

Electronics for Analog Signal Processing - II
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Lecture - 7
Operational Amplifier in Negative Feedback Structures

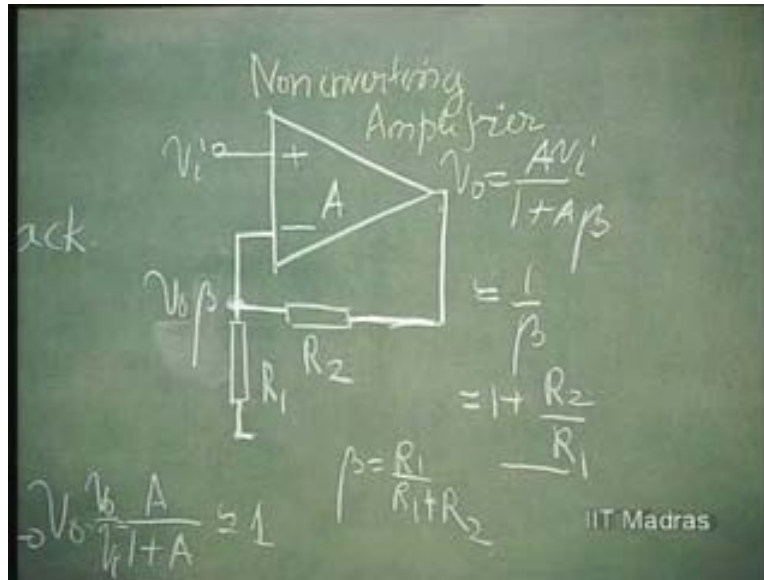
We had started discussing about negative feedback structures in op amp. First, we gave full output feedback, negative feedback; and then we got V_{naught} equal to V_i . V_{naught} equal to A by $1 + A$, A being very large; V_{naught} is very nearly... V_{naught} over V_i , this is V_{naught} over V_i ; very nearly equal to 1. Buffer, it is called; unity gain amplifier.

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Another one where we sampled V_{naught} ; this was V_{naught} into R_1 by $R_1 + R_2$, where β was R_1 by $R_1 + R_2$, definition. So, β times V_{naught} was fed back. Therefore, ultimately, according to us, V_i should be equal to β times A V_{naught} . This voltage should be zero, if it is working at finite output situation. So, we saw that according to equation $A V_i + \beta A V_{naught}$ was V_{naught} ; this was very nearly equal to 1 over β . This was equal to $1 + R_2$ over R_1 . Therefore we can design a non-inverting amplifier of gain $1 + R_2$ over R_1 which is 1 over β .

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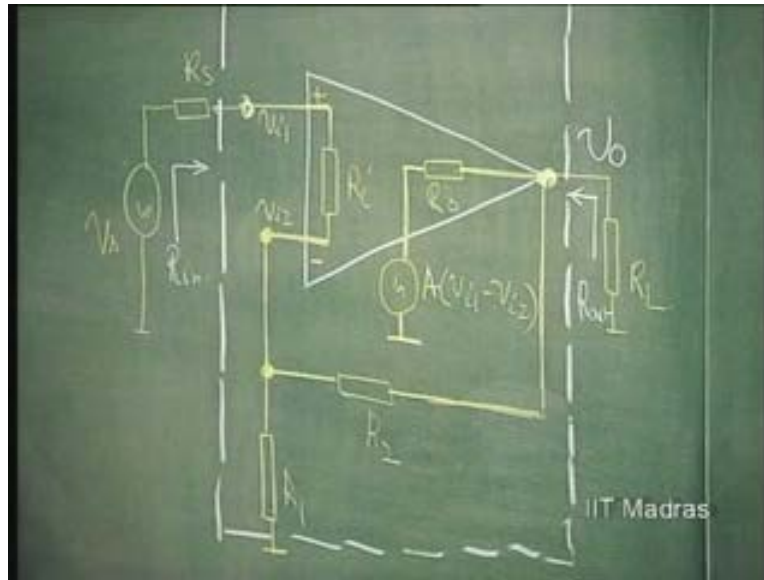


So, this is done by applying h feedback. So now, we will go into the two port parameter technique that we have used. Now, we will introduce all the non-idealities associated with op amp.

First we said, op amp is a structure with forward transfer parameter very high. So, A was tending towards infinity in the g matrix of this. The other three parameters were zero. But now, the other three parameters are not zero. They are finite. That means finite input impedance, finite output impedance and finite non-infinite gain. So, when we consider such an op amp, that means, such an op amp equivalent we can get for any configuration of cascaded amplifier. This we know how to obtain.

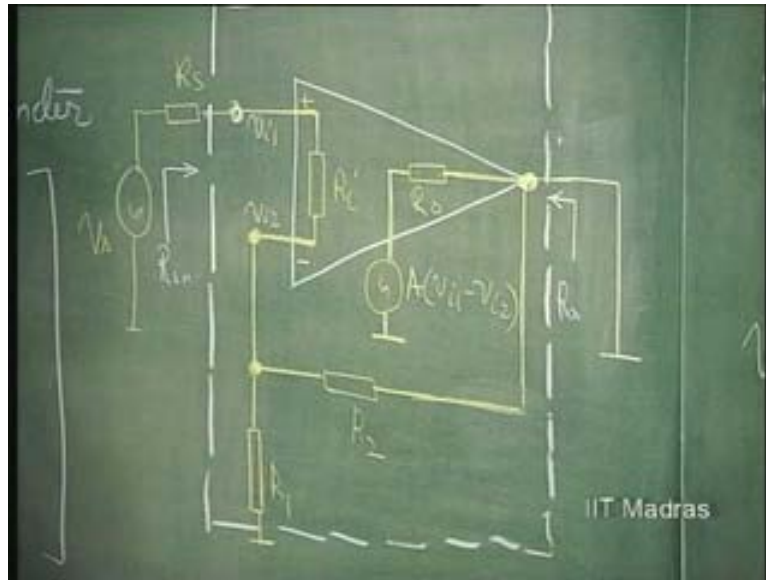
Once you obtain this and then give a h feedback using a passive network R 1 and R 2, this R 1 R 2 passive network, samples the output, feeds back Beta times V naught or R 1 by R 1 plus R 2 times V naught at this point, as the feedback voltage. Now, under that situation, what happens, in an actual situation?

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So, we would like to apply now, h parameter. Or a voltage control voltage source analysis with h feedback, we would like to use h parameter. So, composite h parameter we will write. So, h_i and h_f we get by short circuiting the output. So, we short circuit the output. Then you can see that the feedback comes out of it and the feedback is in series at the input. You can see, this is the amplifier input; this is the feedback network. So, these two are coming in series with the actual input. So, it is shunt at the output and series at the input. So, the h parameter of the composite network is nothing but R_i .

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The input current flows through R_i and parallel combination of R_1 and R_2 , because R_2 is grounded. So, R_i plus R_1 parallel R_2 ; that is, h_i . Once again, h_i is nothing but the input impedance of the composite structure which is R_i of that amplifier and then R_1 parallel R_2 , that of the feedback network. These things simply add. So, it is very simple to evaluate this.

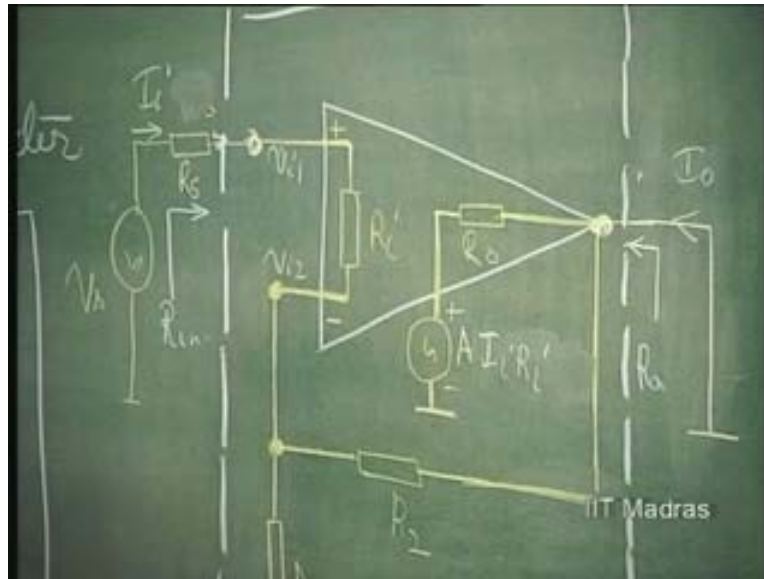
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$$R_i + \frac{R_1 R_2}{R_1 + R_2}$$

Next, let us evaluate the h_f which is the short circuit current gain. When the output is shorted, what is the current gain?

So, the current output I_o is defined now, under the situation of output being shorted. So, I_o is what is defined now, under the situation of output being shorted. So, if I_i is the input current, this I_i will flow through R_i and develop a voltage V_{i1} minus V_{i2} as I_i into R_i . So, this voltage is I_i into R_i because the current I_i is flowing through it. That means this is I_i into R_i ; V_{i1} minus V_{i2} is I_i into R_i .

