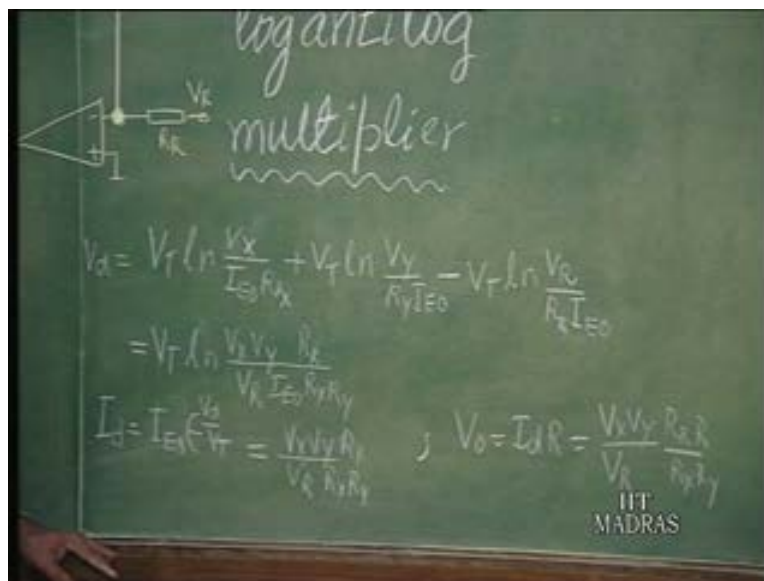


Electronics for Analog Signal Processing - II
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Lecture - 31
Log - Antilog Multipliers

In the last class, we discussed log-antilog amplifiers. Let us now consider how a multiplier can be built using log-antilog operation. This, I had illustrated in the end of the last class. Suppose we develop a voltage which is summation of log of voltages, $V_T \log$. These are all diode voltages. $V_T \log V_x$ by I_E naught R_x this is one log amplifier voltage, plus $V_T \log V_y$ by $R_y I_E$ naught minus $V_T \log V_R$ by $R R I_E$ naught. Then, that voltage will be looking as $V_T \log V_x V_y$; these will be getting multiplied, divided by I_E naught squared $R_x R_y$, multiplied by I_E naught. So, I_E naught gets cancelled. $R_x R_y$, divided by V_r .

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So, that is the voltage that you develop and that voltage, if it becomes the forward biasing voltage of another diode, then you take a...antilog of that voltage. That means that will be I_E naught exponent V diode divided by V_T . So, this V_T , V_T gets cancelled. It is

exponent log of this value which is that value itself; $V_x V_y$ by V_R , $R_x R_y R_R$; I_E naught getting cancelled.

So, that I illustrated as a sort of place where it is not necessary to use compensated amplifiers because when you take log and antilog, both effect of V_T and I_E naught get cancelled. So, this current is got. This is a very accurate method of getting this multiplier and this current when it is made to pass through a resistance, develops a voltage which is $V_x V_y$ by V_R .

If I make R_R , R_x , R_y all equal resistors, then we know that this becomes $V_x V_y$ by V_R and V_R can be made equal to 10 volts and we have the multiplier. But this is one quadrant multiplier because you please note that all these diode voltages are valid for one polarity of the current.

So, this is called a single quadrant multiplier. Single quadrant multiplier because $V_x V_y$ and V_R can only take one polarity; in this case, let us say plus. How to implement this scheme using, let us say op-amps and transistors is what we are going to now see.

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Handwritten equations on a chalkboard:

$$\frac{V_y}{R_y I_{E0}} - V_T \ln \frac{V_R}{R_R I_{E0}}$$

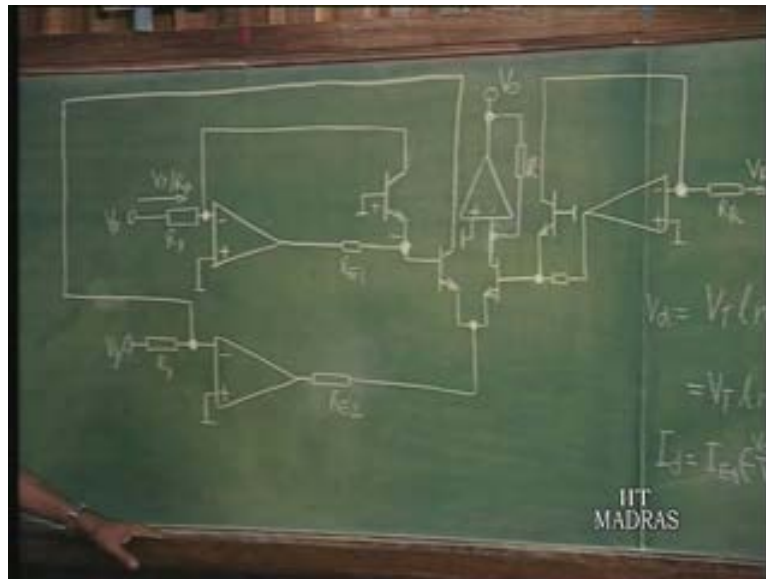
single quadrant

$$; V_o = I_d R = \frac{V_x V_y}{V_R} \frac{R_R R}{R_x R_y}$$

IIT MADRAS

This is the circuit of a log-antilog multiplier. Let us see what it is. I have the op-amp here and V_x is connected and R_x is connected like that, so that current in this is V_x divided by R_x . So, this converts this voltage into current. This current is now made to flow through the collector of a transistor which means that is done by the op-amp's negative feedback.

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So, this op-amp has a negative feedback arrangement such that this current is forced to flow through this. If that current flows, then the voltage here is going to be V_{BE} corresponding to that current, which corresponds to nothing but $-V_T \log V_x$ by I_E naught R_x . So, this voltage here is nothing but $-V_T \log V_x$ by I_E naught R_x . So, we get here this voltage straightaway; but the thing is, I can, for negative feedback, keep this connected to this output.

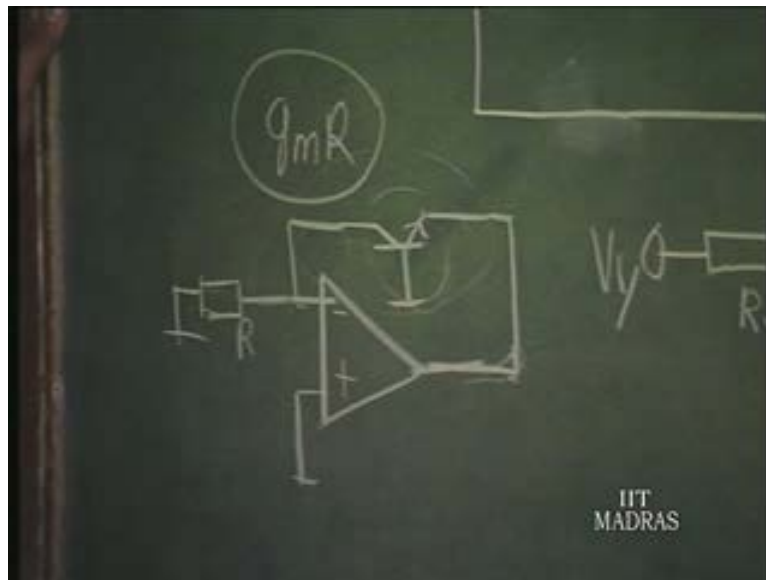
Now I just want to digress a little bit and say why this is not connected here. This particular thing is not connected here because look at this log amplifier of ours.

If this is like this, this is what we discussed as a log amplifier. If you consider this as a feedback circuit, the original amplifier was getting fed back from this point - unity gain feedback.

Now you are putting output of this to an amplifier here. This is nothing but a common base amplifier. This is fed to the emitter and at the collector load you are taking the output. So, it is not a simple op-amp. It is an op-amp with active feedback. In that, there is normally passive feedback is used. Here, in this case, it is a thing with active feedback because feedback factor can be more than one.

So, this feedback factor in this case is nothing but $g_m R$ where g_m is $1/R_e$ of this transistor. This is the gain of this. There is no phase shift between this voltage and this voltage which is common base. Therefore, this is a negative feedback with feedback factor itself equal to $g_m R$.

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If the amplifier gain is A naught, A , then A into $g_m R$ should be less than 1, when the phase shift of A is equal to 180 degree. That is the condition for frequency compensation; otherwise, it will go into oscillation.

Normally, what is done for making these op-amps work is when the phase shift of A is equal to 180 degrees, magnitude of A is made less than 1.

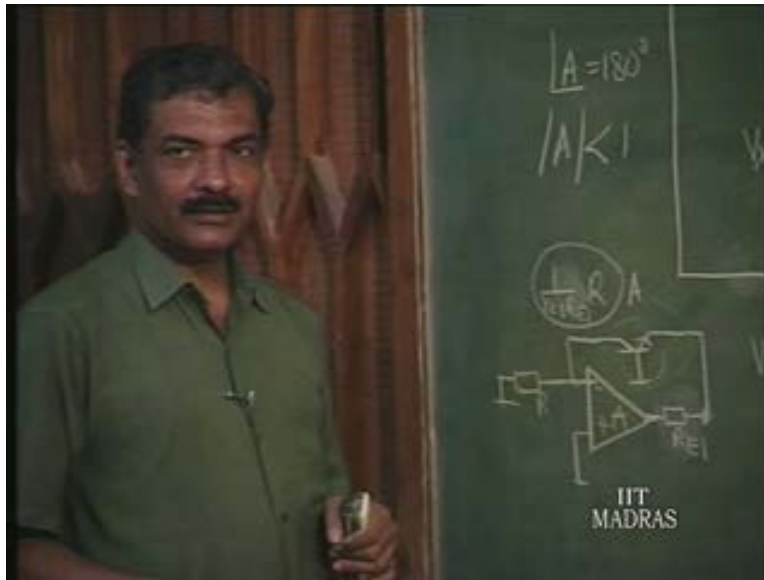
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But that will be violated here, when the phase shift of A equal to 180 degree occurs at the same frequency as the other one. But the magnitude of the whole thing, loop gain, even if A is less than 1, is not going to be less than 1 because g_m into R may be greater than 1.

So, this might go into oscillation even if the op-amp is compensated for unity gain. So, this will go into oscillation. How to prevent this or how to use compensated op-amp here and not cause any oscillation in this circuit? That can be done by reducing the gain here. So, that means g_m has to be reduced. g_m is reduced by putting a resistance in series with R E, let us say, R E 1. So, this g_m , instead of small r e, 1 over small r e, it will be 1 over small r e plus R E 1, so that R over R E 1 is less than 1.

