

Cooling Technology: Why and How utilized in Food Processing and allied Industries

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Lecture 28
Carnot Cycle (Contd.)

Good afternoon my students. We are in the last phase of Carnot cycle right. If you remember we started with Carnot and today it will be the last Carnot cycle plus and we will be recapitulating a little then come to some problem solution. In the previous class we have shown that what is the efficiency Carnot efficiency that is $1 - \frac{Q_L}{Q_H}$ and that is $1 - \frac{T_L}{T_H}$. We have done one problem also perhaps around 62.5 percent towards the efficiency.

If, I remember, we have done the cycle from point 1, point 2, point 3, point 4. Before that, we had done the state points in psychrometry, all in detail, and all the state points, we have said, are reversible in Carnot cycle, right. All the paths from the state points 1, 2, 3 and 4 back to 1 are reversible. This we have shown and said many times. Apart from this, we have also shown that, if we have the two hot and cold reservoirs, and if we have two engines, one is reversible and another is irreversible, then the reversible engine will have higher efficiency than that of the irreversible, because we showed that the work done or obtained from an irreversible engine is always less than that of the reversible one under the same operating hot and cold reservoirs, right. This you have to keep in mind that, both the hot and cold reservoirs, they are to be identical for both the engines.

If there is a discrepancy, definitely the output also will be different, and we cannot compare. For comparison, it has to be identical. We have also shown that the reversible engine, whatever it is, producing work as work output as W_R from the hot reservoir source as Q_C quantity of heat supply, Q_H quantity of heat supplied, and then Q_C quantity of heat is rejected to the cold reservoir, and we reversed and showed that, since it is reversible, then Q_C quantity of heat, if it is extracted from the cold reservoir and if W_R quantity of work is done on the engine, then Q_H quantity of heat is produced, which we had also supplied without a reservoir, as if, this is the reservoir to the irreversible engine and obtain the same W_I quantity of work and Q_C dot or Q_C prime quantity of heat was rejected to the cold reservoir, right, and by this, we had said or we had come to the conclusion that W_R is never less than W_I because, that violated the Kelvin Planck statement, and W_I is never equal to W_R , because if W_I is equal to W_R , then it is converted to a reversible engine only, right. Then, we had also shown that, if

there are two reservoirs working under the same two, sorry, if there are two reversible engines working under the same two reversible same two heat and cold reservoirs, then, the work obtained from one engine is W_{R1} and work obtained from the other engine is W_{R2} , and we also, we also showed that W_{R1} is equal to W_{R2} and that is why, yeeta thermal $R1$ is equal to yeeta thermal $R2$ right. So, on continuation of that, this being the last on the Carnot, we recapitulate, a little, as we are doing, we have shown that this W_{R1} , W_{I1} , Q_{C1} , Q_{C2} dot, that, if they were W_{I1} , was more, then that was violating the current Kelvin Planck statement. Then, we made W_{R1} equal to W_{I1} , then, that becomes equal to Q_{C1} equal to Q_{C2} . That is, it is converting into reversible engine. Then, we also showed that, if W_{I1} is less than W_{R1} , then, yeeta thermal irreversible, that is, W_{I1}/Q_{H1} , and yeeta thermal reversible is W_{R1}/Q_{H1} and yeeta thermal irreversible is less than yeeta thermal reversible, right, and we concluded from there, that, all reversible power cycles, operating between the same two thermal reservoirs, have the same thermal efficiencies, right. And here also, we showed that, instead of irreversible engine 1, if we substitute to that with reversible engine $R2$, and another one is reversible engine, $R1$, then, operating between the two same hot and cold reservoir one is giving W_{R1} work, and other is giving W_{R2} work, and same Q_{H1} quantity of heat is supplied to $R1$ and Q_{C1} quantity of heat is rejected to the cold reservoir, and if, we reverse, then, we got the same Q_{H1} as output and Q_{C1} as input and W_{R1} was done on the system, and when, we supplied it to the $R2$, the same quantity, we are getting Q_{H1} to the reservoir $R2$ to the reversible engine $R2$, and W_{R2} work was obtained and Q_{C1} quantity of heat was rejected. This, we got to the corollary of the Carnot, that both engines receive, Q_{H1} , and Q_{H1} quantity and Q_{C1} quantity of heat is rejected for which, Q_{cycle} becomes 0, and W_{cycle} also becomes 0, for both the engines, with one reversed, because, they are both reversible, right, and here, we can also show, tell, one more thing, let me say that, instead of this, instead of this, that you are supplying Q_{H1} and Q_{H1} you are obtaining, you could have done the same thing with air, you have done supplied Q_{H1} , you had supplied air Q_{C1} , and you obtain, the same Q_{H1} and that same Q_{H1} could have been supplied to this right.

So, it is, yes, I mean irrespective, whether, you are getting it from $R1$ by reversing, or you are getting it from $R2$ by reversing, because, both are reversible, right. So, that we have not specially or categorically, differently, we had shown, but here, we are saying that, instead of $R1$ reversing, we can also reverse $R2$ and obtain the same, right. This we have to keep in mind that instead of reversing $R1$, if we reverse $R2$. the same Q_{C1} quantity of heat, we extract from the cold reservoir, then, we obtain the same Q_{H1} quantity of heat, given to the hot reservoir, and the same will be, then, coming back to the $R1$, and there will be no change. So, there also you will get W_{R1} equals to W_{R2} and here also we will get W_{R1} equals to W_{R2} right. So, that, what, corollaries, we are saying in the cycles that becomes then reality. So, that, if we have reversed, and now we

said that reversing can be done, by either R 1 or by R 2, the same result will be obtained, right.

