction. That is why, that is  $I_{\text{naught}}$  and that is  $I_{\text{naught}}$   $C I$  by  $C$ .

And this is some  $I_{12}$ . So, the current through  $M_{11}$  will be  $I_{12}$  minus  $I_{\text{naught}}$  times  $1$  plus  $C I$  by  $C$ . Now, is it possible for this to attain any value? Clearly not. In the quiescent condition  $I_{12}$  is flowing through  $M_{11}$  and when we reduce  $V_i$ ,  $I_{\text{naught}}$  flows this way.  $I_{\text{naught}}$  flows that way and the output voltage will reduce, then the current in  $M_1$  will reduce. Now the smallest that the current in  $M_{11}$  can be is 0. The current in  $M_{11}$  will reduce and the smallest value of the current in  $M_{11}$  is 0.

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$$I_{D11} = I_{12} - I_0 \left(1 + \frac{C_L}{C}\right) > 0$$

If  $I_{12} > I_0 \left(1 + \frac{C_L}{C}\right)$ ; output will reduce @  $\frac{I_0}{C}$

$I_{12} < I_0 \left(1 + \frac{C_L}{C}\right)$ ?

output slew rate =  $\frac{I_{12}}{C_L + C}$  } Total current in C &  $C_L = I_{12}$

So, what does it mean?  $I_{D11}$  which is  $I_{12}$  minus  $I_0$  plus  $C_L$  by  $C$  must be greater than 0. Now, if this is the case, if  $I_{12}$  is greater than  $I_0$  times  $1 + \frac{C_L}{C}$ , the output will reduce at the rate of  $I_0$  by  $C$ , but what happens if  $I_{12}$  is less than  $I_0$  times  $1 + \frac{C_L}{C}$ . What happens in that case is that as we apply a negative step to  $V_I$  and make the size of the step larger and larger, more and more current will flow into the integrated capacitor ok?

Now, before all of a current  $I_0$  can flow through this, transistor  $M_{11}$  will cut off because  $I_{12}$  minus the current in this, minus the current in  $C_L$  will become 0. The current in  $C_L$  will always be the current in  $C$  times  $C_L$  by  $C$ , because the output is changing at the same rate. The voltage across the 2 capacitors are changing at the same rate. So,  $M_{11}$  will cut off before the input differential pair can switch completely.

So, in that case the output slew rate will be  $I_{12}$  divided by  $C_L + C$ . This is because the total current in  $C$  and  $C_L$  must be equal to  $I_{12}$  when  $M_{11}$  cuts off. When this cuts off, some current is flowing there and some current is flowing there and the sum of 2 equals  $I_{12}$ . If that happens, then the change of output will be  $I_{12}$  divided by  $C_L + C$ .

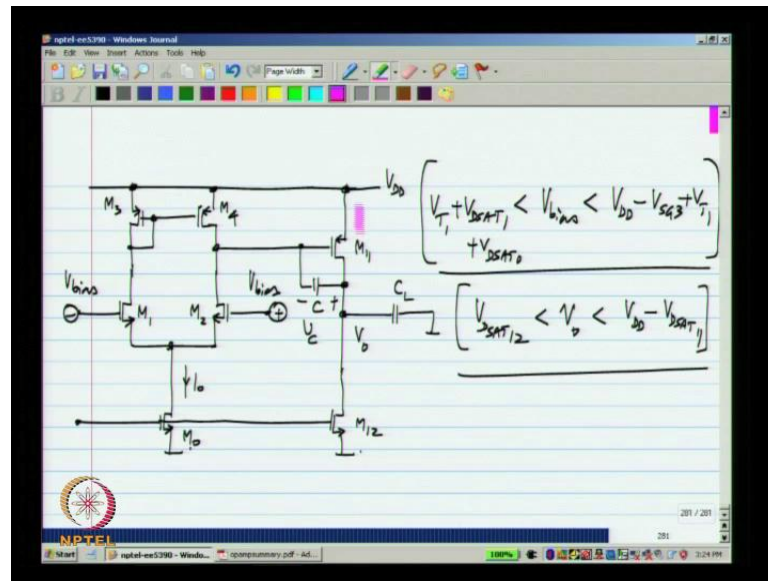
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The image shows a screenshot of a digital whiteboard with handwritten mathematical formulas. The first formula is  $SR_+ = \frac{I_0}{C}$ . The second formula is  $SR_- = \min \left[ \frac{I_0}{C}, \frac{I_{12}}{C_L + C} \right]$ . The whiteboard interface includes a toolbar with drawing tools and a taskbar at the bottom with a Windows logo and the text 'NPTEL'.

So, in 2 stage Opamp, the positive slew rate is limited by  $I_0$  and  $C$  and the negative slew rate is whichever is smaller of  $I_0$  and  $C$  and  $I_{12}$  divided by  $C_L$  plus  $C$ . So, there are 2 mechanisms of slewing. Either the input differential pair can cut off, in which case maximum current out of first stage will be equal to  $I_0$ . Alternatively, the second stage can cut off, in which case the maximum current through  $C$  plus  $C_L$  would be  $I_{12}$ . Which of this is limited depends the value of  $I_{12}$  and  $I_0$ . So, it is possible for the negative slew rate to be either  $I_0$  and  $C$  or  $I_{12}$  by  $C_L$  plus  $C$ . So, this is come out for some sort of simple calculation.