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So, that is the idea for putting a resistance in series here. Now, whether you put a resistance or not, the voltage developed is going to be always the same in order to make this current flow.

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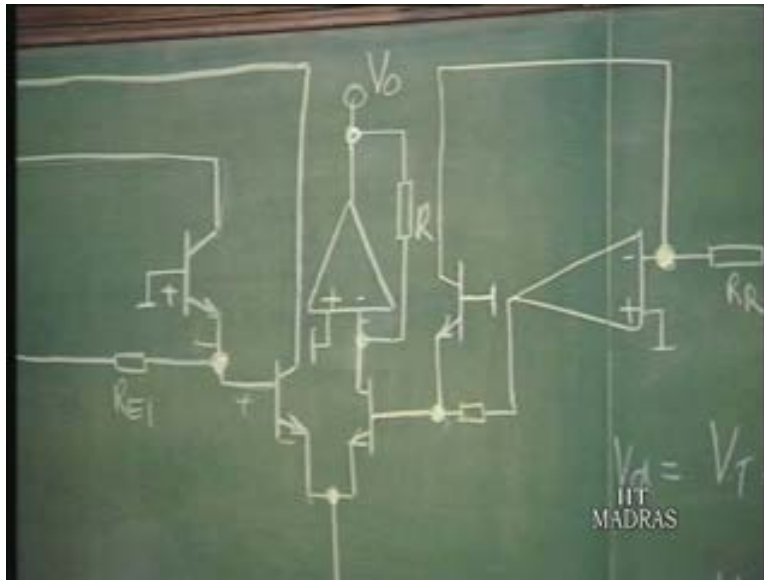
So, this is something that you have to see that in all log amplifiers, they will put a resistance in series in order to make it work for the same frequency compensation arrangement as before. Now, what happens to the output voltage? Obviously, R_E can be made very large so that this can...gain can be reduced considerably. That is not the point. As R_E is increased, the voltage which is necessary to sort of for...a certain current is going to increase, because suppose 1 milliamperes flows through this.

Normally, if you have not put a resistance here, the voltage would have been the diode voltage. But now that you have put a resistance, this voltage has to rise up to 1 milliamperes into R_E . That should not go up to the supply voltage. That means R_E cannot be increased so much that it goes up to supply voltage. So, this is the limitation of this circuit.

Now that we have understood the presence of R_E , how to select it, we can further discuss about the circuit for multiplier.

So, we have already developed a voltage. This corresponds to $-V_T \log V_x$ by $R_x I_{E0}$ with respect to ground. Now, to this voltage, we have to add $-V_T \log V_y$ by $R_y I_{E0}$. So, that we can add by putting a...another diode, whose current is forced to be equal to V_y by R_y . So, that can come in series; addition of...so, base emitter junction.

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The collector of this should be all the way connected to this point so that the current is V_y by R_y . In order that the feedback is effective, obviously, the emitter of this is connected through another R_{E2} to the output. So, you can see that this transistor, base to emitter junction voltage is decided by the negative feedback arrangement of this...

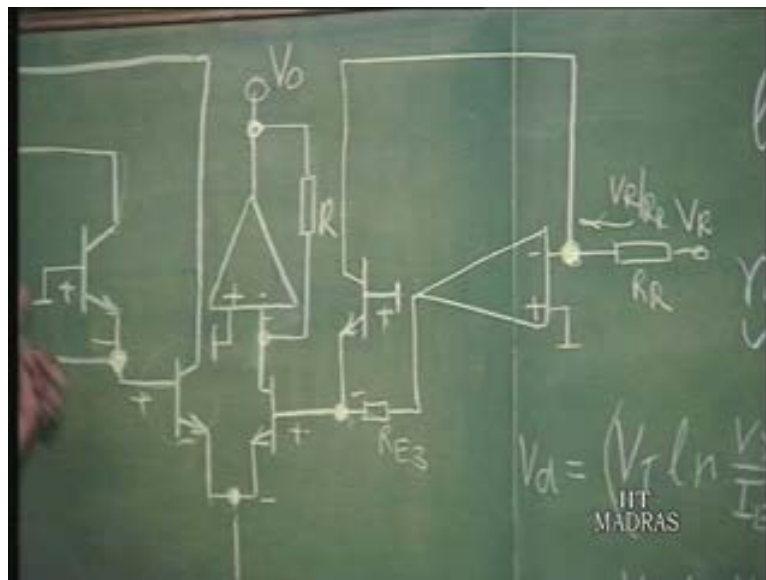
So, V_y by R_y is the current here and this collector current is forced to be the same as this. So, emitter base voltage is going to be that minus $V_T \log V_y$ by $R_y I_{E0}$ naught; and that gets added automatically here. If I connect the negative feedback, R_{E2} has the same property that I mentioned about R_{E1} , in order to make the frequency compensation become valid; and also, in order to prevent the op-amp from going to saturation in that attempt.

Now that we have got here a voltage which is summation of minus $V_T \log V_x R_x$...by R_x into I_{E0} naught minus $V_T \log V_y$ by R_y into I_{E0} naught here, this is what we have got. Of course, only negative sign. So, this is a negative voltage. This is a negative voltage comprising of sum of these. Then I had to subtract from this another voltage which is minus $V_T \log V_R$ by $R_R I_{E0}$ naught, I had to subtract; or, what I can do is I can again for these two voltages to be the difference voltages, both are negative; and

apply that as the diode voltage. So, this also I generate with respect to ground. What is the voltage that we want to generate?

Corresponding to minus $V_T \log \frac{V_R}{R R I_E}$ naught; you can see V_R by $R R$ is the current here and this collector current is forced to be the same as that. If the emitter resistance, let us say R_{E3} is properly chosen so that it is connected to the op-amp output automatically, this voltage is developed. So, this voltage minus this voltage is going to be the voltage...that is going to be the voltage between these two terminals of another base emitter junction, which will convert the voltage into antilog current.

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So, this voltage now is nothing but this negative voltage minus another negative voltage and that is more negative on this side and more positive on this side. So, this is forward bias by a voltage which is equal to this, exactly. So, this generates then a current which is I_{diode} which is going to pass through a resistance R and therefore that will be developing voltage like this. So, V_{naught} is going to be nothing but I_d into R . This is at zero volts.

So, this amplifier converts that current into a voltage I_d into R and as you can see here this, if you have 4 op-amps and 2 pairs of transistors match, you yourself can build a very accurate log-antilog multiplier.

These matching pairs of transistors are available very readily as transistor. You can build a multiplier very easily and this will be very accurate as long as they are perfectly matched. What you have to remember is this is only a single quadrant multiplier, because the current can only flow in this direction in all these things. So, V_x , V_y , V_R , have to be all positive in this case.

So, it is going to work only in one quadrant. So, only in this quadrant it is going to work; but that is not a very serious limitation because by properly selecting this operating point of this, I can make it work for signal which is going both positive and negative. That means I can put V_x as equal to V_x dash plus 10 volts, V_y as V_y dash plus 10 volts.

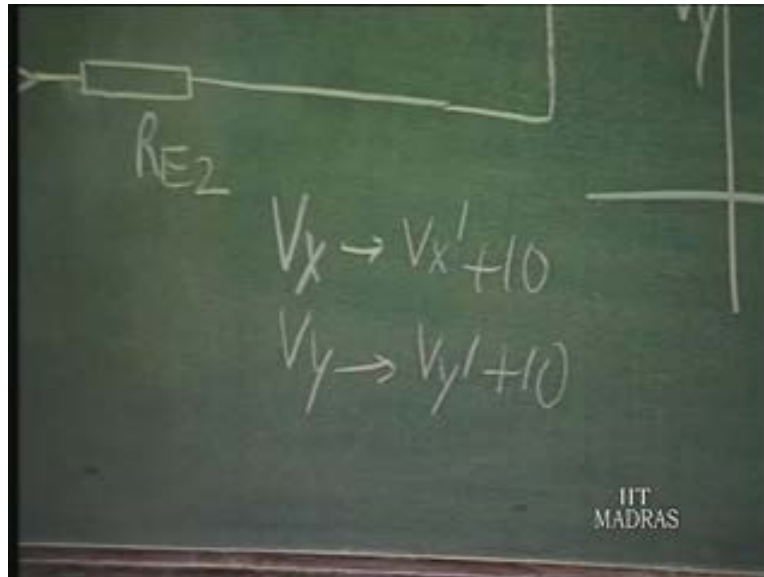
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So, what I can do is V_x can be put as V_x dash plus 10 volts. V_y is V_y dash plus 10 volts. Both V_x dash and V_y dash have to go 2 plus minus 10 volts. That means effectively, V_x and V_y will have to go up to 20 volts in this case. Therefore, if V_x and

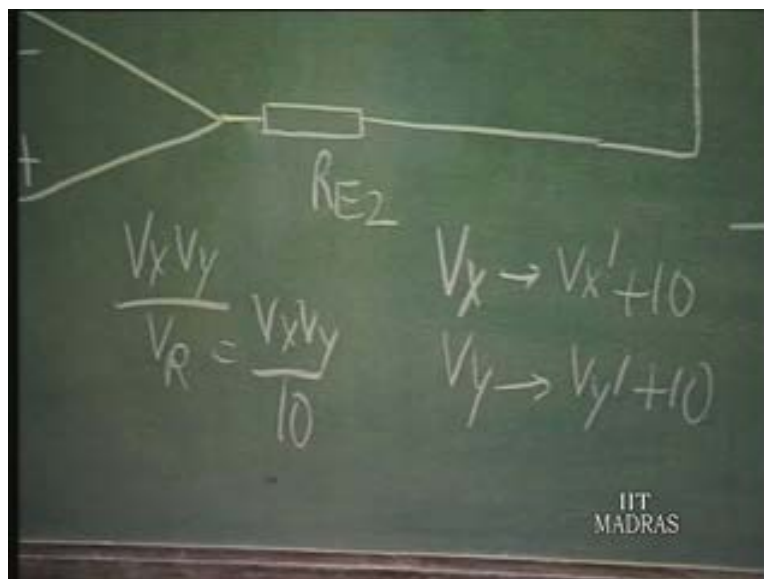
V_x and V_y limits are made equal to 20 volts, zero to 20 volts, then V_x and V_y can be made plus minus 10 volts. Then, we will do the multiplication using this.