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Next, if this is the voltage, what will be the current through the short circuit? $A I_i R_i$ divided by R_{naught} , but flowing in the opposite direction that we have assumed. So, negative sign indicating that it is actually flowing this way. So, A times R_i divided by R_{naught} ; this into I_i , divided by I_i is the current gain. That is the output current. This is not the only current. I_o has this current as well as... you can see. This input current comes like this and portion of the input current... What portion? R_1 by R_1 plus R_2 of the input current is also going out. That means minus R_1 by R_1 plus R_2 divided by I_i . So, that is the current gain.

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$$\left[-\frac{A R_i'}{R_o} - \frac{R_1}{R_1 + R_2} \right]$$

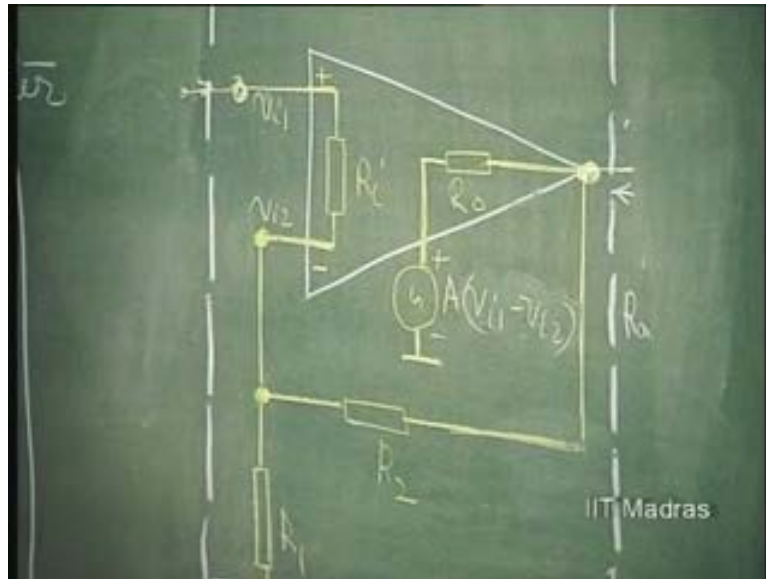
Once again, let us see. Going through the amplifier, this voltage is I_i into R_i ; and therefore, A times I_i into R_i is the voltage here and that will drive the current A times I_i into R_i by R_o in the opposite direction. So, minus... So, A times I_i into R_i into I_i divided by R_o divided by I_i . Here, I_i also has a part of the current going in the forward path here. I_i into R_1 by $R_1 + R_2$, flowing this way. So, these two are the parameters h_i and h_f .

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$$\begin{bmatrix} R_i + \frac{R_1 R_2}{R_1 + R_2} \\ -\frac{A R_i'}{R_o} - \frac{R_1}{R_1 + R_2} \end{bmatrix}$$

Next, we have to evaluate open circuit input. Input is open. **Input is open**. So, this source is removed. So, what happens? There is no current in this. That means this is inactive. So, there is $V_{i1} - V_{i2}$ equal to zero. So, this is not... So, R_{naught} is shunting this. Apart from that, R_2 plus R_1 is shunting that.

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So, this h_{oo} is $1/R_{naught} + 1/R_1 + R_2$. This is that of the amplifier output conductance. This is the feedback network output conductance.

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$$\begin{bmatrix} -\frac{AR_i'}{R_o} & -\frac{R_1}{R_1+R_2} \\ \frac{1}{R_o} & \frac{1}{R_1+R_2} \end{bmatrix}$$

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As far as feedback voltage is concerned, if I apply V_{naught} here, the only voltage that applies here, comes here, is R_1 by $R_1 + R_2$ times V_{naught} . So, R_1 by $R_1 + R_2$ times V_{naught} . That is h_r ; that is positive. So, we have simply written the composite h parameter of this fairly complex feedback network, where nothing is neglected.

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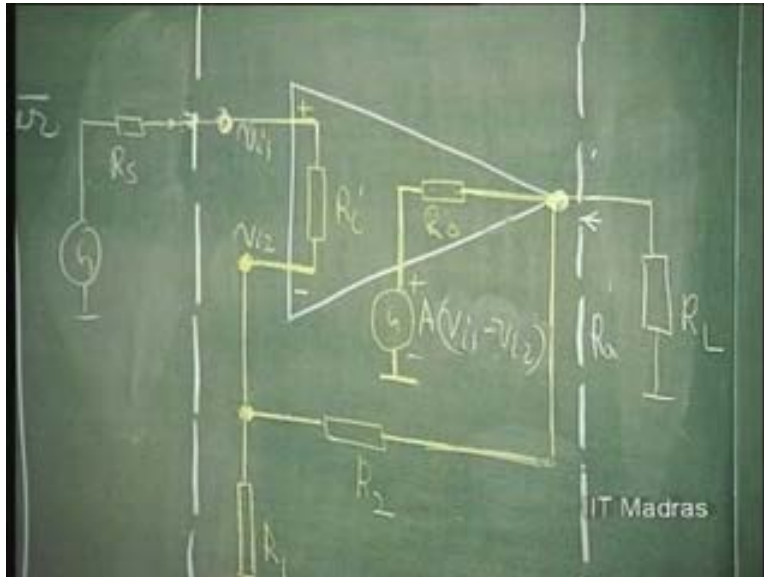
h-parameter

$$\begin{bmatrix} \frac{R_1+R_2}{R_1+R_2} & \frac{R_1}{R_1+R_2} \\ -\frac{AR_i'}{R_o} & -\frac{R_1}{R_1+R_2} \end{bmatrix}$$

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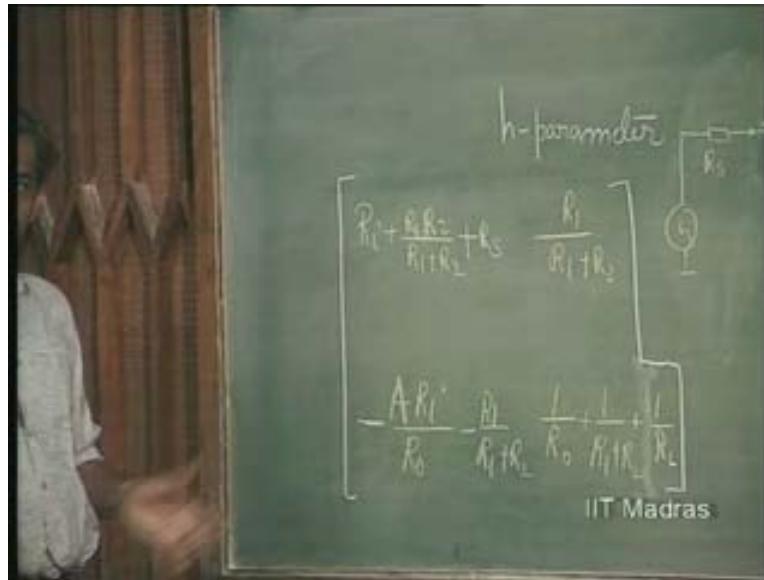
Now, if you include the source impedance here, this is the situation. Source impedance is coming in series with R_i and the load impedance in the case of h parameter always comes in shunt with the output impedance.

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So, this is the total situation where we are now considering also load impedances and source impedances. So, this is giving you the complete picture of a negative feedback situation with operational amplifier. Nothing is neglected. Now, of course, there is no point in keeping things which are things which can be neglected.

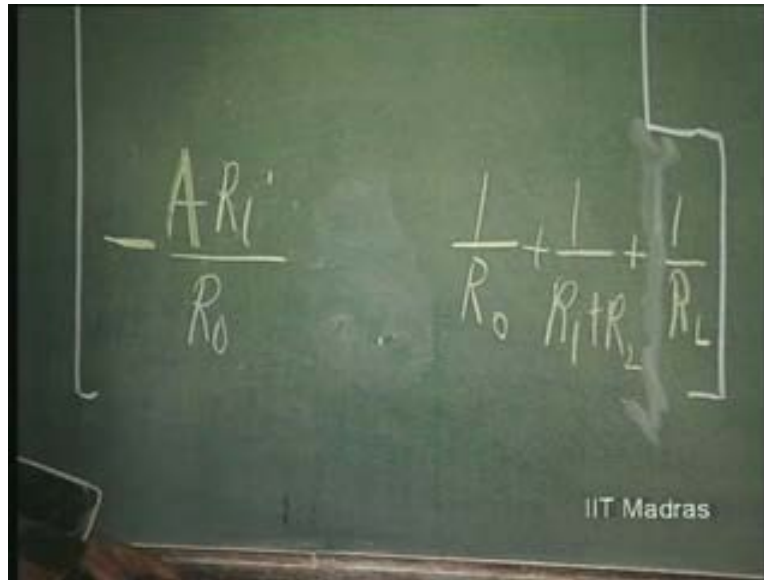
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Now, I would like you to come out with some definitions, practical definitions. See, what did we say about the forward transfer parameter here? Or, this is A which should have been infinity; R_i which should have been infinity; $1/R_{naught}$ which should have been infinity. So, if any... actually, A is infinity itself. That is sufficient to make this infinity; but we can see that the other parameters will make this a very huge value. So, having R_{naught} equal to zero and R_i equal to infinity and A equal to infinity means, this is, really speaking, infinity cube kind of thing. That is a high value; a third or a high value here.