This is actually an approximate calculation because we assume that at the input of the second stage we have 0 volts, but this is good upon practical purpose, this also means that if the current in the second stage is very small, then that will be the end of the rather small slew rate in 1 direction.

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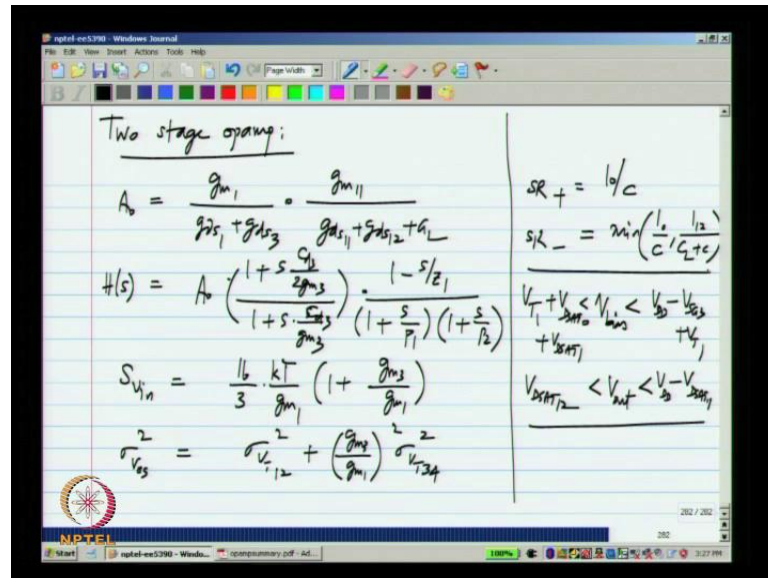
And it is also possible for slew rate to be different in positive and negative direction. So, the next thing is the single swings. Last time, we have determined, here is the single swing limits. Let me remove this feedback loop. Now, what are the limits on the input bias voltage  $V_{bias}$ ? We have evaluated this many times. If the input voltage  $V_{bias}$  increases, the input transistors  $M_1$  and  $M_2$  can go into triode region and if the input  $V_{bias}$  reduces the tail current transistors  $M_{naught}$  can go into the triode region ok?

So, the limits are exactly the same as before. The maximum value would be the drain voltage of  $M_1$  plus 1. Threshold voltage and the minimum value would be the old drive voltage that is required across  $M_{naught}$  to keep it in saturation region plus the voltage of  $M_1$ . That will be  $V_{T1} + V_{DC} + V_{DSAT_{naught}}$ . We can see that it is very close to  $V_{DD}$  at somewhat far away from the ground and what is the limit of the output as the  $V_{naught}$  increases? There comes a point where across  $M_{11}$ , very small falling into the saturation region. So,  $V_{naught}$  has to be less than  $V_{DD} - V_{DSAT_{11}}$ . Similarly, as  $V_{naught}$  increases the voltage across  $M_{12}$  becomes smaller and smaller and at some point it will go into triode region.

That will be  $V_{DSAT_{12}}$ . So, you can see that this kind of output structure, where we have a single transistor connecting to the supply voltage and a single transistor in to ground will give you the maximum possible swing limit. It can go within  $V_{DSAT}$  of the upper rail and within the  $V_{DSAT}$  of a lower rail which is ground. In general this the maximum swing

that is possible. In integrated circuit, this is the maximum possible swing a transistor circuit. Now, there are some specials where the voltage can go above supply rail or below the lower supply rail. We will not consider that. In general, we have to leave at least one  $V_d$  sat loop on the top and the bottom.

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So, to summarize, the 2 stage opamp has a DC gain which is the product of the first stage and the second stage gain and the important thing is that even if you have a resistive load  $G_L$  with a very high conductance, it affects only the second part of this ground. The first one can remain very large. So, that is how we will be able to operate the opamp resistive loads in the frequency response, can be return as  $G_m$  the transconductance of the first stage and the 0 and pole which appear due to current varying and right up plane 0. This should be a DC gain  $A_{naught}$  of 0 the dominant pole and the non dominant pole.

Now, that we have spent lots of time evaluating, I am not going to write down the expression. The dominant pole appears at the output of the first stage and the non dominant at the output of the second stage and the noise and offset are contributed mainly by the first stage. So, input refer noise voltage density is that and the input referred offset voltage is that and we also calculated the slew rate and the swing limits.

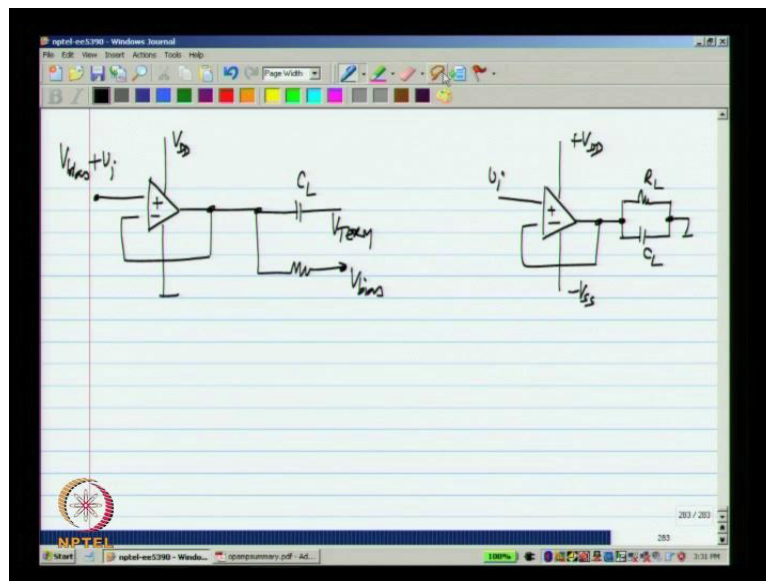
So, what does the second stage opamp operate at? The other opamps that we studied so far told us first of all that it has a higher DC gain that off the small slop  $G_m$  by  $G^3$  square. If it is a capacitive load and even with a resistive load, the first stage has to be