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This will be $V_x V_y$ by V_R which is $V_x V_y$ by 10 volts. V_R can be made equal to this 10 volts. So, $V_x V_y$ by V_R .

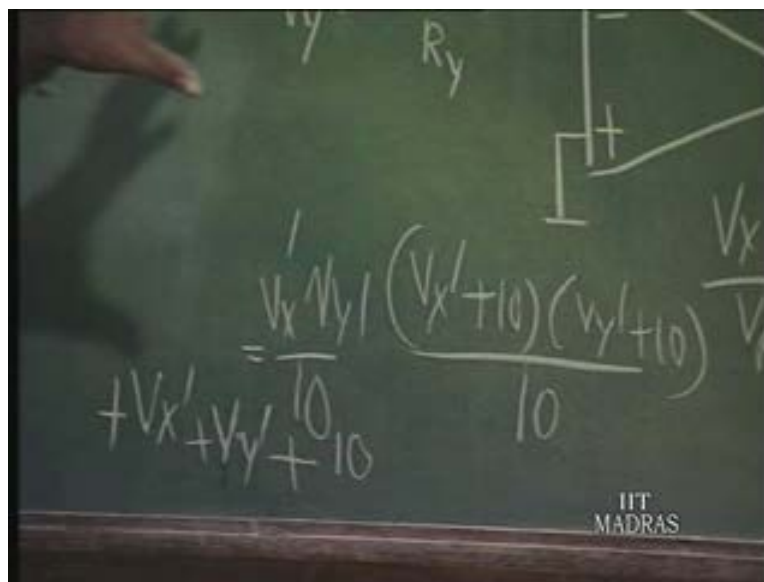
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So, what it will become is V_x dash plus 10, V_y dash plus 10 divided by 10. So, this is going to be equal to V_x dash V_y dash by 10 which is what we want here, plus...now, you will have error components in this. V_x dash into 10 by 10. That means this will have V_x dash along with it. Then V_y dash into 10 by 10. That is, plus V_y dash, plus 10 into 10 by 10. That is the offset.

So, this as the x feed through y feed through and the offset which can be subtracted because we have already V_x dash and V_y dash as input to the multiplier. So, you subtract V_x dash V_y dash and the D C of that 10 volts. Then you will get at the output of this which is V_x dash V_y dash by 10 volts as the apparent multiplier.

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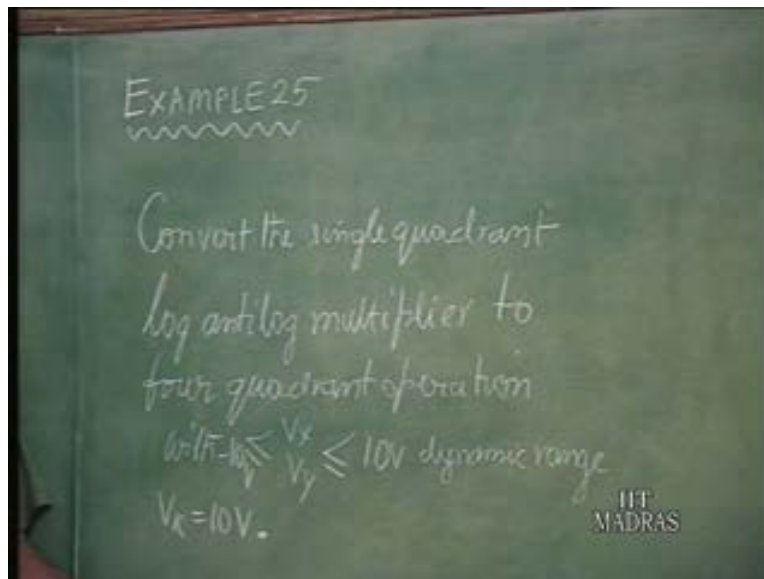
So, any single quadrant multiplier can be converted to four quadrant by means of the pre bias arrangement. Once again, we made V_x is equal to V_x dash plus 10 volts so that V_x dash can vary from plus 10 to minus volts as desired by us, when V_x is going on varying only from zero to 20 volts, because it is single quadrant.

Similarly V_y , when it varies from zero to 20 volts, this V_y dash can vary from plus 10 volts to minus 10 volts. Then we get the multiplied output of this multiplier, single

quadrant multiplier, as $V_x - 10$, $V_y - 10$, divided by 10 which will give us the wanted output which is $(V_x - 10)(V_y - 10) / 10$. This can be deducted from the total output of the multiplier by using another operational amplifier which we know how to design, because in our earlier discussion we have discussed how to design an amplifier which will subtract whatever voltage you want to from the output.

So, the offset can be removed, the x feed through can be removed and y feed through can be removed, so that output of that op-amp which is subtracting all these things will be giving you the four quadrant output, $V_x V_y / 10$. So this particular thing, we will work out as an example so that we can design a four quadrant multiplier out of a single quadrant one.

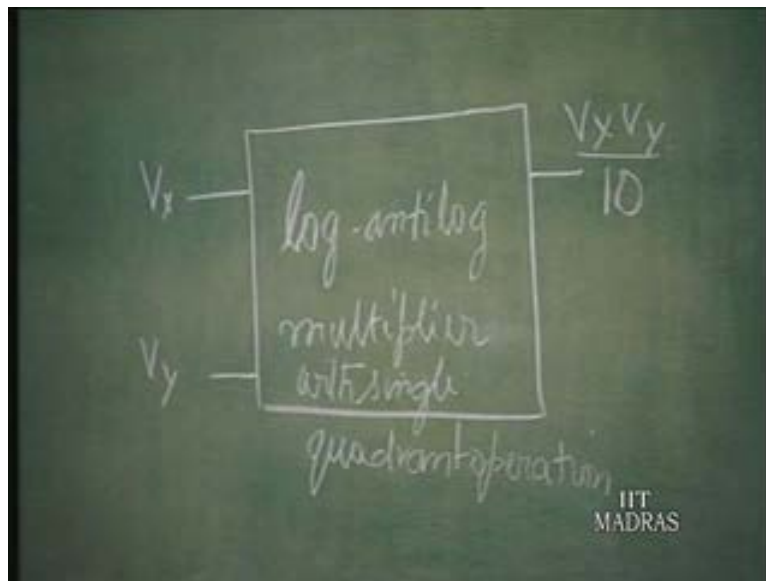
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Consider this example in order to illustrate how to convert any four quad...single quadrant multiplier into four quadrant. Example 25. Convert the single quadrant log-antilog multiplier to four quadrant operation with 10, minus 10 volts less than or equal to $V_x V_y$ less than or equal to 10 volts dynamic range. V_R equal to 10 volts.

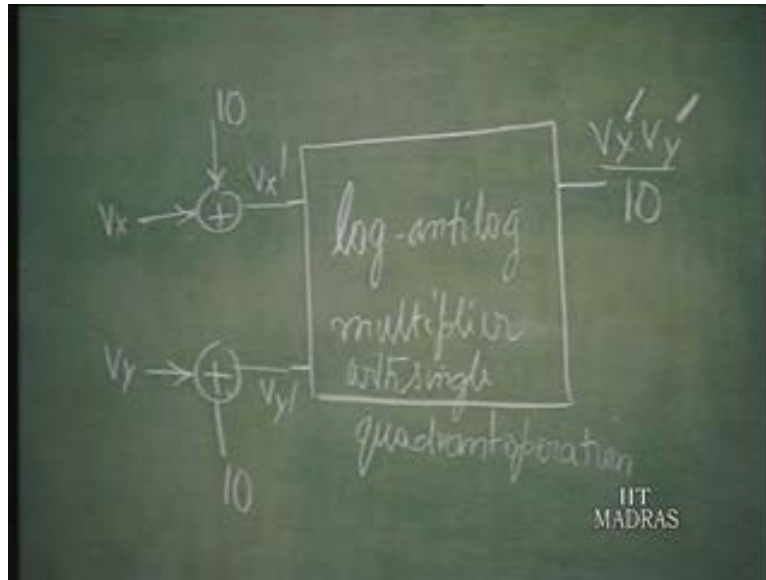
So, let us assume that this is my...the block that we have already discussed log-antilog multiplier with single quadrant operation. So, we want to give this, let us say input V_x and V_y ; output, we will get as $V_x V_y$ by 10 volts by making V_R equal to 10 volts. Only thing is how to select V_x and V_y such that it is operated in single quadrant even though our actual input is plus minus 10 volts, dynamic range.

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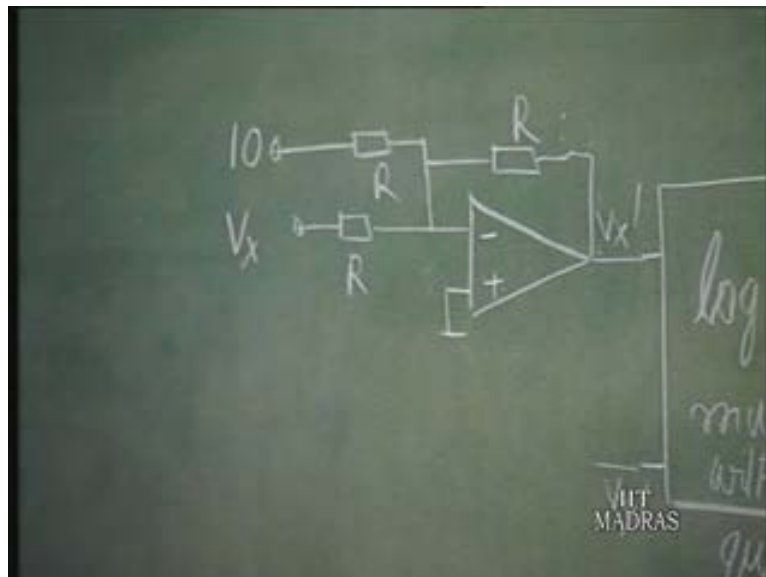
So, we have to assume that we will give this V_x dash and V_y dash. So, this is going to become V_x dash and V_y dash into 10 volts. So basically, we have to have now V_x dash and V_y dash as nothing but V_x ... This is V_x dash and V_y dash. V_x plus 10 volts is V_x dash; V_y plus 10 volts is V_y dash.

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So, this can be easily done with the help of an op-amp. This op-amp I do not have to really draw because all of you are knowing how to do it. So, one simple way is... So, you have here, let us say... V_x let us say; and this is 10 volts. This is R, R, R.