So, this therefore is very huge in a practical op amp itself wherein A is any way high. R_i is going to be also high. R_{naught} is going to be very low. So, there is no point in retaining this, which is always a fraction. So, this can be ignored, compared to this, always.

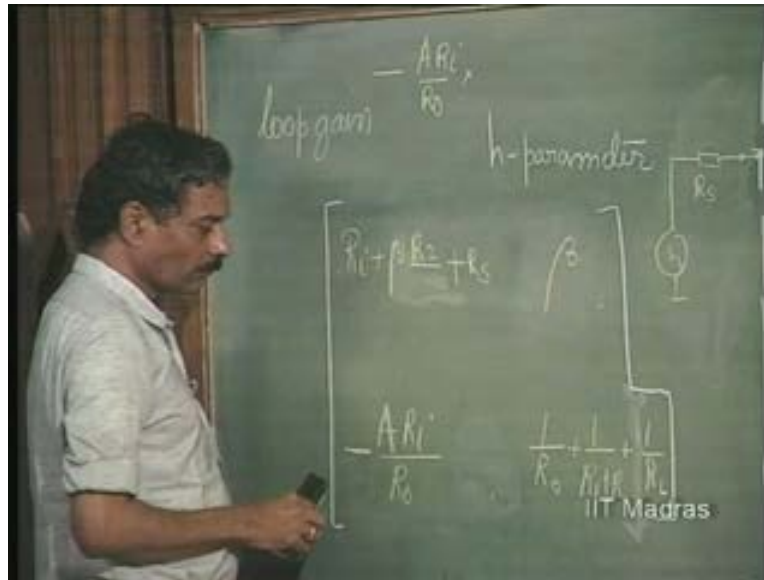
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$$-\frac{AR_i'}{R_0} \quad \frac{1}{R_0} + \frac{1}{R_1 + R_2} + \frac{1}{R_L}$$

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That means, the forward transmission parameter contribution due to passive device can be ignored. Here, the active device has not contributed to any reverse transmission at all. That is something that you have to remember. Only the passive device has contributed to the reverse transmission. So now, you can find out the loop gain. It is an important thing. This should be much greater than 1 and this should be negative for negative feedback; that you can verify. This is negative and this is positive. So, the loop gain is negative. This A into R_i by R_{naught} into, let us call this β ; because we have defined this R_1 by R_1 plus R_2 as β .

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So, $A R_i$ R_o naught into β divided by... Now you can consider this. This into this; R_i . Now R_i is normally very huge compared to βR_2 plus R_s . R_s is anyway going to be source resistance. Normally, R_i is going to be very high compared to βR_2 and R_s ; but then, we cannot... R_i plus R_s βR_2 . Here, normally, R_o naught is very low compared to R_1 plus R_2 and R_L .

So normally, this factor alone becomes significant. See here, this factor alone becomes significant. So, that is the actual loop gain.

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$$\text{loop gain} = \frac{-A R_i / R_o \times \beta}{(R_i + R_s + \beta R_2) \left[\frac{1}{R_o} + \frac{1}{R_1 + R_2} + \frac{1}{R_2} \right]}$$

$$R_i + \beta R_2 + R_s$$

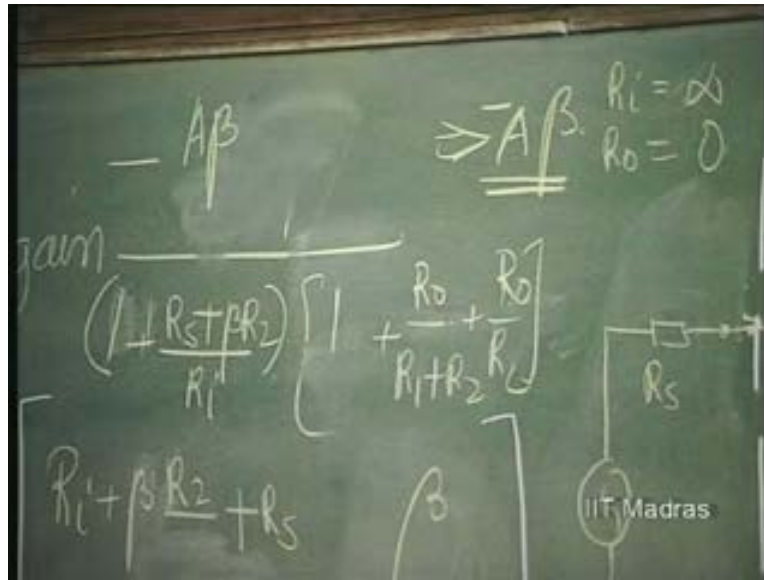
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I will rub it off. So you can see here... A, one thing that is supposed to be high; R_i which is very high, R_o is very low. That means this is infinity to the power 3 here. R_i which is high, R_o which is low; this is infinity square. So, loop gain is still very high.

So generally, this loop gain is going to remain very high and this R_i by R_o will get cancelled with this R_i by R_o ; and it is really A into Beta which we had earlier defined as the loop gain, there. A into Beta. So, you can see here. I will therefore take this R_i and take this R_o , retain the actual loop gain as minus A Beta; and how is it different from that? Divide R_i by R_i here; and here, multiply by R_o . So, you can see that it is the normal loop gain minus A Beta, under the situation, R_i is infinity and R_o is zero. You can put R_i equal to infinity here. This will go to zero. R_o - zero; this will go.

So, if this is minus A Beta, under the situation, R_i is equal to infinity and R_o equal to zero, the loop gain is equal to minus A Beta for R_i equal to zero, R_o equal to... R_i equal to infinity and R_o equal to zero.

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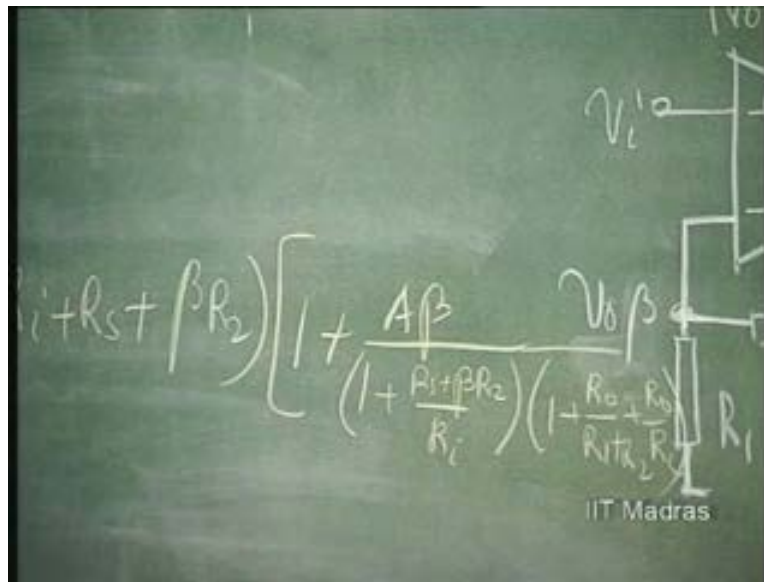


Otherwise, it is going to be dependent upon this R_S by R_i ratio in relation to 1. Similarly, R_{naught} by R_1 plus R_2 ratio in relation to 1. So now, what is the input impedance? What is the forward transfer parameter? All these things, we can now define. First, let us find out the input impedance. See, input impedance is going to increase over and above what? - the original input impedance. The original input impedance is R_i plus βR_2 plus R_S .

And the present input impedance will be 1 plus loop gain times the original impedance. This can be also found out by taking the matrix Δh as this into this plus this into this. Find out Δh and divide this by Δh . That is the input conductance. Instead, I have also told you that original input impedance gets modified by a factor of 1 plus loop gain. So, this is the original input impedance; R_i plus βR_2 plus R_S . So, that is getting multiplied by 1 plus loop gain.