designed to have a substantial amount of gain. The noise and offset contributed only by the first stage. So, it is similar to what we would get as the differential pair and the slew rate. It depends on either the first stage, second stage limiting it can be similar to what we can get in a single differential pair case and finally, the signal ranges the range of input bias voltage and the output voltage are the largest waves in so far.

The input bias range is same as what we would get in simple single differential pairs case and the range of the output voltage is the largest that is possible. That is, within the  $V_{d\text{ sat}}$  of upper rail and the  $V_{d\text{ sat}}$  of the lower rail. Before we go further, little bit clarification on how I connected the load to the 2 stage opamp. As I mentioned earlier they are operating with a single supply. So, the input signal and the load can be connected to some bias current voltages, the  $V_{d\text{ d}}$  on the top and the ground on bottom.

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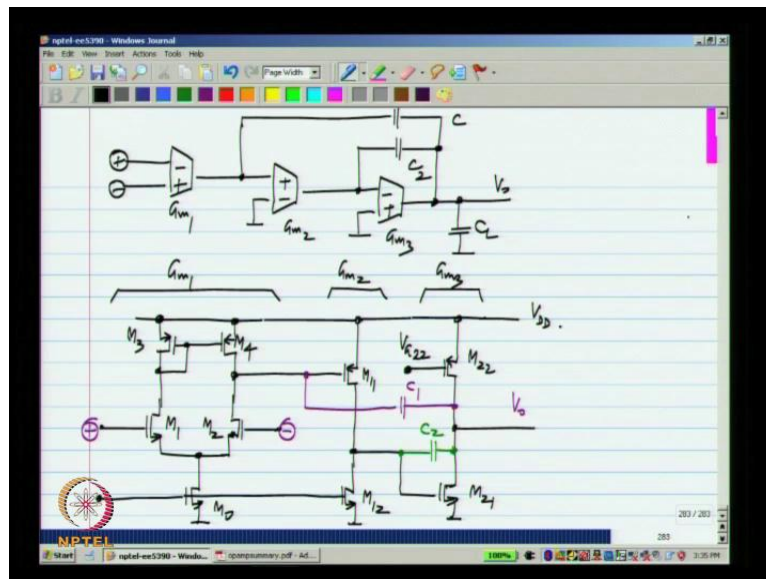
So, the input will be some  $V_{\text{bias}}$  plus  $V_i$ . I have taken a voltage follower as an example, but it can be any circuit and the load that we have must also be connected to  $V_{\text{bias}}$  ok? So, what happens is if  $V_i$  is 0, the input is  $V_{\text{bias}}$ , the output is at  $V_{\text{bias}}$  due to feedback. So, no current will flow through  $R_L$ . In fact, this is the very similar situation to having the conventional picture of opamp with the dual supply and the load going to ground as was explained earlier. Simply by shifting all the voltages in this, we get that circuit. Now if we have only the capacitive load, it is not necessary to connect to the  $V_{\text{bias}}$ .



We can be connected to any voltage because even if we have some DC across the capacitor, it is not going to draw any current. So, if we have only capacitive load it can be connected to any voltage. So, this  $V$  term can be anything, but we do have a resistive load. If the voltage on the right side is anything other than the  $V$  bias, even in the quiescent condition some current will be flowing out of the opamp ok?

What does it mean is, this side I have a resistor here  $R_1$  and this is at some  $V$  bias. It is different from the quiescent output voltage. Current will be flowing through that, that has to be supplied by the transistor  $M_{11}$ . So, that is not a good way to operate it. Just to connect a resistive load, such that the quiescent output current is 0. When we do have a resistive load, we connected up to  $V$  bias. Now, what else is there? With these opamps we have discussed single stage opamp and the 2 stage Opamp. We can make 3 stage opamp by just following this procedure. I will not discuss that in a great detail, but just put on the topology here.

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We know that at the signal level, what we need is three stages. This is the input of the opamp and that is the output. We can think of it as the input  $G_m 1$ , driving a current controlled voltage source with a transadmittance  $S_c$  and a transimpedance  $1$  by  $S_c$  and the current controlled voltage source is made this opamp ok?

In the 2 stage opamp itself, can through of  $G_m 2$  as driving the current control voltage source with the transadmittance of  $S_c 2$  and transimpedance of  $1$  by  $S_c 2$ . Now, how