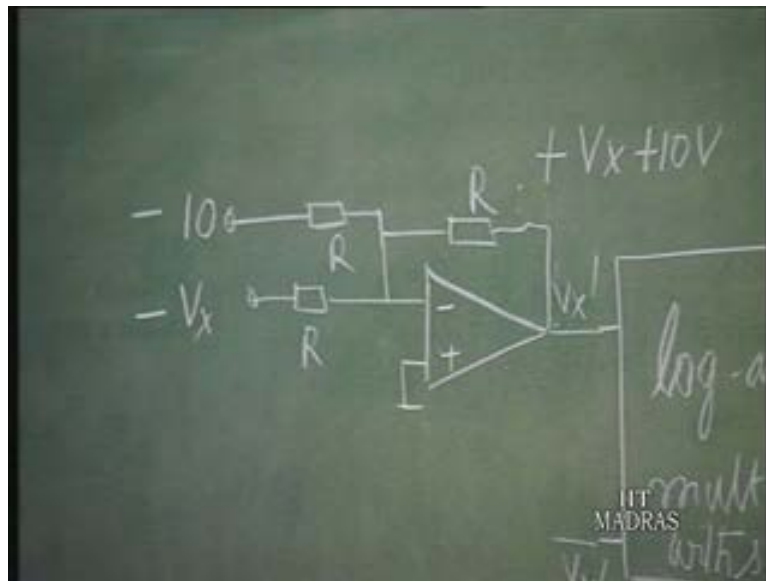
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So, what will appear at V_x' is minus V_x minus 10 volts; minus V_x minus 10 volts...so, if this is operating only in one quadrant corresponding to only negative

voltages. If it is operating with only positive voltages, then what we have to do is apply minus x , V_x and minus 10 volts here. Then, this will be plus V_x and plus 10 volts; or use a summing amplifier which will not give a phase inversion of 180 degree. That also can be done.

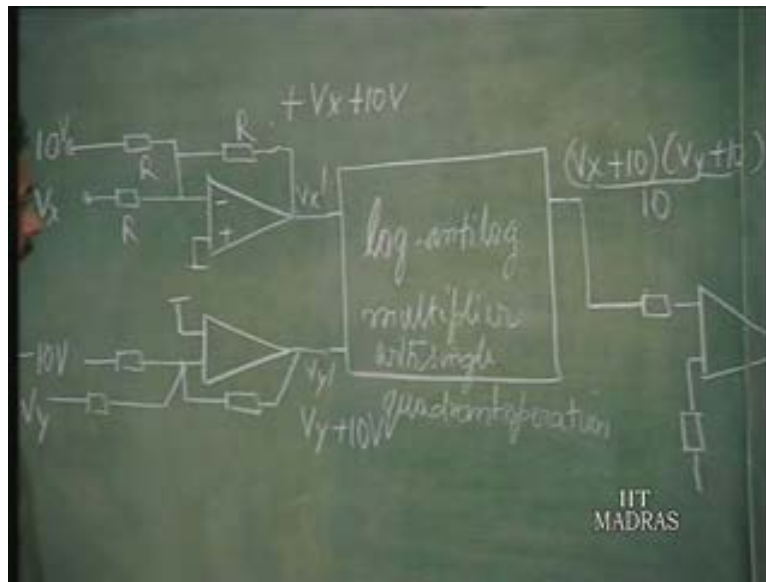
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I just want to illustrate the point. Now another one, where we will give minus 10 volts and V_y , minus V_y . So, V_y dash now becomes plus 10 volts plus V_y . So now, output is V_x dash V_y dash by 10 volts, which is essentially speaking, equal to V_x plus 10 into V_y plus 10 divided by 10, which as I told you earlier, has the wanted component of $V_x V_y$ by 10 and x feed through of V_x and y feed through of V_y and an off...D C offset of 10 volts, which has to be deducted from this.

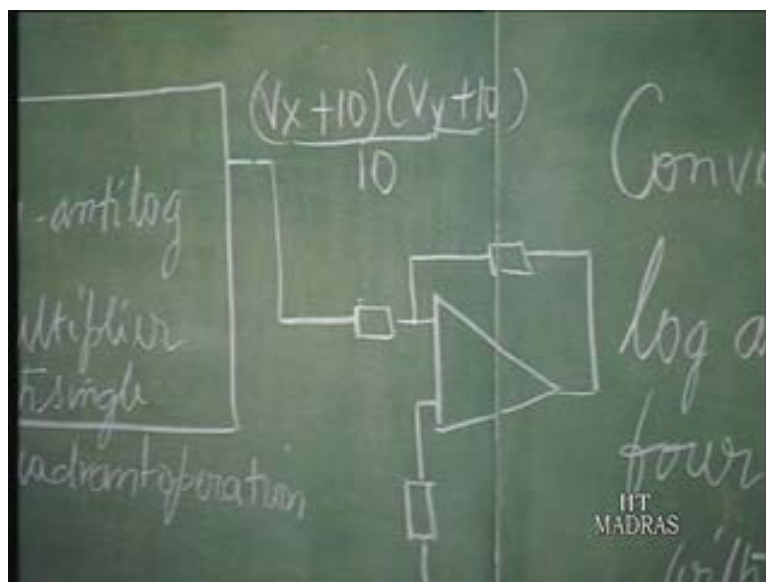
So, let us assume that this is going to be another amplifier that I am going to use for the purpose of subtraction and all that. How to do that? So, we have from this, 10 volts to be subtracted.

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This particular thing let us say, is going to be there such that it is going to simply invert this.

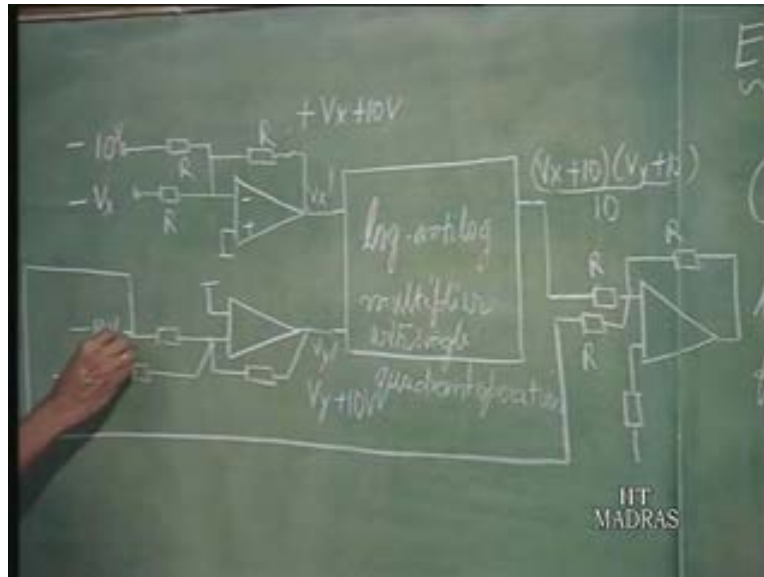
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So 10 volts to be subtracted from this has to be applied to... You have minus 10 volts; you can therefore add minus 10 volts to this. So, this minus 10 volts is already here. So in

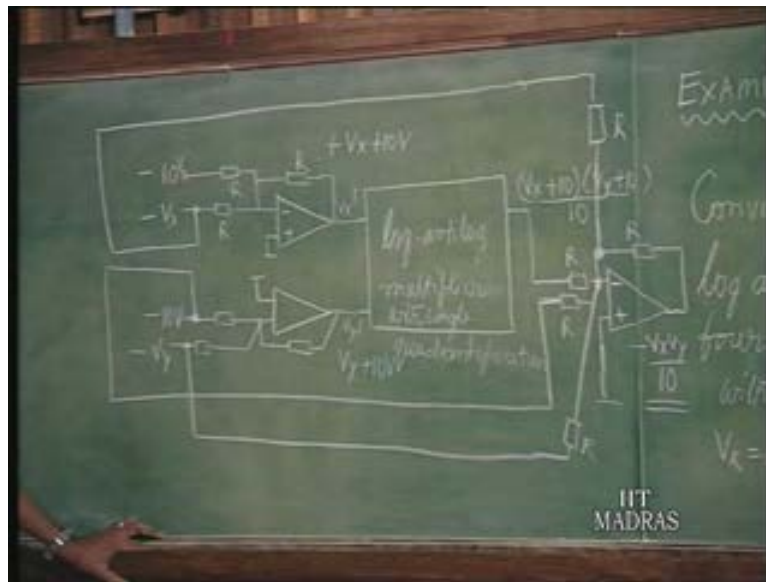
this, you have plus 10 volts. We are therefore subtracting minus 10 volts. So, if these are all R, R and R, that purpose is achieved already. So, the D C offset is already removed.

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Next, we have to remove V_x . We already have minus V_x here. So, that also can be added simply. So, it is a very simple circuit which is going to be giving us whatever we want, R at this node. Then similarly, we want to remove V_y , can also therefore put this R. So, that is the circuit, very simple circuit that will at the output now give... What will it give at the output? In fact, it will give you minus $V_x V_y$ by 10 volts.

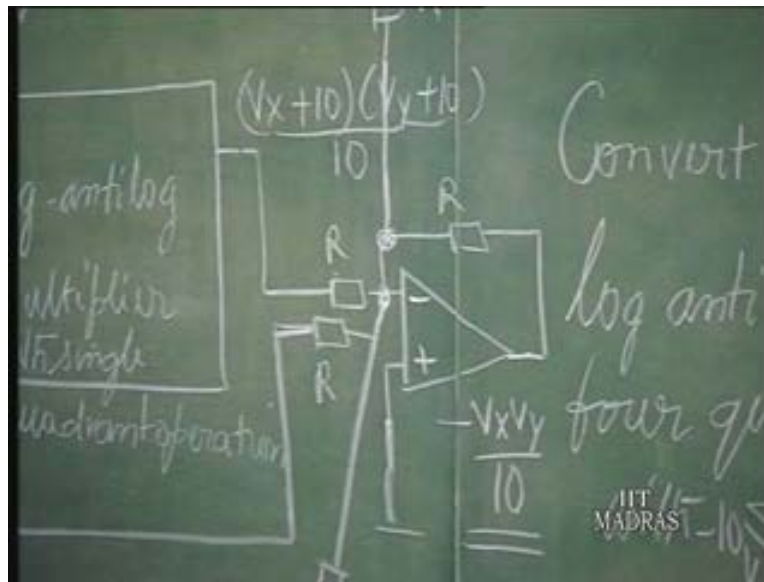
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If you are not happy with the inversion, you can put another inverter and get rid of that; but that is not...because basically, this is a four quadrant multiplier, whatever be the polarity of V_x and V_y . We have not really given now any polarity to V_x and V_y .