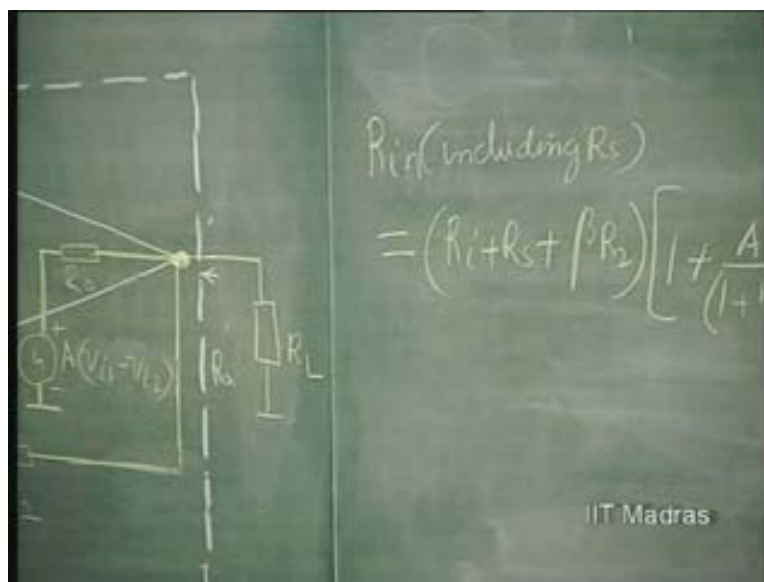
So, actual loop... input impedance R_{in} is R_i plus R_S plus βR_2 into 1 plus $A\beta$ divided by that factor. That is actually the input impedance. So, you can see that it is increasing very much. Input impedance seen from this side which is going to include R_S ... So, if you remove R_S , it will be input impedance without R_S .

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From this, you subtract R_s . That is the actual input impedance. So, R_{in} of the amplifier, really speaking, is this. So, this is including R_s .

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Now, output impedance. Once again, you can do it by this method. This one is to be divided by Δh , the matrix of this. That is the output impedance; or, original output impedance is this. That is, output conductance is this.

So, that has to be reduced by a factor of this. So, the conductance is increased by a factor of 1 plus loop gain. So, original output impedance - 1 over R out is going to be this... This is the original output conductance into the same factor in which you have to remove the effect of 1 over R L.

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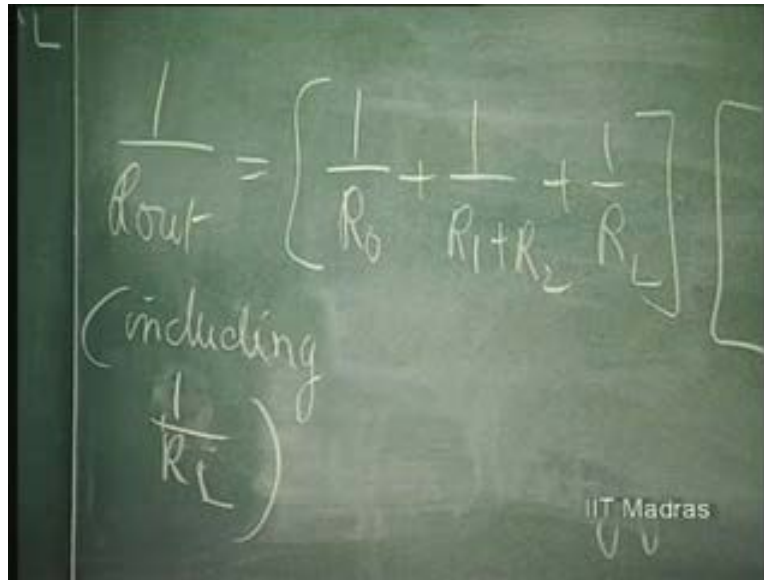
$$R_{in}(\text{including } R_s) = (R_i + R_s + \beta R_2) \left[1 + \frac{A\beta}{\left(1 + \frac{R_i + \beta R_2}{R_i}\right) \left(1 + \frac{R_o + R_L}{R_i \beta R_2}\right)} \right] R_i$$

$$\frac{1}{R_{out}} = \left[\frac{1}{R_o} + \frac{1}{R_i + \beta R_2} + \frac{1}{R_L} \right] \left[1 + \frac{A\beta}{\left(1 + \frac{R_i + \beta R_2}{R_i}\right) \left(1 + \frac{R_o + R_L}{R_i \beta R_2}\right)} \right] R_i$$

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This 1 over R L that is coming here so that actual output impedance... so, this is including shunting effect of R L.

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$$\frac{1}{R_{out}} = \left[\frac{1}{R_o} + \frac{1}{R_1 + R_2} + \frac{1}{R_L} \right] \left[\frac{1}{R_i} \right]$$

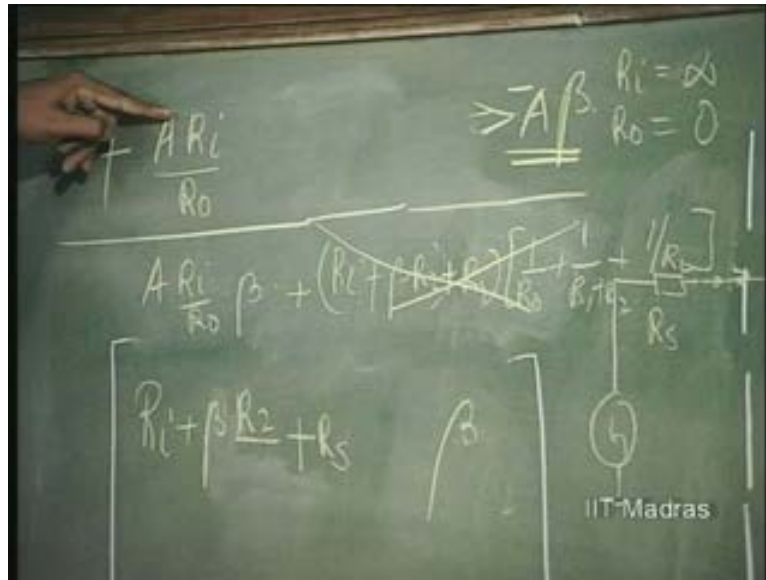
(including $\frac{1}{R_L}$)

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So, you subtract from this - 1 over R L. Then, you will get the actual output impedance. So, you see this, this conductance increases enormously. That means output impedance is brought down considerably. Now finally, the gain. This divided by the loop gain.

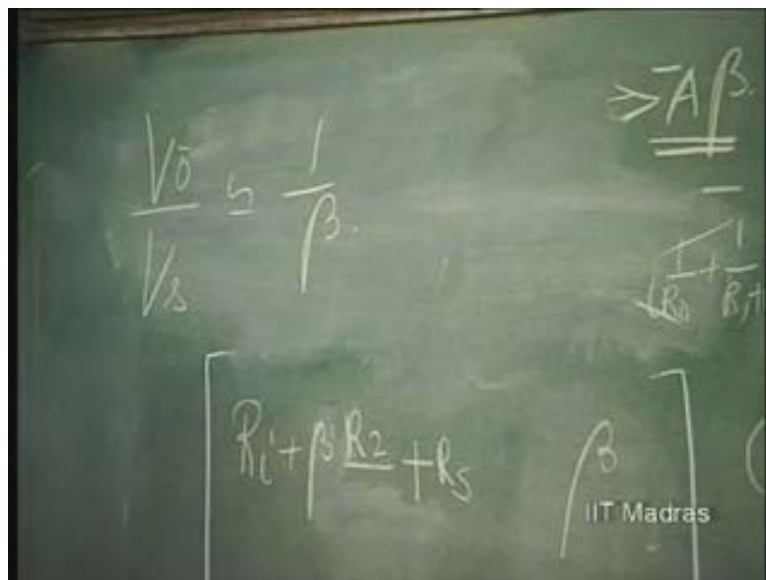
So, as far as this is concerned, this divided by Delta h. Delta h, you will see is nothing but this into this. That is going to cause only infinity square; but this into this is going to get added to it. So, Delta h has major part of it as A R i by R naught into Beta. This is infinite cube. This plus this factor into 1 over R naught plus 1 over R 1 plus R 2 plus 1 over R L. This is actually the... this is with plus. So, this is the forward transfer parameter out of which this factor is much less than this. So, this can be ignored. So, what do you see?

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This is simply becoming one over Beta. So, this factor really gets cancelled here. So, this becomes... this is nothing but V_0 naught over V_s . Please remember. This is nothing but V_0 naught over V_s .

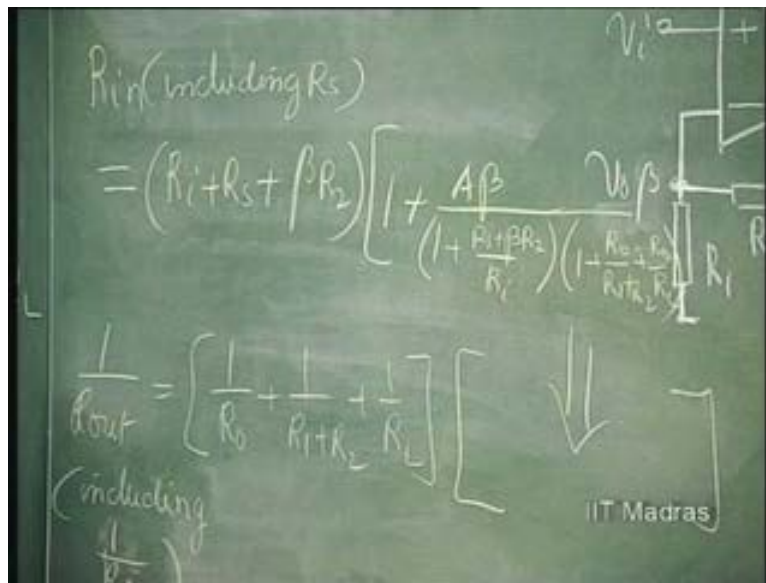
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This is... Loop gain, V_{naught} over V_s . So finally, we can say that, as far as the gain is concerned, it is very nearly equal to 1 over β ; and input impedance is equal to this. Output impedance is given by this. So, these are the exact values of the... actually g matrix; one is g_i . That is really g_i . This is g_{naught} . This is g_f .