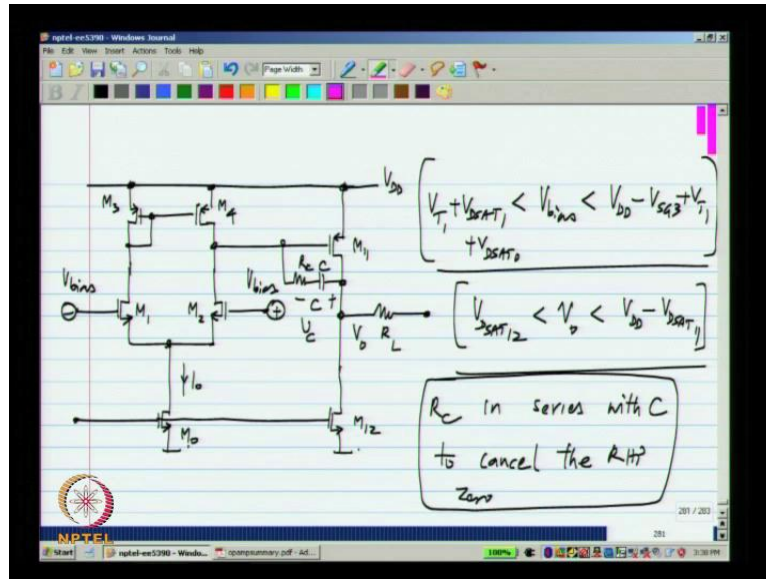
would we go to implementing this is a simple connection of 2 stage opamp we have that can continue the same topology. This forms the second stage  $G_m 2$ . This is  $G_m 1$  and it is required to take the difference between 2 inputs and providing an output current and  $G_m 2$  is single ended. In that, 1 of the inputs is at ground and  $G_m 3$ . Now, we have a freedom to choose either an nmos stage or pmos stage just for variety. Let me make this an nmos amplifier, where this pmos is biased at some fixed voltage. Now, as usual that is derived from current error ok?

So, this is  $G_m 3$ . We have to connect the integrated capacitors. That will be  $C 2$  and this will be  $C$  here. I am not showing requirements like possibly connecting resistors in series with  $C$  and so on. This is the output. This is the negative input, that is the positive input of the Opamp. Now, exactly as we did before, you can analyze this. In fact the transfer function has already been analyzed and you can do the exact analysis including these zeros and poles. The principle is same.

The non dominant zeros and poles are sufficient at the unity loop gain frequencies. So, that the system is stable will behave. Now, at the transistors level, more stages you go to, the more degrees of freedom you have. Now, one obvious one is, now either 2 choose a nmos trans conductors or a pmos trans conductor in the third stage. I have drawn it for the nmos transconductor, but other way round is equally possible. Now, it is also possible to analyse the other parameters like the noise, offset, slew rate, swing limit and so on. It is very obvious that the swing limits are similar to that of the 2 stage opamp.

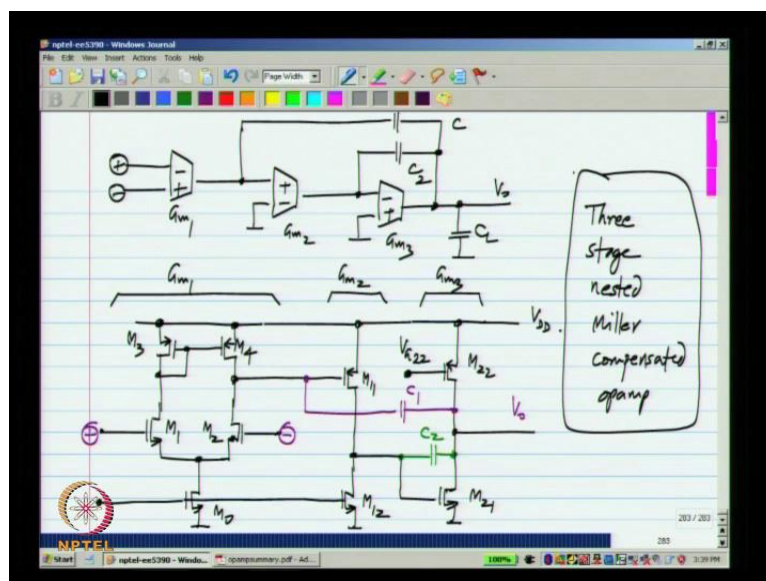
The input bias voltage limits the same and the output voltage can be within one week DC sat of the supply. The slew rate can also be calculated. It is also limited by current in first stage going to capacitor and there is a possibility of the current in the first and the third stage limiting the total slew rate as far as the noise and offset is concerned. As with multistage amplifiers, they are dominated by the contribution from the offsets and the expressions will remain exactly the same, as for the 2 stage opamps, for the simple differential pair single stage opamp. Now, one thing I did not mention earlier. Let us say we have 2 stage opamp. One of the requirements, we can do to make this more stable is to add a resistance in series ok?

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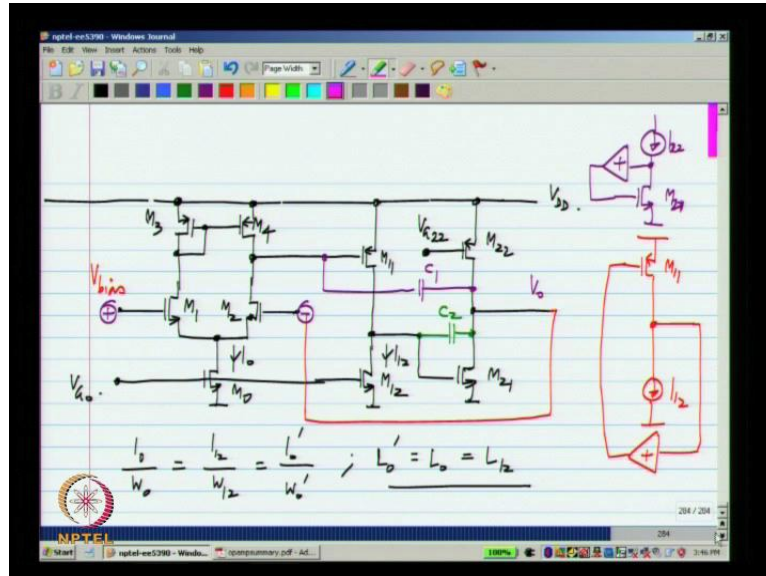
So, that the right of plane 0 cancelled it is implemented exactly as we did in the single level. That is, at the level of transconductance the value of R1 must be equal to 1 over g M 11, in this case 1 over Gm 11 of the transistor M 11. So, now to ensure that, may be difficult if you use a real resistor. So, there is a resistor we put there has to matched to reciprocal of the Gm of the transconductance of the M 11 and sometimes what you can do is to implement the resistor also has mos transistor in triode region. So, that they are matching across process and temperature corners is good similarly.