So, it is...it is just simply that, if this is minus V_x and this is minus V_y , this will be minus $V_x V_y$ by 10. If this is plus V_x and this is plus V_y , which could as...you can as well call that, then this will be still minus $V_x V_y$ by 10. So, it does not make any difference.

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So, this is a four quadrant multiplier conversion using single quadrant multiplier as the basic building block.

This is a commonly adapted technique and the dynamic range remains the same as what we want: plus minus 10 volts. So, this is a precision multiplier which can be used up to hundreds of Kilo hertz. Primarily, the frequency limitation is due to these op-amps which are not readily available for very high frequencies. So, up to hundreds of Kilo hertz, if you want to design a very good precision multiplier, this is the technique. This is very cheap.

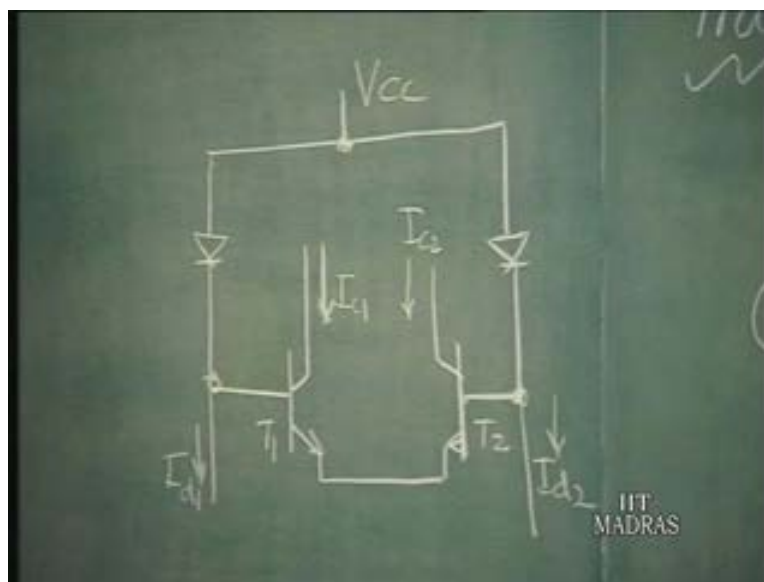
Let us now discuss another important popular multiplier. This is available also in IC form. This is called transconductance type multiplier; or actually, the basic idea, even it is from what is called Gilbert's gain cell. We will discuss what this Gilbert's gain cell is. This uses a very important principle called translinear principle in bipolar transistors.

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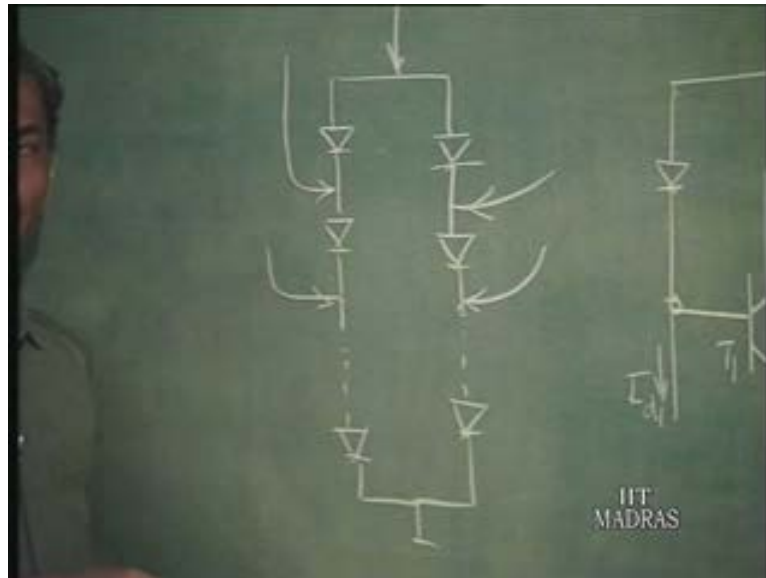
What is that translinear principle? The Gilbert gain cell is given here. This is a very important cell.

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This comprises junctions, base emitter junctions or diode junctions, forward biased; but forming a loop. So, this translinear principle is applicable to any loop formed by forward biased diodes. It could be just simply this...just... I have so many diodes, let us say, with

some kind of currents coming in here and may be current coming here also. So, suppose we have a string of diodes all of them form a loop, let us say.



Then the Kirchhoff's voltage law is valid here. That the total voltage in this is zero; summation of all the voltages in this should be equal to zero. What is required in this translinear principle is number of diodes connected in the clockwise manner; let us say these are all clockwise forward biased; these are anti-clockwise forward biased. These numbers should be the same.

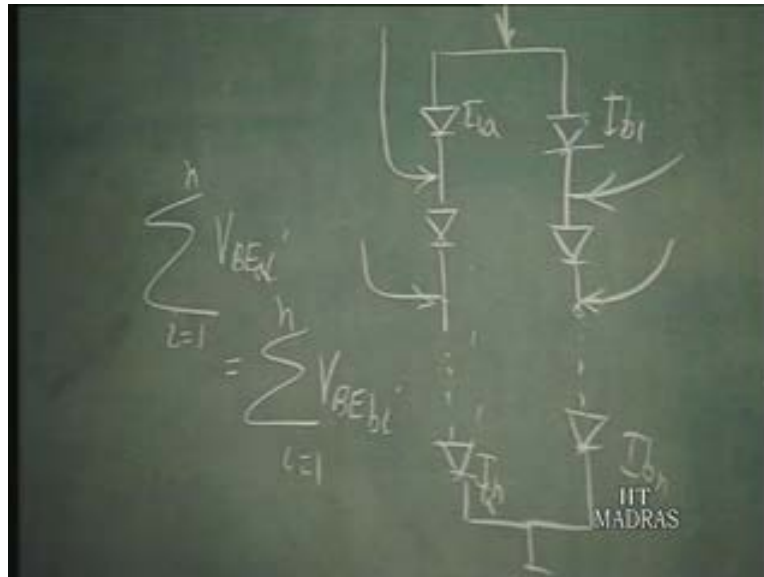
If that is the case, then the product of the currents in each of the diodes, let us say, this is I_1 up to I_n and this will be, let us say, I_0 up to I_n . The product of the current of these anti-clockwise connected diodes is the same as the product of the currents in this.

This can be easily proven because summation of sigma of all these voltages should be equal to zero. That means the forward biased diodes in clockwise direction should have the voltage equal to the forward biased diodes in the anti-clockwise direction.

Therefore we have, let us say, n number of diodes. So, I is equal to 1 to n . V_{BEi} should be equal to, let us say $V_B I$ of this... We will call this 'a' for clarity and this as 'b' so that

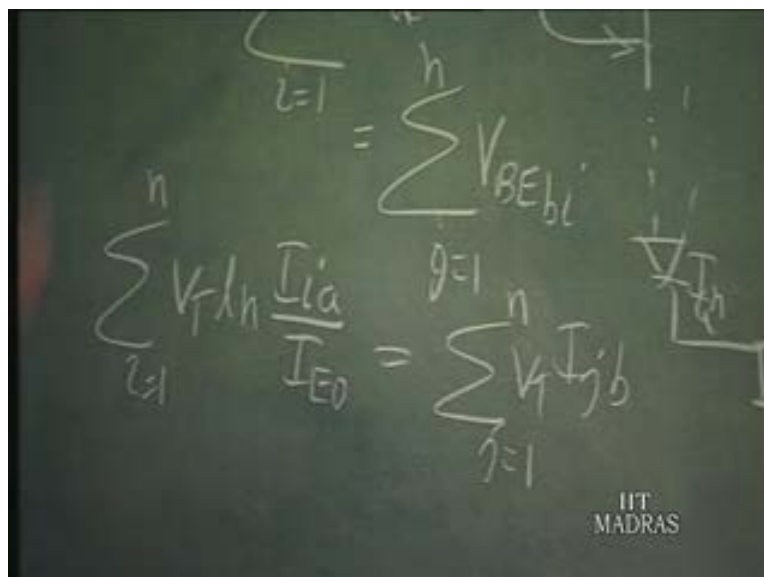
those are which are 'a' should be same as V_{BE_i} . i is equal to 1 to n . This is from Kirchhoff's law.

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So, once these sigmas are same, we know that this is same as $V_T \log$. These VBEs are same as $V_T \log$, corresponding currents which we are calling I_1, I_2, \dots, I_n by I_E naught; and this is also equal to $\sum V_T \log I_j$. Let us say we call it j , j is equal to 1 to n .

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So, these V_T s get cancelled... $V_T \log I_j$ by I_E naught. These V_T s get cancelled.

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The chalkboard shows the following derivation:

$$\sum_{i=1}^n \ln \frac{I_{i,c}}{I_{E0}} = \sum_{j=1}^n \ln \frac{I_{j,b}}{I_{E0}}$$

Below the second equation, there is a diagram of a BJT base-emitter junction with a voltage V_{BE} and a current I_{E0} entering the emitter. The text "IIT MADRAS" is visible in the bottom right corner of the chalkboard image.

Logarithm of sum of these products...sum of these, is equal to product itself. Product. i is equal to 1 to n - is same as log... So, that means product of... j equal to 1 to n .

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The chalkboard shows the following derivation:

$$\prod_{i=1}^n \frac{I_{i,c}}{I_{E0}} = \prod_{j=1}^n \frac{I_{j,b}}{I_{E0}}$$

The text "IIT MADRAS" is visible in the bottom right corner of the chalkboard image.

This will give you 1 over $I E$ naught to the power n . This also will give you 1 over $I E$ naught to the power n . So, this is the basic principle, translinear principle; very important.