So, these actually gives a very good idea as to how to select the value of R_1 and R_2 so that this approximation becomes valid. You can see that if R_i is known to you, then you can select this R_s and βR_2 such that this is predominantly determined by R_i . Here also, you can... if R_{naught} is known to you, R_1 plus R_2 and R_L can be so selected that this becomes negligible compared to 1 over R_{naught} .

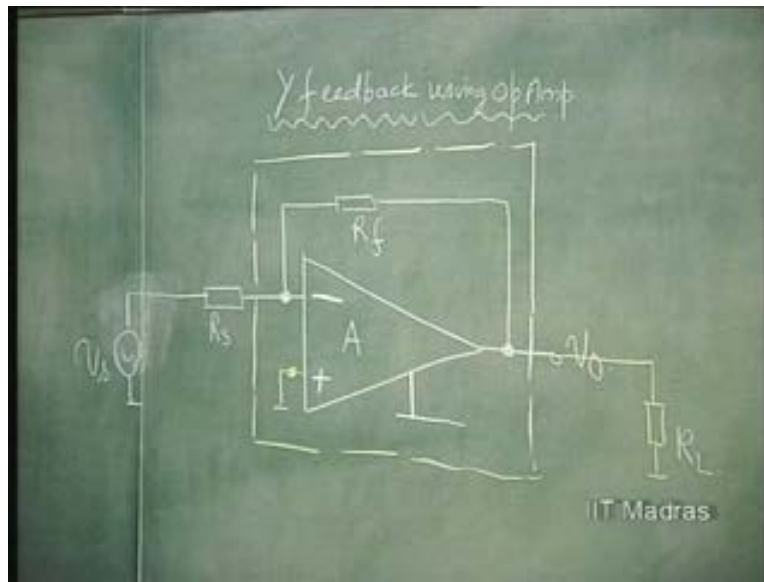
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So basically, R_i gets multiplied by 1 plus $A\beta$; R_{naught} gets divided by 1 plus $A\beta$; and A gets divided by 1 plus $A\beta$, if R_i and R_{naught} were to be made respectively infinity and zero.

So, this concludes the discussion about h feedback. The next circuit that we have discussed, as far as this is concerned, is the Y feedback which is the only other negative feedback possible with operational voltage amplifiers.

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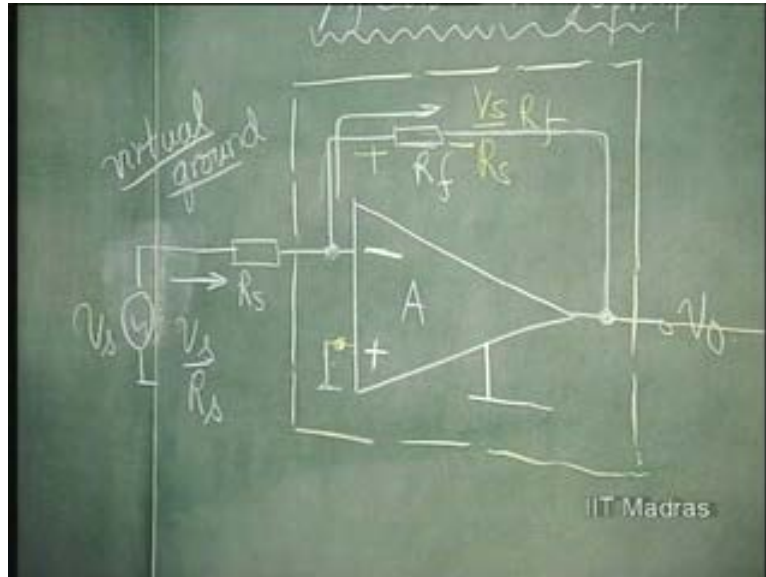
Now, let us consider Y feedback as applied to the operational amplifier, negative feedback. So, we have this op amp. The feedback is from the output; shunt at the output. That means output voltage is common to both amplifier as well as the feedback network. Shunt at the input; again, the input is...voltage is common to both the amplifier as well as the feedback network.

So, the feedback network is R_f , a single resistor, from... connected from output to input. Output - it is coming in shunt; input - it is coming in shunt. So, this is shunt, shunt feedback or called Y feedback. Now, simple way of analyzing this is... As I told you, if A were to be infinity, if A is infinity, we know that this is grounded; and this is a nullor. We have introduced this equivalent earlier also. So, this voltage is zero. Why? Because, if this is finite, V_o by A is this voltage; A is infinity. So, this voltage is pulled down to zero. This therefore is called virtual ground.

This is an important concept. If I ground the amplifier and if the amplifier gain is made infinity and if the output is finite and output is connected to input through negative feedback, then it is always this potential that becomes virtual ground. Potential here is the same as that of the ground potential, virtual; which means, the current in this is V_s

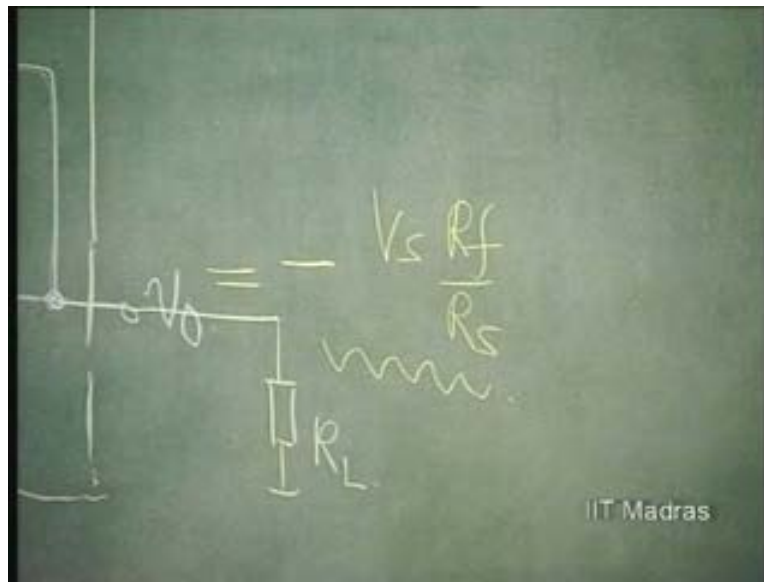
divided by R_s and this current cannot go into a nullor. So, it can only go into R_f and develop a potential which is V_s by R_s into R_f , with this end positive and that end negative.

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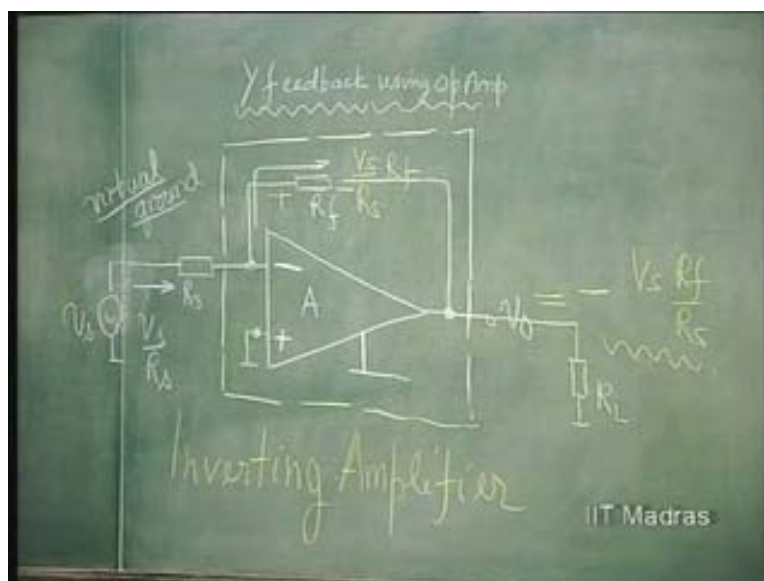
So, this is at ground potential and therefore output potential V_o is nothing but the potential across R_f because this is at ground potential, virtual ground. So, this is minus, because this is plus and that is minus; V_s into R_f divided by R_s , independent of R_L .