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If you want tailer to zeros in series with C 1 or C 2 or both, we can connect resistor in a 3 stage opamp. This is 3 stage nested Miller compensated Opamp. Let me copy over this circuit just illustrated the couple of details.

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So, first of all as I mentioned earlier several times the gates of M 0 and M 22 and M 12 and so on are not connected to fixed voltages they are always derived from current mirrors. Let me call this as M 0 prime and this is I 0 prime. As usual, whenever you make a current mirror, you made a lens of all transistors same and the widths are in the ratio of currents. That you let us have this is I 0 and this is I 12. That means, that I naught by W naught should be I 12 by W 12 which should be I 0 prime by W 0 prime and I 0 prime and I 0 and I 12 should all be equal. Let us say now we did not make lengths of M 0 and M 12 equal to each other.

Now, the best thing to do is to not use common biasing line for M 0 and M 12 bias then separately for another connected transistor. Similarly Vg 22 has to come from some diode connected transistor which also is same in length and the width ratio is such that the current ratio is required. So, that is how we bias the opamp, but it is very common some.

If we slow transistors in the circuit, so it is very frequently not shown, current mirror devices are not shown. We show only that much. Now, the other thing is we have a current source going into the drain of the transistor and there is no other path for direct

current DC. Similarly M 22 is a current source that is speeding into the drain of M 21. How is this bias proper? Because, normally if I have something like this that is a  $I_x$  and this is a mos transistor there what is going to be happen?

How much will be the current through this transistor? Unless there is feed back around this transistor we cannot say that the current in this will be  $I_x$ . The transistor is a unilateral device. It is only by adjusting the  $V_g$  s that we can change the drain current. We cannot apply a current through a drain directly and expect the  $V_g$  s to be established automatically. We have to provide the feedback from the output from the drain side to the input side to  $V_g$  s so that the correct  $V_g$  s is established for whatever bias current we want to have in the opamp. We have drawn it. The current source is going directly to the drain and nowhere else. Obviously, as we know opamp can be used only inside a feedback loop ok?

Let me again for illustration consider a unity gain pole over. What happens in that case? You have a connection from there to there and the plus input. That is why it is biased at  $V_{bias}$ . Now, if you think of let us say M 11, M 12 states, let me redraw that here. So, this M 12 is a current source. So, I show it as a current source. This is  $I_{12}$ . There is feedback through this M 21 and through the input differential pair. Now, if you see from here to there, there is an inversion. This is a common source amplifier and from there to the drain of M 2, there is an inversion. So, what we have is some amplifier with a positive incremental gain feeding back to the gate of M 11.

We know that this is exactly what we need if the voltage here increases. That means, that the current in M 11 is too much and gate voltage should be increased so that it reduces and vice versa for smaller current. Similarly, if we think of M22 and M 21, M 22 is a current source  $I_{22}$  and this is a M 21. So, that again is the gain from here to there is negative and the gain from there to there is negative. It is a common source amplifier. So, we have a positive incremental gain amplifier connecting that way and we know that if we do that M 21 is a negative feedback and a current  $I_{22}$  flows through that.

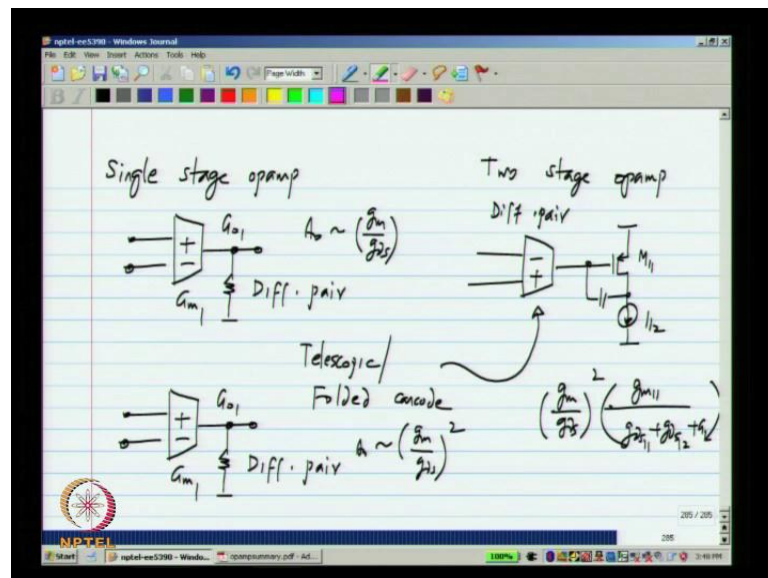
So, if there is DC negative feedback around the entire opamp, each of these stages will be negative feedback and everything will be biased correctly. If you operate the opamp in open loop, there is no guarantee that bias current will flow through the transistor because we have to establish the  $V_g$  s for the transistor for correct current to flow. Now,

while discussing opamp, already we have heard that we have to use them in negative feedback this is the reason ok?