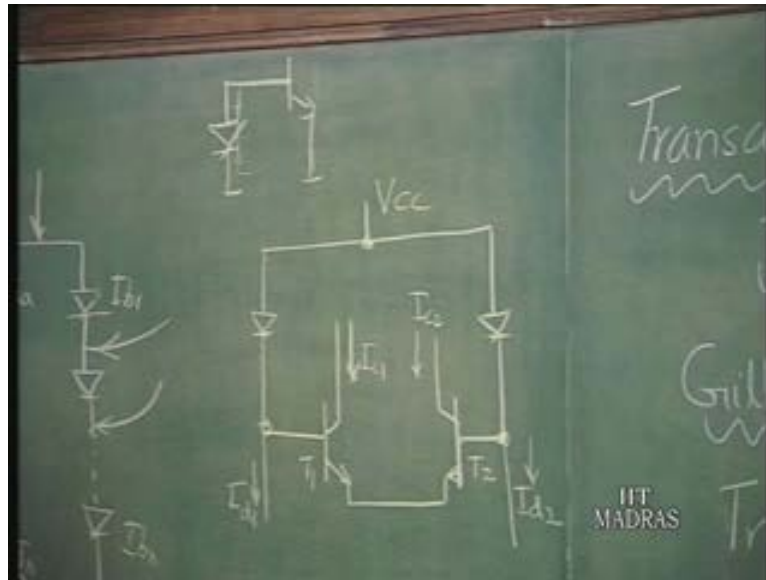
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What it simply says is that if there is any loop, close loop formed of n number of diodes in clockwise direction, n number of diodes forward biased in the anti-clockwise direction, then the current flowing through the clockwise direction diodes, product of these, will be equal to current flowing through the product of the diodes, which are in the anti-clockwise direction.

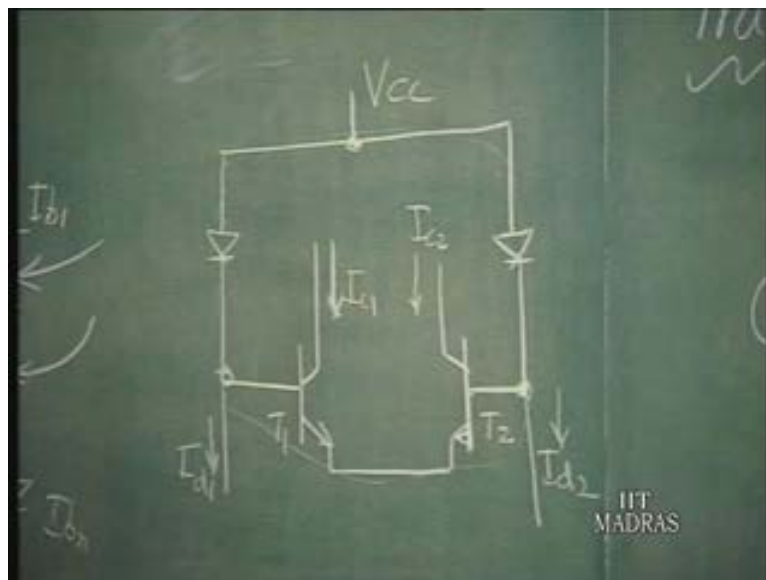
Let us apply it simply to...for example, a current mirror. A current mirror is the first example. For example, one diode with another junction. So this current in this should be same as this current; that single diode. So, that is the basic principle of translinear this thing applied to a pair like these.

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Now here, this is slightly more complicated. We have two diodes and two junction transistors connected in a loop.

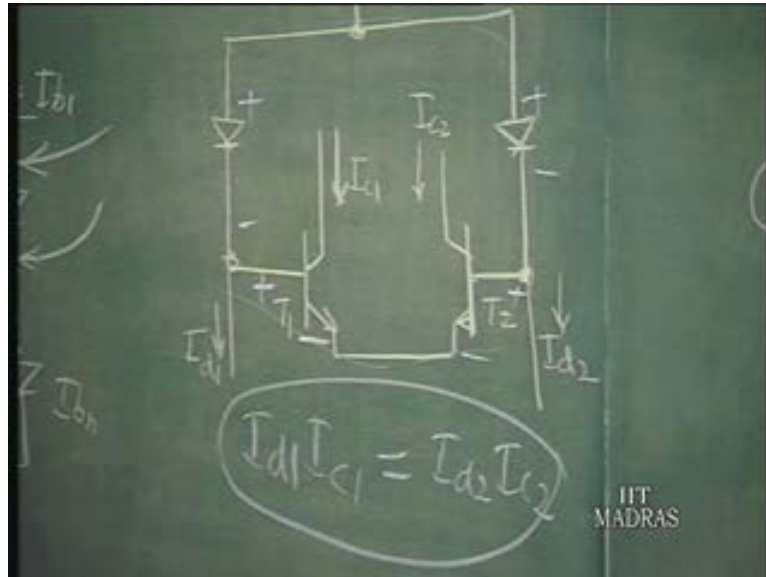
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So, according to this now, these are, let us say diodes which have one polarity; and these are diodes which have another polarity. The current through these diodes, product of these, should be same as the current through these junctions. That means, actually

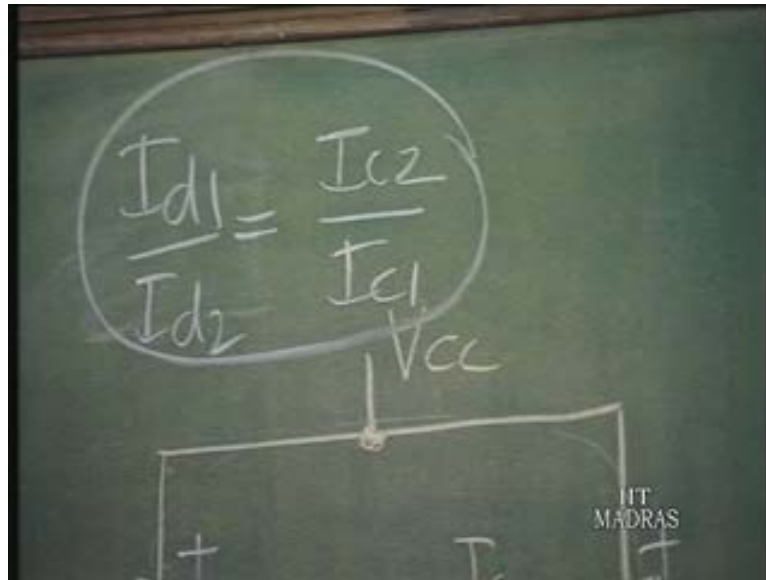
speaking, you can now see that I_{d1} is the current through this. So, I_{d1} into current through this is essentially I_{c1} , because it is I_{E1} which is very close to I_{c1} . This is equal to I_{d2} into I_{c2} .

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This is what the Gilbert's gain cell says. Product of the current of the diode into this transistor, corresponding transistor, is equal to product of the current of this diode into this transistor; or $I_{d1} I_{c1} = I_{d2} I_{c2}$.

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This is valid over a wide range of variation of current because this is not a small signal thing. We have assumed large signal property for the transistor, exponential relationship; and that relationship is valid for almost six decades of variation of current.

And therefore, this is a very powerful signal processing aspect which has been used in many applications of integrated circuits. But now, we would like to use this for multiplier. You can see here. Here already, current multiplication is taking place. I_{d1} by I_{d2} into I_{c1} is equal to I_{c2} . Or, we can see here that I_{d1} minus I_{d2} divided by I_{d1} plus I_{d2} equals I_{c2} minus I_{c1} by I_{c2} plus I_{c1} .

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Trans linear

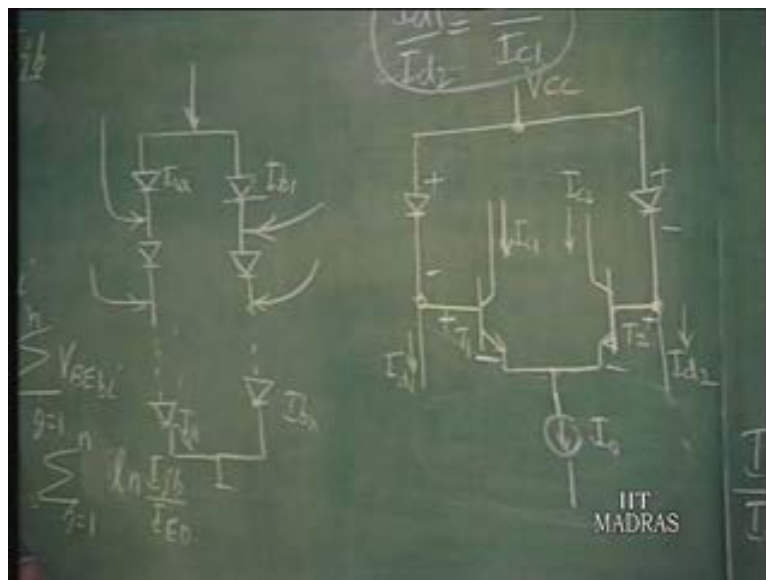
$$\frac{I_{d1} - I_{d2}}{I_{d1} + I_{d2}} = \frac{I_{c2} - I_{c1}}{I_{c2} + I_{c1}}$$

nBJTs

IIT MADRAS

I can make these two currents equal a constant current. That is the Gilbert's gain cell; a constant current I_{naught} ; force the current to be constant.

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So, that means I_{c2} plus I_{c1} is equal to I_{naught} . So, I_{d1} minus I_{d2} - the differential input current, divided by I_{d1} plus I_{d2} - the common mode input current, twice that, into I_{naught} which is a D C current is equal to I_{c2} minus I_{c1} . This is the basic principle of Gilbert's gain cell.

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Trans linear

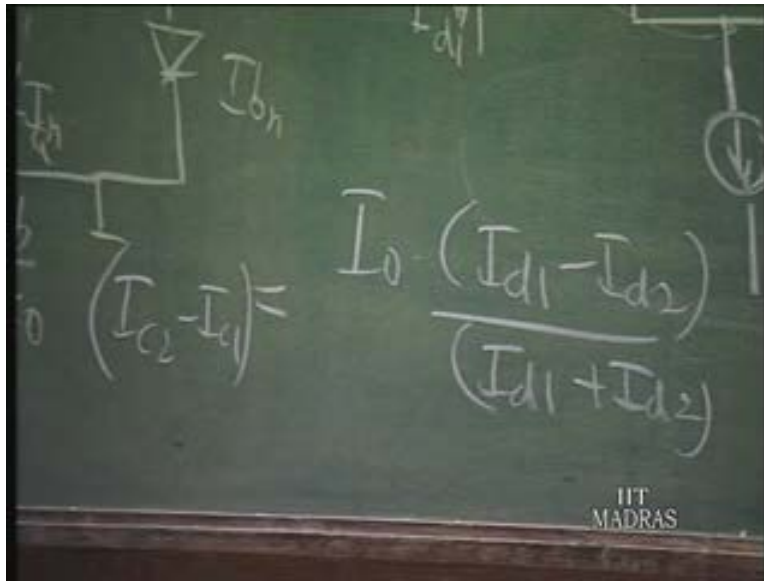
$$\frac{I_{d1} - I_{d2}}{I_{d1} + I_{d2}} = \frac{I_{c2} - I_{c1}}{I_0}$$

nB JTs

IIT MADRAS

I_{naught} into I_{d1} minus I_{d2} divided by I_{d1} plus I_{d2} equals my differential output current, I_{c2} minus I_{c1} .