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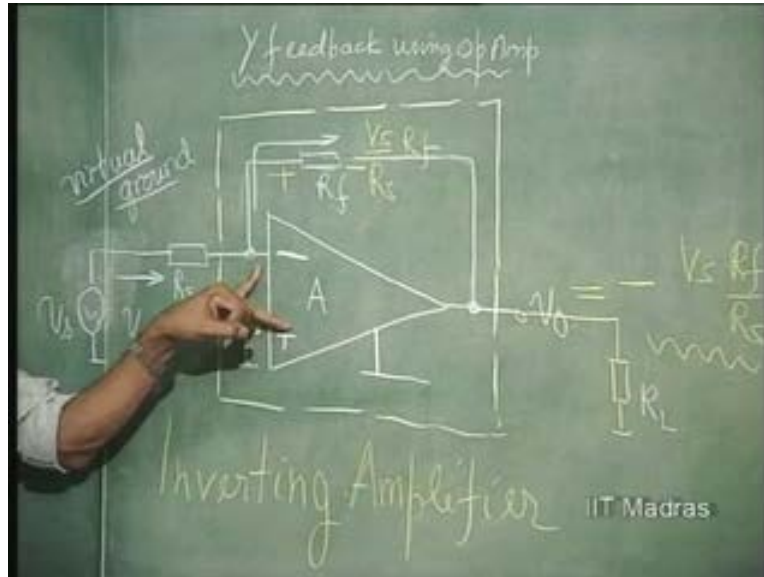
Because this is virtual ground, the current pumped into this is V_s / R_s and the same current is forced to go into this feedback network, R_f ; develops a potential, V_s / R_s into R_f . Therefore, V_o is... This is therefore called an inverting amplifier. Why inverting? There is a phase shift of 180 degree here. If the input amplitude is increasing, here it will be decreasing.

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So, there is a phase inversion, inverting amplifier; and the gain is R_f by R_s . So, there is a concept here that is to be highlighted is that, this point is always at virtual ground. That means this is a current summation point.

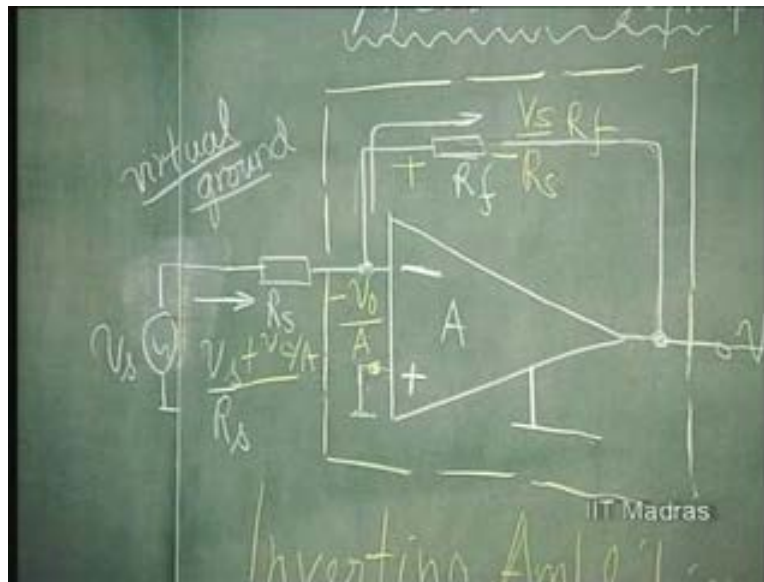
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Any number of currents can be added here; and all those currents will be pumped into the feedback network. So, this concept is very useful in a variety of applications of converting current into voltage. We will see this later.

But now, suppose this is not infinity. Then what happens to this? We therefore will modify this. If this is not infinity, this potential is minus V_{naught} divided by A . It is not zero because this is V_{naught} . So, this is minus A . So, this potential is minus V_{naught} by A ; and therefore, this current is not V_s by R_s ; but it is V_s minus V_{naught} by A . That is, V_s plus V_{naught} by A by R_s ; and it is this current that will be going into the R_f .

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Therefore, the potential is going to be V_s plus V_o by A divided by R_s into R_f . Instead of... here we... V_s into R_f by R_s . Therefore, V_o is going to be not zero; because this potential is not zero. So, it is minus... V_o is going to be minus V_o by A , this potential, minus V_s plus V_o by A into R_f by R_s .

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$$V_o = -\frac{V_o}{A} - \frac{(V_s + \frac{V_o}{A}) R_f}{R_s}$$

So, if A is infinity, you can just look at it. This will go to zero; this will go to zero; and we will get back what we had earlier. That is minus V_s into R_f by R_s . Therefore, V_o naught into 1 plus... you have 1 over A plus R_f by R_s over A from this; and this is equal to... This factor, these two factors, have been taken into account and minus V_s into R_f by R_s .

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The image shows a chalkboard with handwritten mathematical equations. The top equation is $V_o = -\frac{V_o}{A} - \frac{(V_s + \frac{V_o}{A})R_f}{R_s}$. The bottom equation is $V_o \left[1 + \frac{1 + R_f/R_s}{A} \right] = -V_s R_f / R_s$. To the right, there is a small circuit diagram showing a voltage source V_s in series with a resistor R_s . The text "IIT Madras" is visible in the bottom right corner of the chalkboard image.

So, V_o naught by V_s , which is the transfer function now becomes modified at minus V_s into R_f by R_s divided by 1 plus 1 plus R_f by R_s by A.

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The image shows a chalkboard with the following handwritten equation:

$$\frac{V_o}{V_s} = \frac{-V_s R_f / R_s}{\left[1 + \frac{1 + \frac{R_f}{R_s}}{A} \right]}$$

Below this equation, there is another expression: $V_o = -\frac{V_o}{1} - \left(V_s + \frac{V_o}{A} \right) R_f$. The text "IIT Madras" is visible in the bottom right corner of the chalkboard image.

So, you can see... if A were to tend to infinity, this is what it was. With A finite, we have that getting modified by gain. This is the loop gain. 1 plus loop gain. This is the loop gain. If you look at this, A into R s divided by R f is the loop. You short circuit this. A into R s by R s plus R f is the loop gain here. If you break the loop here... So, that is what it is. A into 1 plus 1 over loop gain. So, I will write this. So, if the loop gain is very high compared to 1, this goes towards zero. So, 1 plus 1 over loop gain.

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The image shows a chalkboard with the following handwritten equation:

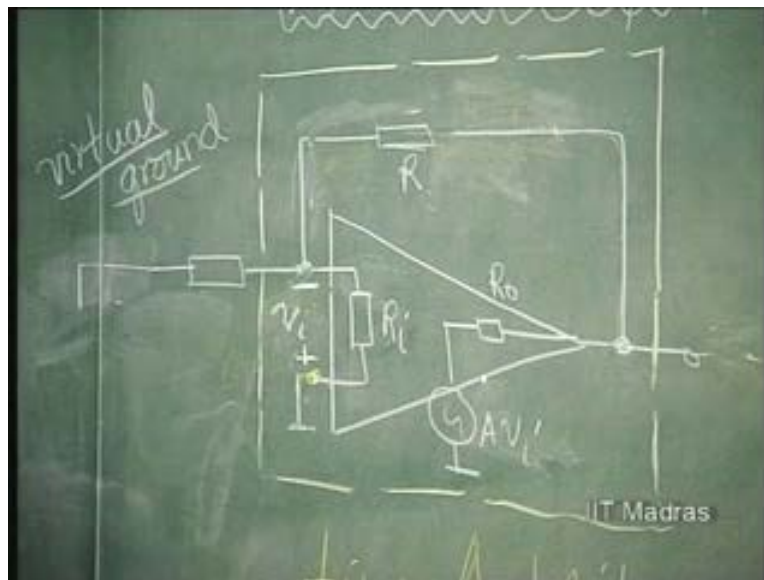
$$\frac{V_o}{V_s} = \frac{-V_s R_f / R_s}{\left[1 + \frac{1}{A \beta} \right]}$$

Below this equation, there is another expression: $V_o = -\frac{V_o}{1} - \left(V_s + \frac{V_o}{A} \right) R_f$. The text "IIT Madras" is visible in the bottom right corner of the chalkboard image.

So, let us now investigate this using proper parameters. What I mean is, just as I did in the case of h parameter, we investigate the feedback with R_i , R_{naught} , etcetera, also taken into account. So, instead of making this approximation, we will retain this just like this. Now we will consider the same circuit without neglecting R_i and R_{naught} .

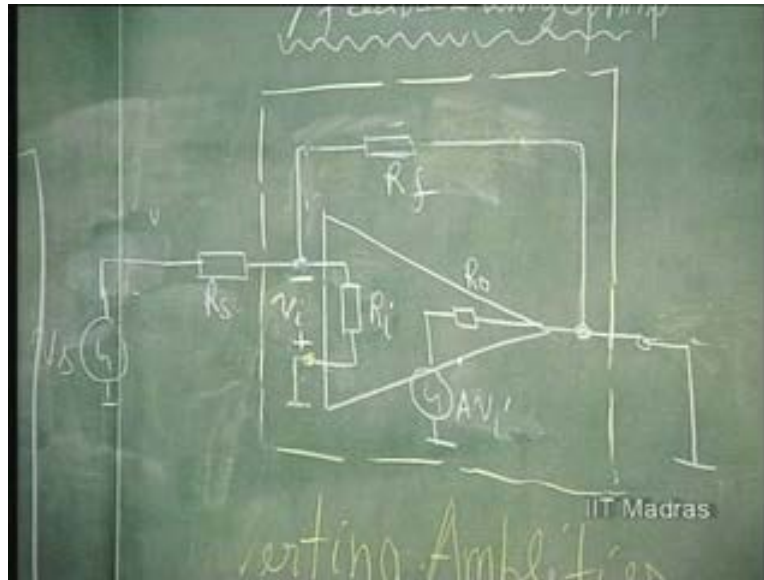
So, that means here instead of it being an open circuit, we have R_i , same thing; and here, the output R_{naught} and... if this is, let us say, V_i here, this is V_i ; A times V_i there. If this is positive and this is negative, this is A times V_i . So, this is the equivalent circuit now, of the op amp. Then, how does it work?