If they are not in negative feedback and you apply a 0 differential input voltage, there is no guarantee that the opamp will be biased properly. In fact, because of mismatches and so on there is almost guaranteed that the transistor will all being some triode region. 1 of the transistors will be triode region. That is about DC negative feedback around the opamp.

Now, let us say the 2 stage opamp used a gain of  $G_m$  by  $G_d$  s square. Let us say we want even higher gain. What should we do? For a 3 stage opamp and we can go for 4 stage opamp and so on. That is possible. That is one of the ways of doing it. Also there are other ways. What we want to do is to go through the DC gain. What did we have?

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We have a single stage Opamp of some  $G_m$  1 and this is just a differential pair. It has some  $G_{naught 1}$  and the DC gain approximately  $G_m$  by  $G_d$  s of a single transistor. We can also simplify this by going into telescopic or folded cascode. What that will do is to have a similar topology.

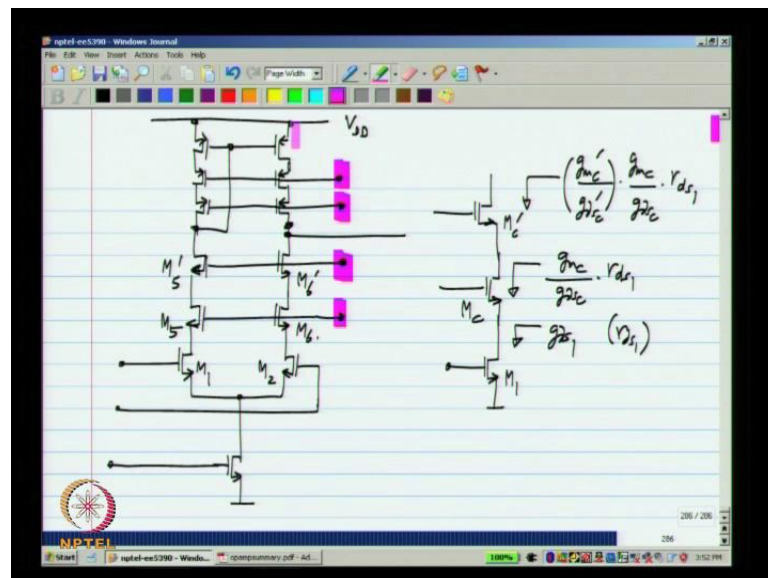
But the gain will be approximately  $G_m$  by  $G_d$  s square. Now, we had a 2 stage opamp. We use a simple differential pair here followed by the second stage that is  $M_{11}$  with a current  $I_{12}$ . What we can instead do if you use a telescopic or folded cascode at this

stage. If we do that, what happens is the gain of first stage increases. It will be of approximately  $G_m$  by  $G_d$  s square and the second stage will have a gain of  $G_m$  11 by  $G_d$  s 11 plus  $G_d$  s 12 plus  $G_l$ .

So, by increasing the first stage gain, we can increase the gain of overall opamp. So, we can still stay with 2 stage. Which means that the composition scheme, the scheme to make the opamp behave like a integrate is as same as 2 stage opamp, but the difference is... So, we can stay just with 2 stages and have a higher gain by making first stage as a telescopic cascade opamp or a folded cascade opamp ok?

This is the very commonly used technique as what does it happened is that as we go finer and finer technologies that is shorter and shorter channel lengths. The problem is that the  $G_m$  by  $G_d$  s transistors will keep becoming smaller and the smaller. This is simply because the length is becoming smaller. Now, if we make the length higher and a higher values of  $G_m$  by  $G_d$  s, but that reduces the speed. So, if you stay with shorter channel length, the way to increase the gain is to go for a cascade first stage and the second stage so that with 2 stages you will get a very high gain. So, that is very much possible and that is also quite frequently done.

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Now, another possibility is that we used not just 1 cascade, but 2 cascades. Usually such a thing is called as triple cascade. I will show it for the telescopic cascade topology. Now, just to illustrate the principle, I will show also a just common source amplifier



looking in here. That is why it is  $M_1$ . I will have  $G_{ds1}$  as the output conductance or  $V_{ds1}$  as the output resistance.

If I cascade with C, the output resistance will be  $G_m c$  by  $G_{ds c}$  times  $R_{ds1}$ . I could cascaded with 1 more transistor that is why  $M_c$  prime the output resistance will be  $G_m c$  prime by  $G_{ds c}$  prime  $G_m c$  by  $G_{ds c}$  times  $R_{ds1}$ . So, it is even higher. Same thing can be done with the opamp as well. This is a differential pair of 2 cascades ok?

We have  $M_1, M_2, M_5, M_6$  earlier and that is why I call it as  $M_5$  prime and  $M_6$  prime and similarly on top I need to have a current source with 2 cascades. There is no point in proving only one side on both sides is contributing to the output conductance. So, I should have a current mirror which is also triple cascaded. So, we need to establish a bias voltages at all these points. So, that all transistors remain in saturation and afterword similar thing can be done with folded cascade as well. Also an additional constraint is that we have now stacked more transistors.