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If I select currents I_{d1} and I_{d2} such that it has a common mode current which is a D C current, and a differential mode current which is the signal current...how do I do it?

I can make I_{d1} equal to, let us say I_{naught} ; a D C current by 2 plus, let us say I_{\dots} let us say ΔI_i by 2, input current, differential current; and I_{d2} equals I_{naught} by 2. This is the common current which is common to both; minus ΔI_i by 2...

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You can see here, I_{d1} plus I_{d2} will have this getting cancelled. So, it will be simply I_{naught} , D C current. I_{d1} minus I_{d2} will have this getting cancelled; and it will be simply ΔI .

This is how we had represented common mode current, common mode voltage and differential mode voltage in difference amplifiers. Same way, any two currents can be represented as a common current and differential current, a common current and a differential current. So this one, I_{d1} is equal to I_{naught} by 2 plus ΔI by 2; I_{d2} is equal to ... Then, what happens to this? This becomes I_{naught} ; I_{d1} minus I_{d2} is ΔI . That is the differential input current. I_{d1} plus I_{d2} is simply I_{naught} .

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This is of great significance because you can see, I_{naught} is a D C current, I said. Suppose this is 1 milliamperes and I_{naught} is 10 milliamperes. You are getting a gain of 10 for the current amplifier as the output differential current. This is the input differential current. Output differential current is simply 10 times input differential current. This is unique in this because such constant gain, we could only obtain in other schemes by giving negative feedback. This is having no negative feedback. This is independent of temperature, active device, anything. This is dependent purely on the current ratios.

How can I get current ratio like that? I use current mirrors. Let us say 1 milliamperes current mirror, I use ten times in shunt, I get 10 milliamperes. So, it will be an absolute constant independent of temperature and all that.

So, we can get current gain without any effort and these are all of what are called wide band current amplifier circuits. That is why this Gilbert gain cell is very famous today as a basic building block for current amplifiers.

Here, the voltage never changes above V_{BE} . All these voltages are V_{diode} voltages and therefore the capacitors need not be charged to large voltages. That means time taken for operation of this circuit is very small. That means these are all high speed circuits.

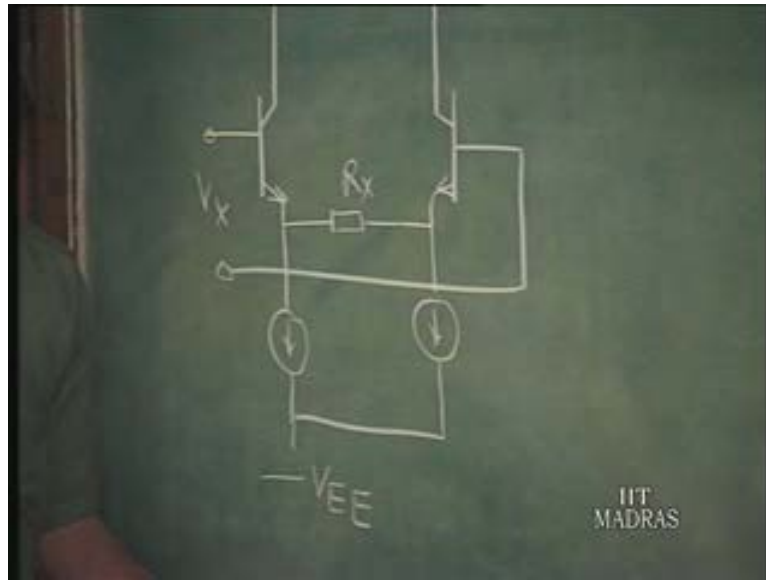
So, these circuits are nowadays being used as wide band amplifiers with constant gain and you can reach the required gain by simply cascading such structure, because this differential input could be the input to the next stage, which looks exactly identical. Only thing is the operating current of that is, let us say, 10 times more than this.

So, you can put one structure over this other structure. That is why it is called a cell. So, the next stage will be having two other diodes connected to same V_{cc} with this as input now. This has now, as you see, a differential input and a common mode input; the common mode input is nothing but I_{naught} .

So, this can become the input in the next stage and that will be exactly looking like this with this current operating at a higher value. That much should be sufficient for Gilbert's gain cell. Now, how to use this for multiplier is something that we have to discuss.

This circuit as is shown here is the circuit which is able to convert a voltage into differential input current required for the Gilbert's gain cell.

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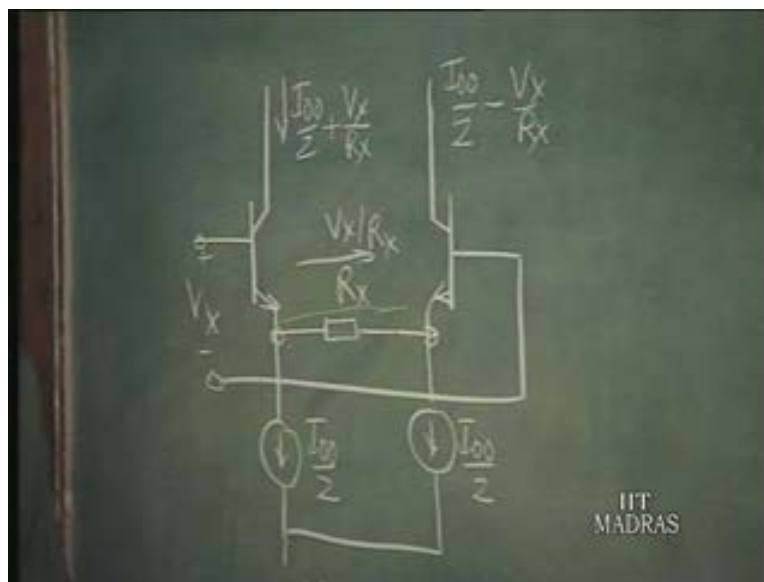


After all, most of the signals that are available to us are going to be voltages. So, even though this Gilbert's gain cell tells us that the output differential current is input differential current into I_{in} by I_{out} , there is some kind of multiplication taking place in terms of currents. But, we would like this to happen in terms of voltage. So, we need a voltage to current converter; but that voltage to current converter should be voltage to differential current converter which is required as input to these gain cells, I_{d1} and I_{d2} . How to do that?

This is called a transconductor block. This does it beautifully. You can look at it. V_x is the input. We have here a current which is going to be, let us say, I_{D1} . That is the common mode current, constant current and this is linking the two emitters. You have a resistance R_x . So, what happens now?

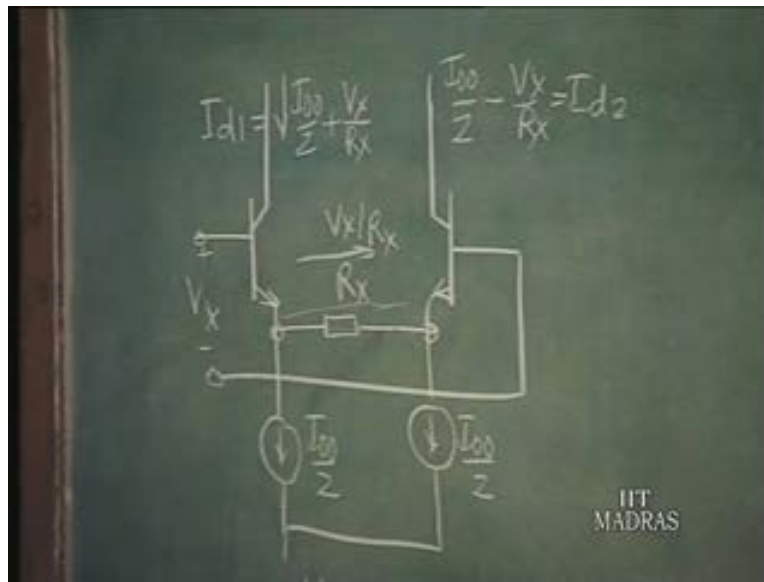
This current is I_{D1} and this current is going to be V_x . V_x will come across this R_{e1} , R_x , R_{e2} . If you neglect this R_{e1} and R_{e2} , this V_x will directly come across R_x . You can select R_x such that it is large compared to R_{e1} and R_{e2} . Then the current in this is V_x divided by R_x . So, the total current here is I_{D1} plus V_x by R_x ; and the current in this is I_{D1} minus V_x by R_x .

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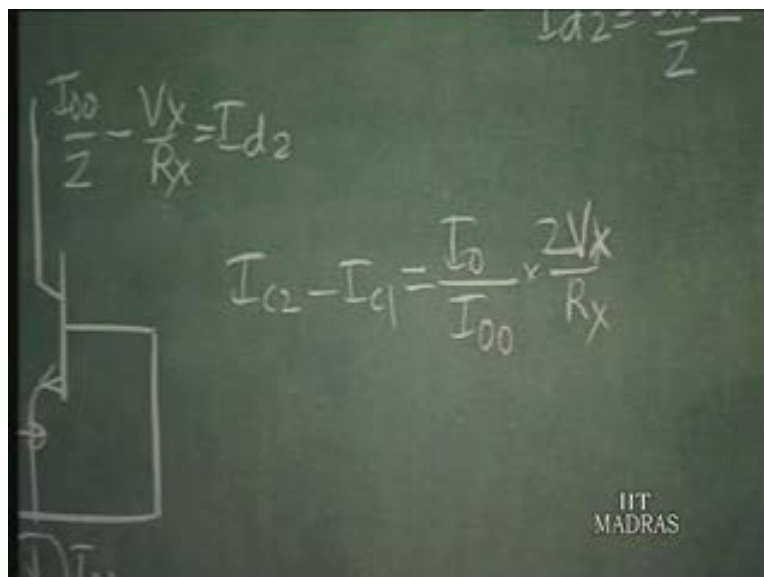
So simply, we get a linear transconductor here which converts a voltage into what we want - a constant current with signal current equal to V_x by R_x added to it; another constant current with signal current V_x minus R_x deducted from it. That is exactly what we want as the input to the cell here - I_{D1} and I_{D2} , so that this be I_{D1} and this be I_{D2} ; inputs to these. Then what happens?