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So, once again... Now we will consider Y feedback. This is Y feedback. So, composite Y parameter must be determined. What is composite Y parameter? I short circuit the input and find out Y_i and Y_f . Short circuit the output; short circuit the output, find out Y_i and Y_f . Short circuit the input; find out Y_r and Y_o . So, let us do that. So, short circuit the output. So, we have here $1/R_i$. When I short the output, $1/R_i$ comes in shunt with $1/R_f$; $1/R_i$ comes in shunt with $1/R_f$.

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This is that of the amplifier; this is that of the feedback network. As far as the forward transfer parameter is concerned, if the voltage is V_i here, this way, this way, A times V_i is the voltage there and the current is $A V_i$ by R_o , that way. But, actual input is positive here and negative here. So, let us put it that way. Clearly understand. If this is V_i , then I should put here minus and plus indicating that there is an inversion.

So, if this is V_i , there is an inversion; A times V_i here... this applied to the inverting terminal. So, the current is going to be pumped in. If this is plus and minus, it will be pumped out. So now, pumped in... that means for an input current like this, this will be having a current, this way.

So, A times V_i by R_o is the output current. Output current divided by input voltage, this parameter. So, A times V_i by R_o divided by V_i . So, A by R_o is the Y_f of the amplifier alone. What about the feedback network? If we apply V_i here, the current V_i by R_f will be going out. So, minus 1 over R_f . So, you can see A by R_o is due to the amplifier; minus 1 over R_f is due to the feedback network. Simple.

Next, I short circuit the input and apply voltage at the output, the feedback parameter Y_f . When I apply voltage V_{naught} , if I short this, V_{naught} by R_f will be going out. So, minus 1 over R_f is Y_r . For the amplifier, there is no feedback. So, only the passive network has feedback. As far as output conductance is concerned, this is zero. V_i is zero. So, this is zero. So, 1 over R_{naught} plus 1 over R_f .

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$$\begin{bmatrix} \frac{1}{R_i} + \frac{1}{R_f} & -\frac{1}{R_f} \\ \frac{A}{R_o} - \frac{1}{R_f} & \frac{1}{R_o} + \frac{1}{R_f} \end{bmatrix}$$

These are the short circuit parameters very simply obtained by definition. Then, as far as the input is concerned, the source admittance is added in shunt. 1 over R_s . As far as the output is concerned, you can add 1 over R_L , so that, effectively you have, strictly speaking, the source that you have to use here should be compatible to that of the Y parameter. That means, instead of Thevenin source, you use Norton source, which means you put a shunt resistance of R_s and a current source of I_s , instead of using Thevenin source.

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Now, this is the composite Y parameter of this fairly complex Y feedback network. We can now find out the loop gain. Once again, you can see. Because A is coming here, R naught is coming here. So, this is infinity square. So, this can be neglected.

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$$\begin{bmatrix} \frac{1}{R_i} + \frac{1}{R_f} + \frac{1}{R_s} & -\frac{1}{R_f} \\ \frac{A}{R_o} & \frac{1}{R_o} + \frac{1}{R_f} + \frac{1}{R_L} \end{bmatrix}$$

And loop gain is A by R naught into minus 1 over R f divided by 1 over R i 1 over R f plus 1 over R s into 1 over R naught 1 over R f 1 over R L. This is the loop gain.

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loop gain

$$= -\frac{A}{R_o R_f}$$

$$\left(\frac{1}{R_o} + \frac{1}{R_f} + \frac{1}{R_D}\right) \left(\frac{1}{R_i} + \frac{1}{R_f} + \frac{1}{R_s}\right)$$

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So, you can again make the approximation. R_{naught} can be taken inside. $1/R_{naught}$, R_{naught} . So, I will rewrite it. $1 + R_{naught}/R_f + R_{naught}/R_L$. Once again, R_f can be taken inside this. So, $1 + R_f/R_i$, R_f/R_s .

So, you can see. Basically, the loop gain is minus A ; basically the loop gain is minus A ; or, if you... if you were to really make R_{naught} equal to zero, R_{naught} equal to zero and R_i equal to infinity, then the loop gain is minus A into $1 + R_f/R_s$. That is what we have got. This will go to zero; this will go to zero; this will go to zero. So, it will become minus A into $R_s/R_s + R_f$. Now, strictly speaking, R_s should be made equal to infinity also because it should be driven ideally by a current source. It is a current control thing.

So, R_s also... if it is made equal to infinity, then actual loop gain is minus A , if it is strictly a current feedback. So, you can see that this is the loop gain and everything decreases by loop gain. $1 + \text{loop gain}$.

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loop gain

$$-\frac{A}{\left(1 + \frac{R_0}{R_f} + \frac{R_0}{R_s}\right) \left[1 + \frac{R_f}{R_i} + \frac{R_f}{R_s}\right]}$$

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That means R_i becomes R_i divided by this factor. The original input impedance, input conductance, is this. This conductance is going to be multiplied by 1 plus loop gain. This conductance is $1/R_{nought} + 1/R_f + 1/R_L$. So, this again decreases; output impedance decreases. Or, output conductance increases by 1 plus loop gain. So, we will see how this gets now modified. As far as this parameter is concerned, it will become minus A divided by R_{nought} . This is the Y feedback. So, we have to convert it into Z parameter. So, what is the Z parameter? minus A by R_{nought} divided by this into this plus this into this. In this, A by R_{nought} into $1/R_f$ is dominant factor plus you have that factor which is $1/R_i + 1/R_f + 1/R_s$ into $1/R_{nought} + 1/R_f + 1/R_L$.

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$$-\frac{A}{R_o}$$

$$\frac{\frac{A}{R_o} \frac{1}{R_f}}{1 + \left(\frac{1}{R_i} + \frac{1}{R_f} + \frac{1}{R_o}\right) \left(\frac{1}{R_o} + \frac{1}{R_f} + \frac{1}{R_i}\right)}$$

loop gain

$$-\frac{A}{R_f}$$

This factor is negligible compared to this because you have A going towards very high value - 1 over R naught going very high. Strictly speaking, therefore, this will converge towards minus 1 over R f; sorry, that is 1... 1 by minus 1 over R f; or, this is going to be equal to minus R f, here. A by R naught will get cancelled by A by R naught. So, this will be 1...minus 1 by 1 over R f; or minus R f.

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$$-\frac{A}{R_o}$$

$$\frac{\frac{A}{R_o} \frac{1}{R_f}}{1 + \left(\frac{1}{R_i} + \frac{1}{R_f} + \frac{1}{R_o}\right) \left(\frac{1}{R_o} + \frac{1}{R_f} + \frac{1}{R_i}\right)}$$

loop gain

$$-\frac{A}{R_f}$$

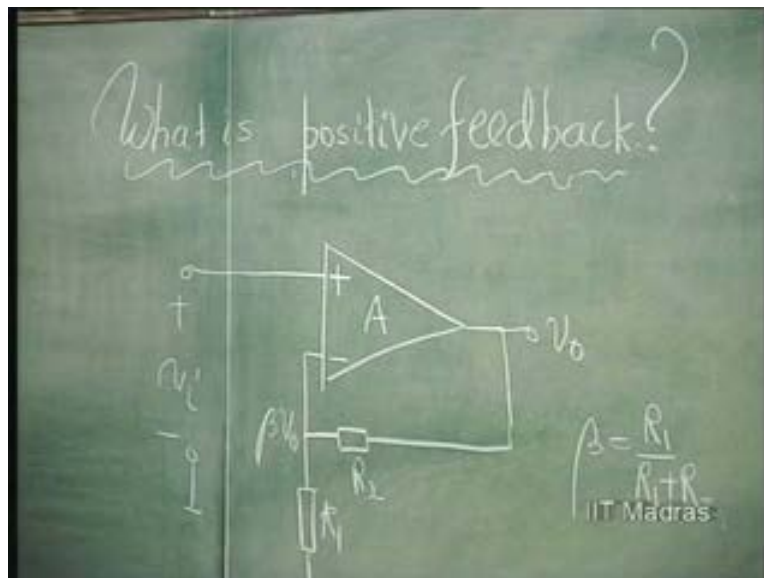
$$\left(1 + \frac{R_o}{R_f} + \frac{R_i}{R_f}\right) \left(1 + \frac{R_f}{R_i} + \frac{R_f}{R_o}\right)$$

So, the Z parameter, Z_f is going to be minus R_f . Now, all these parameters... Z_i is going towards zero; Z_{naught} is going towards zero, by a factor which is 1 plus loop gain, from the original value. So, please see this. This becomes insensitive to operational amplifier gain. It is simply the impedance connected between output and the input.