So, that means, that things will be constrained more even before. So, we can have more and more cascades, but we will have lesser and lesser swings, but when you have a 2 stage opamp the swing at the output of the first stage does not have to be very high with this. It is possible to do this. So, some times when you want even higher DC, you can go for something known as triple cascade in the first stage and in the second stage ok?

There are lots of alternatives and lots of possibilities. One of the reasons why you should not try to remember the topologies without understanding what is going on behind them is because I have some basic topologies. I can combine them in many different ways to get seemingly very different alternatives, but once you understand the underlined principles they are all the same. So, we started with a single stage opamp. We went to telescopic and folded cascades. That is one way of increasing DC gain. We can go to 2 stage opamp as another way of increasing the gain.

So, in some ways the 2 stage opamp and the telescopic or folded cascade will have same DC gain. If you have a capacitive load, you have a resistive load. You cannot use cascade stage because that only increases output resistance, but does not increase the transconductance. Now, if you want further increasing gain, you can go for 3 stages or 4 stages or you can go for triple cascade telescopic stage or triple cascade folded cascade

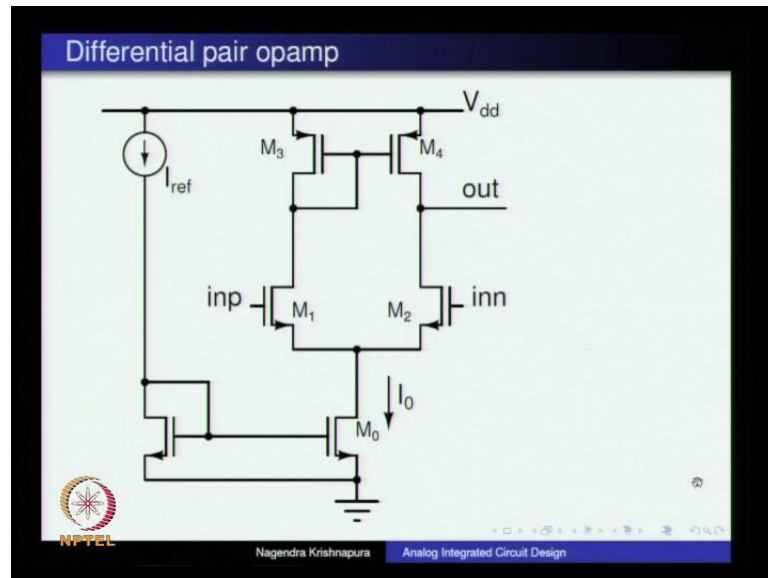
stage. Alternatively you can combine the 2. You can have a telescopic stage followed by second stage or a folded cascade stage followed by second stage and so on.

The possibilities are endless and it is up to you as a designer to pick the right one for you. If you understand the trade of arrival you will be able to do that. Now, as usual in design you have a number of parameters and you will not be able to put down all the parameters on the paper and then turn them into equations and get the dimensions of all transistors ok?

It is very important to understand what to change if something is deficient. Let us say you have designed a 2 stage opamp and you have to find the dc gain to be too little. What can you do? You have to increase the gain of the first stage. That is an easy possibility or you increase the length of the transistors of the first stage or you go for the cascade for first stage. Those are all the possibilities ok?

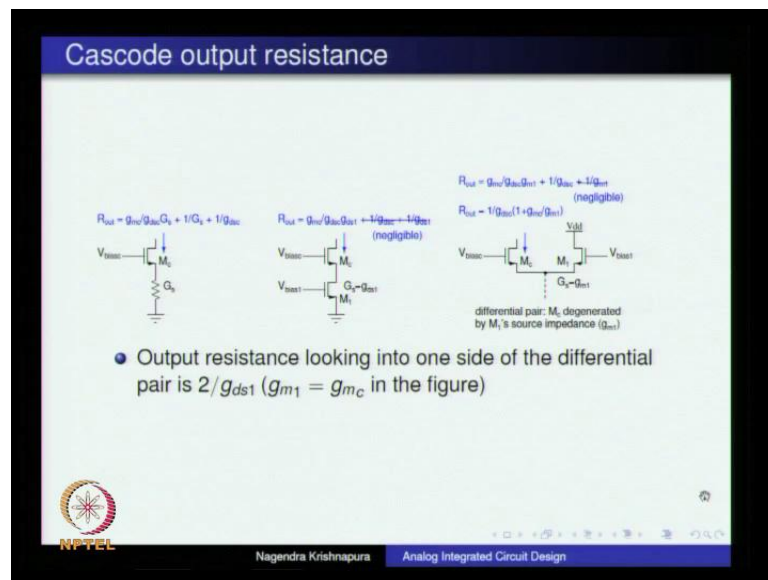
Similarly, let us say you find that the input of the noise of 2 stage opamp is too much. Then what you will do? You know that is the first stage so, you have to manipulate the first stage in some way and you would not like to affect the transfer function at all. So, you do noise scaling for the first one. You do impedance scaling for noise scaling for first stage. Now, that way increases the transconductance of first stage. It means that you have to change the integrating capacitor so that your opamp behaves exactly as same as before. So, you may have to change different things by keeping some other things constant.

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So, if you understand the basic principles very well, you will be able to do this quite easily. This is a quick summary of opamps that we studied so far. This is the differential pair opamp.