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We now know that output which is I_{c2} minus I_{c1} equals I_{naught} divided by the... I_{naught} divided by I_{naught} naught, because it is I_{d1} plus I_{d2} into ΔI_i which is nothing but V_x , twice V_x by R_x . This is ΔI_i by 2. This is minus ΔI_i by 2. So, ΔI_i is twice V_x by R_x . So, we are able to now get V_x here. The differential output current is directly dependent upon V_x now; and we want it to be multiplied by another voltage. How...What we can do?

(Refer Slide Time: 46:26)



Obviously, there is only one choice. I_{naught} has to be dependent upon another voltage. Let us say that I_{naught} is really equal to I_{naught} by 2 plus V_y by some R_y .

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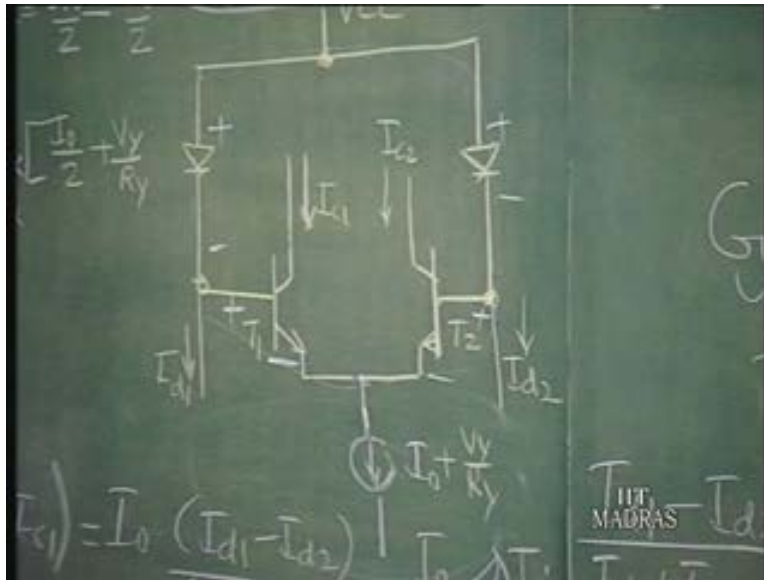
The image shows a chalkboard with handwritten mathematical equations. The main equation is:

$$I_{c2} - I_{c1} = \frac{2V_x}{R_x} \left[\frac{I_0}{2} + \frac{V_y}{R_y} \right]$$

There are also some scribbles and a small diagram on the right side of the board, including the text "IIT MADRAS" and a small circuit diagram with a current source I_{d1} .

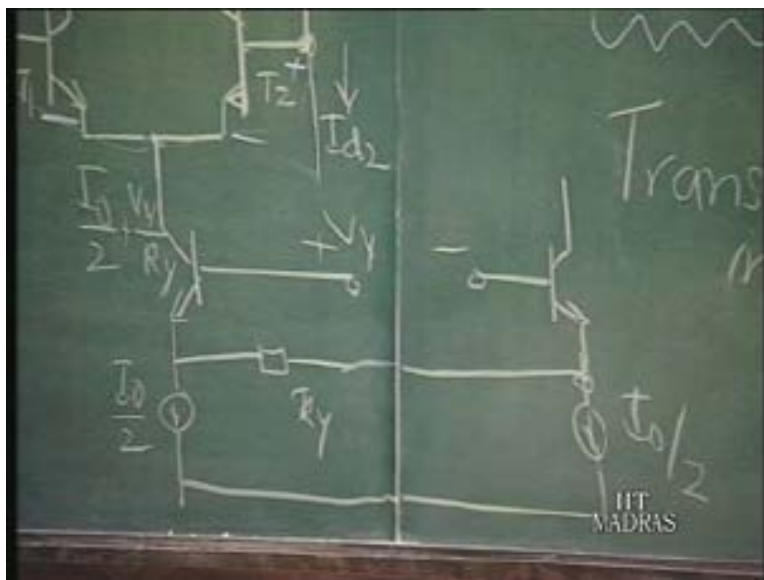
Just as we had here, a voltage to current converter, we can have voltage current converter there also. Only thing is it will be V_y here and R_y there. So, that can generate a current which is in one side I_{naught} by 2 plus V_y by R_y . So, this current can be generated. Instead of therefore a current source of I_{naught} , I will simply put I_{naught} plus V_y by R_y there; a current source. How do I get that?

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That can be got by putting here the same thing R_y , I will put; and then I naught by 2, I naught by 2. So here, I get...if I put V_y here, I naught by 2 plus V_y by R_y .

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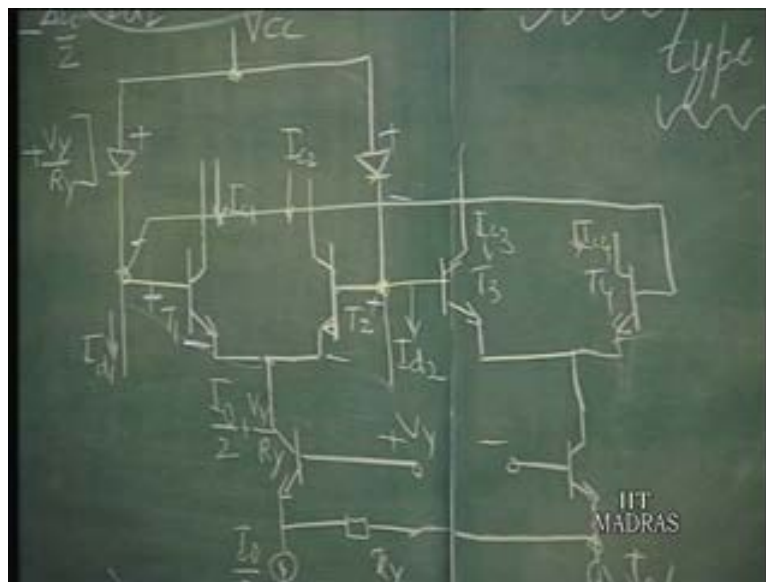


So, you have this being connected here and this current source. So, you have a multiplier component here in this; differential output current, you have this. What to do with that?

That can be applied to another one which is also connected to same pair, similar pair, like this. This same input can be given to another pair like this.

So, this is going to be taken here. That means, this is also going to have similar ratios for the current because same input is being given. So, we will call this T 1, T 2, T 3, T 4. The current in T 3 and T 4 will be, let us say, I_{c3} and I_{c4} . So, these ratios will be exactly similar to what we had as I_{d1} by I_{d2} .

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So, we will have this equal to, let us say, I_{c2} minus I_{c1} here. I_{c2} minus I_{c1} is similar to I_{c3} minus I_{c4} . I_{c3} minus I_{c4} , divided by I_{naught} naught R_x twice V_x . Only thing is here, it will be I_{naught} by 2 minus V_y by R_y because this current, source current, is different.

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$$I_{c2} - I_{c1} = \frac{2V_x}{I_{00} R_x} \left[\frac{I_0}{2} + \frac{V_y}{R_y} \right]$$

$$I_{c3} - I_{c4} = \frac{2V_x}{I_{00} R_x} \left[\frac{I_0}{2} - \frac{V_y}{R_y} \right]$$

So, you can see here that this whole arrangement, we have the product that is got; but only trouble is that the...there is some feed through component of V_x here. So is the output here.

So, that can be simply got rid of by subtracting this from this. So, this differential current can be subtracted. That means $I_{c2} - I_{c1} - I_{c3} + I_{c4}$ therefore becomes equal to... these two will get cancelled. We will get twice V_x by $R_x I_{00}$ into... What is this? Twice V_y by R_y .

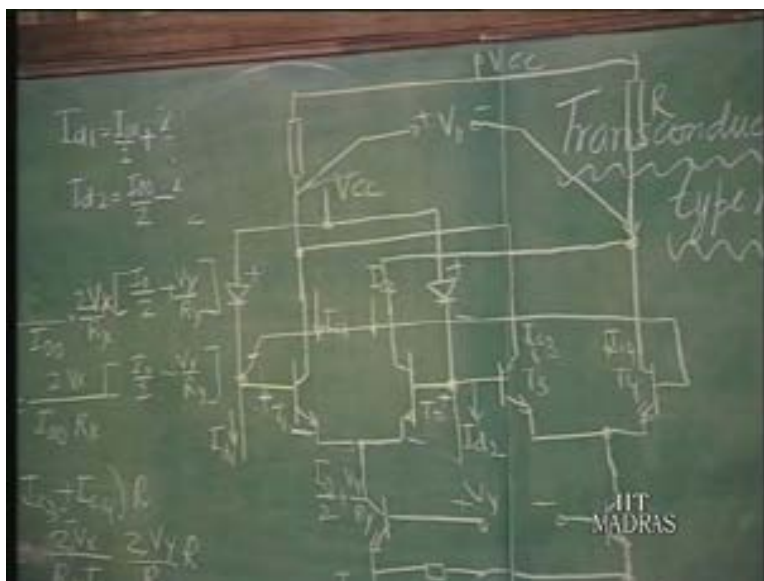
So, you will get here $4 V_x V_y R_x R_y I_{00}$, which is the product of two voltages; that as the current. This can be converted into voltage by multiplying this whole thing by a resistance R . So, how do I do that?

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$$(I_{c2} - I_{c1} - I_{c3} + I_{c4}) R = \frac{2V_x}{R_x I_{s1}} \frac{2V_y R}{R_y}$$

I_{c2} plus I_{c4} , I_{c2} plus I_{c4} simply can be done by connecting those two together. This is I_{c2} plus I_{c4} , node. Then, I_{c1} plus I_{c3} - that is going to be these two currents. So this current is going to be I_{c1} plus I_{c3} and make these flow through resistances R and connect it to V_{cc} and take differential output voltage V_{naught} . That is going to be nothing but this.

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So, this is called a four quadrant multiplier because V_x and V_y , both could be positive or negative. So, this is the complete transconductance multiplier which is available as an IC. We will discuss the application of this and variations of this circuit in the next class.