So, if I apply I_s here, what it means is this I_s will almost totally go across this. This is virtual ground and the output will be minus I_s into R_f . So, now we have seen v feedback and h feedback as applied to the operational amplifier. As I told you, these are the two negative feedback structures available to us.

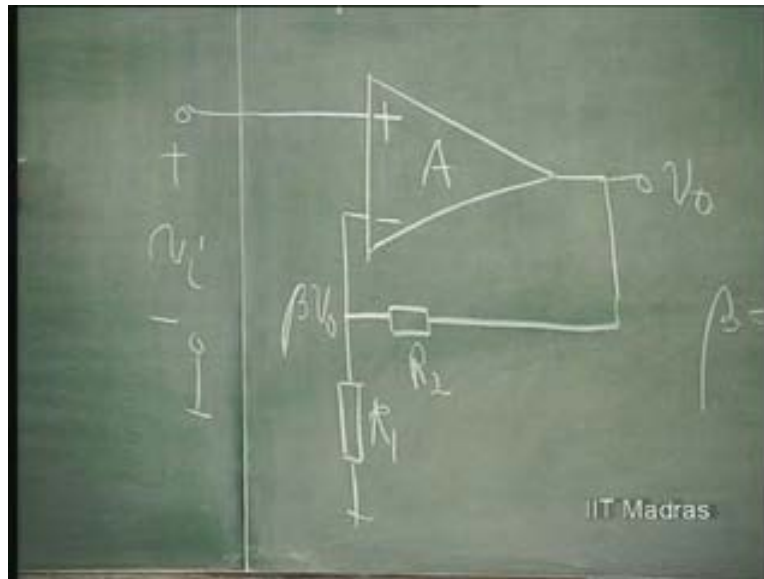
I would like to, at this juncture, also discuss what happens if we give positive feedback. So, I want to now, in the light of the op amp being made available to us... we have understood negative feedback and we have seen that negative feedback improves the performance of the amplifier enormously; brings about linearity; brings about insensitivity; and also reduces effect of noise, etcetera. Now, let us see what happens if we give positive feedback.

(Refer Slide Time: 47:26)



So far, we have been concentrating on negative feedback and its virtues. Let us now consider what is positive feedback. Whether it is going to be useful at all is one point we would like to see; and how far positive feedback can be given. This is the negative feedback circuit illustrating voltage, negative feedback output voltage is sent. Beta times V_{naught} is fed back to the input which is the inverting input.

(Refer Slide Time: 48:04)



This is plus. So, V_i ... V_i is the actual input. Minus βV_{naught} . V_i minus...this is important... βV_{naught} , is what the amplifier takes at the different signal. V_i That means output voltage is fed back. V_{naught} is going to be in phase with V_i because it is applied to plus. So, βV_{naught} is in phase with V_i . If βV_{naught} is in phase with V_i , V_i , βV_{naught} , they are both in phase voltages.

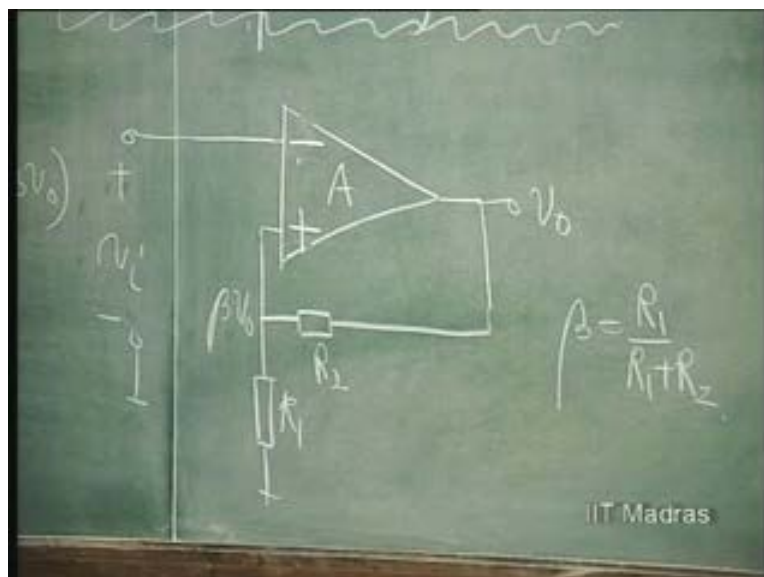
So, V_i minus βV_{naught} means this βV_{naught} is opposing the original input; opposing... the fed back voltage is opposing the input and that is the resultant voltage that is applied to the amplifier. So, V_i ... V_i minus βV_{naught} ; that times A is equal to V_{naught} and from this we have got V_{naught} over V_i as A by 1 plus $A \beta$. This we had discussed earlier.

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$$\frac{v_o}{v_i} = \frac{A}{1+A\beta}$$
$$v_o = A(v_i - \beta v_o)$$

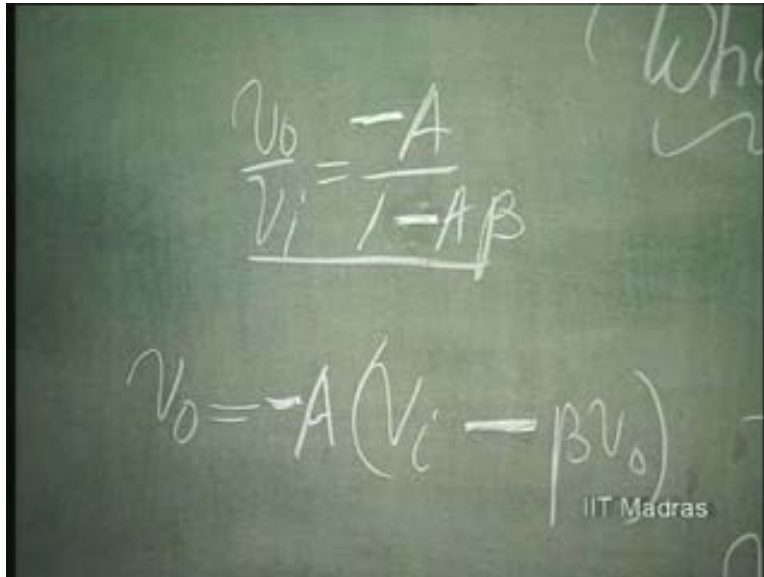
Now I am going to make it different. This is going to be minus and this is going to be plus. So, v_o and v_i are out of phase; and this βv_o is going to be coming in series with v_i . So, what happens here? Now earlier, $v_i - \beta v_o$ was getting multiplied by A . But now, $v_i + \beta v_o$ is getting multiplied by A . That is the thing. Wherever A was there, put $-A$ and you will get the equation because earlier $v_i - \beta v_o$ was multiplied by A .

(Refer Slide Time: 49:57)



So now, V_i minus βV_o is going to be multiplied by $-A$, because of the inversion. So, this becomes $-A(V_i - \beta V_o)$. So, this is what happens with positive feedback. This is called positive feedback.

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$$\frac{V_o}{V_i} = \frac{-A}{1 - A\beta}$$
$$V_o = -A(V_i - \beta V_o)$$

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You consider... Ground this. This is A . This is βV_o . That means if I have V_i here, A times βV_o will appear here. The loop gain is positive. Now, this is V_i . This will be A times V_i and A times βV_o . So, loop gain is positive now. So, you get $-A$ by $1 - A\beta$ as the gain.

So, if $A\beta$ is less than 1, whereas β is zero, no feedback situation; V_o/V_i is going to be $-A$. If β is finite, but $A\beta$ is less than 1, then the gain is going to be greater than A , because A is 10, let us say. $A\beta$ is point 9. This is 10 divided by $1 - 0.9$ which is 100. So, from an amplifier of gain 10, I can get an amplifier of 100. So, using positive feedback, you can increase the gain.

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$$\frac{v_o}{v_i} = \frac{-A}{1 - A\beta} \quad A\beta < 1$$
$$v_o = -A(v_i - \beta v_o)$$

What

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This is an advantage; but then, it is very sensitive to that. If A Beta becomes point 99, then it will go to 1000. If it is point 999, it will go to 10,000. So, a small variation in A Beta will boost up this gain enormously. If A Beta becomes equal to 1, this goes to infinity; a practical way of obtaining infinite gain amplifier is this.

Now question is what happens if A Beta becomes greater than 1? We will discuss this in the next class. That is called regenerative positive feedback. Until A Beta equal to 1...is less than 1, this can be still used as an amplifier. Beyond A Beta equal to 1... Beyond A Beta greater than or equal to 1, this is not possible to be used as an amplifier.

That is called regenerative positive feedback which is finding also application in a large number of circuits. We will discuss this later. The positive feedback of A Beta between zero and 1 is also used in what are called comparators. We will discuss this in the next class. So, positive feedback after all may be quite useful in certain other applications, other than amplifiers.