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Now, the output resistance can be calculated using this. We know this is the output resistance of the cascode. It is given by this formula. When we have a resistor with conductance  $G_s$  and the source of the transistor  $M_C$ , we have another transistor. It will be  $G_d s 1$  instead of  $G_s$  and finally, if we have a differential pair, it is as though this

transistor  $M_1$ . The impedance looking at source is at the source of this transistor  $M_c$ . So,  $R_{out}$  is  $1 / (G_{dsc} (1 + G_m s))$  and  $G_m s$  happens to be equal to  $M_1$ . This is simply  $G_{dsc}$  or the output resistance is 2 times  $R_{dsc}$ .

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**Opamp: dc small signal analysis**

- Bias values in black
- Incremental values in red
- Impedances in blue

Total quantity = Bias + increment

The slide includes the NPTEL logo and footer text: Nagendra Krishnapura, Analog Integrated Circuit Design.

The following slide shows all Opamps with bias values in black, incremental values in red, impedance in blue. The total quantity of course is bias plus increment.

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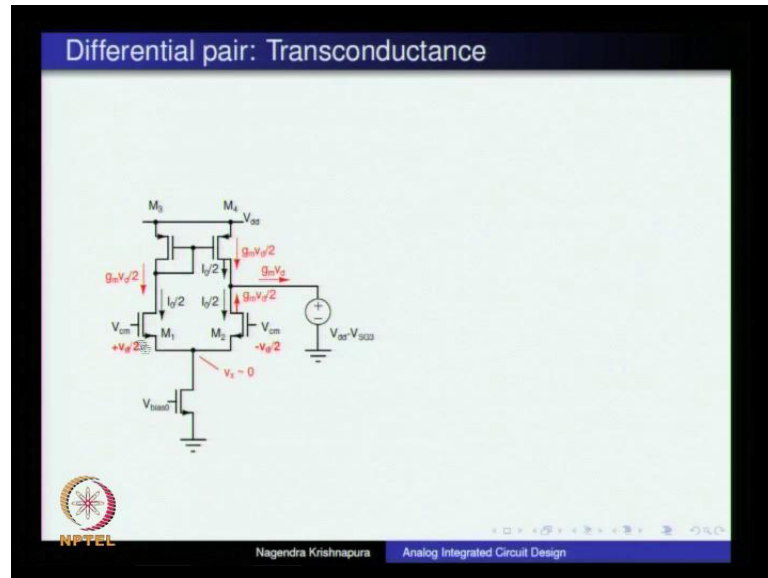
**Differential pair: Quiescent condition**

The slide shows two circuit diagrams of a differential pair. The left diagram shows the full differential pair with bias values in black, incremental values in red, and impedances in blue. The right diagram shows the same circuit with a current source  $I_{tail}$  and a voltage source  $V_{diff}$  connected to the sources of  $M_1$  and  $M_2$ , with the label "zero current".

The slide includes the NPTEL logo and footer text: Nagendra Krishnapura, Analog Integrated Circuit Design.

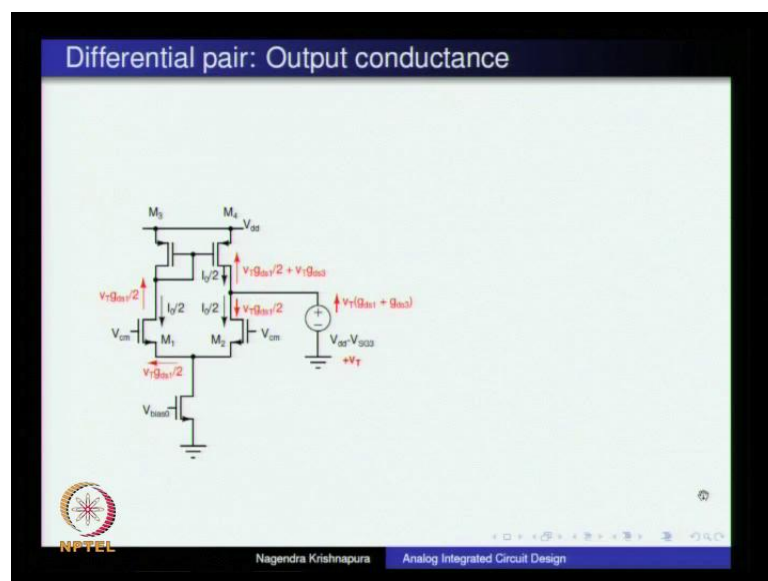
So, we said that this and that voltages are equal by symmetry. That is how we started the analysis. So, if we terminate  $V_d$  s plus  $V_g$  s 3, nothing will flow there and  $I_{naught}$  by 2 flow through all these 4 transistors where  $I_{naught}$  is the tail current.

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To calculate the trans conductance, we have this incremental voltages  $V_d$  by 2 that cause the current  $G_m v_d$  by 2 here and  $G_m v_d$  by 2 in the opposite direction. So, net current of  $G_m v_d$  is flowing through the output.

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To calculate the output conductance, this is what happens if we apply a positive voltage  $V_t$ . We will have  $V_t$  of  $G_{ds1}$  by 2 flowing this way and that will also get an error. So,  $V_t$  of  $G_{ds1}$  by 2 will flow there plus  $V_t$  of  $G_{ds3}$ .

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**Differential pair: Noise**

- Carry out small signal linear analysis with one noise source at a time
- Add up the results at the output (current in this case)
- Add up corresponding spectral densities
- Divide by gain squared to get input referred noise

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So, that is how we get output current at  $G_{ds1}$  plus  $G_{ds3}$ . So, similarly we can calculate the noise and the other parameters. We will continue with that in a next lecture.