So, Q cycle in both the cases becomes 0 and W cycle also in both the cases becomes 0, because both the engines with one reversed are obtaining the same result, because, both are reversible. So, with one engine reversed, we got, and we got this relation, that W cycle is 0 is equal to W R 1 minus W R 2 and that is why we said W R 1 is equal to W R 2, if both are reversible. That obviously, has to be kept in mind, all the time, that this is true, if both are reversible. And if you remember, in the beginning, when we are starting with cycle Carnot, or even earlier, that, we were always, say, I was always saying that, if it is reversible, all the, all the cycles, if they are reversible, then, only it is possible to achieve the Carnot cycle. We also will say, afterwards, the defects or difficulties of the Carnot cycle, but not now, because we are now with the Carnot cycle and that Carnot cycle, all possibilities, all corollaries, we have stated, and we are recapitulating in the last class of the Carnot cycle. Now, yeeta thermal R 1 and yeeta thermal R 2 were also shown to be same, where yeeta thermal R 2 was equal to W R 2 over Q H and yeeta thermal R 1 is equal to W R 1 over Q H and W R 2 over Q H was equal to W R 1 over Q H and that is why, we can say, or we said, rather, yeeta thermal R 2 is equal to yeeta thermal R 1, that is, what we have shown right. Yeeta thermal R 2 is equal to yeeta thermal R 1 because, W R 1 by Q H is equal to W R 2 by Q H, which are equal to yeeta thermal R 1 and yeeta thermal R 2 respectively, and so, yeeta thermal R 2 is equal to yeeta thermal R 1 right, and this is one corollary of the Carnot and that is called second corollary of the Carnot cycle.

Carnot's second corollary

Both engines receive Q_H , and $Q_{\text{cycle}} = 0$
and $W_{\text{cycle}} = 0$ for both engines with
one reversed because they are both
reversible.

Now, with engine 1 reversed.

$$W_{\text{cycle}} = 0 = W_{R,1} - W_{R,2}$$

and $W_{R,1} = W_{R,2}$

Carnot's second corollary

And

$$\eta_{th,R2} = \frac{W_{R,2}}{Q_H} = \frac{W_{R,1}}{Q_H} = \eta_{th,R1}$$

So,

$$\eta_{th,R2} = \eta_{th,R1}$$

Now, from there we came to the principles of Carnot cycle, and we had said, as here we have seen that, the yeeta thermal reversible A and yeeta thermal reversible B, both are identical, right, and if that be true, we also said that yeeta thermal irreversible is less than yeeta thermal reversible, right, and all reversible cycles have the same thermal

efficiency, that also we have said. Now, also we said that, the thermal efficiency of reversible in Carnot engines are yeeta thermal is equal to W_{net} over Q_H and that was equal to $1 - Q_L / Q_H$, and this is a function of temperature only, that is, T_L and T_H , T_L , is the low temperature, and T_H is the high temperature, right. So, that low whatever it be, high, whatever, it be, depending on that the efficiency will be found out. Now, we also found out one efficiency with 800 Kelvin as the boiler temperature and 300 Kelvin as the cooling tower temperature. So, we find found out the efficiency to be 62.5. Now, if we say, some other, high very high temperature, say, T_H is equal to say, 1200 degree centigrade, right and T_L is equal to say, 400 or 500 degree centigrade, T_L is say 500, or for simplicity of the calculation say, 600-degree centigrade right. Then, yeeta thermal we can write to be equal to $1200 - 600$ divided by 1200, right that was, that, $1 - T_L / T_H$, that is $T_H - T_L$ by T_H . So, $T_H - T_L$ by T_H . So, $1200 - 600$ is 600 by 1200 right. So, this two goes out.

So, 6 by 12 is equal to 1 by 2 that is 0.5, that means, 50 percent efficiency, right. Similarly, any such problem, you can find out the efficiency, whatever be the temperature, depending on that, you can determine the efficiency. Then, one more we can take, smaller one, that one, we had taken very high say, one is 100 degree centigrade that is T_H equals to 100 degree centigrade and T_L is say 10 degree centigrade, right. Then what will be the efficiency? I hope you can do it very well.

So, yeeta thermal is equal to $100 - 10$ over 100, that is 90 over 100 that is 9 by 10, so that means, 0.9. So, that is 90 percent efficiency right, sorry, there is 90 percent efficiency. So, if these be 90 percent efficiency, that means, if the temperature is lower, efficiency goes up, if the temperature is higher, efficiency goes down, also the difference of the temperature, that is also a factor, because, here we have taken only 90 degree as the difference. In earlier cases it was, maybe 500, 600 degree centigrade difference.

$$\eta_{th} = W_{net} / Q_H = 1 - (Q_L / Q_H) = f(T_L, T_H)$$

$$\eta_{th} = 1 - (Q_L / Q_H) = 1 - (T_L / T_H).$$

So, that is also one subsequent classes, not in the Carnot cycle, but maybe some other will show that yes, this is because ultimately this Q_L and Q_H , that will correspond to that will correspond to the condenser and the evaporator, right. So, this gradually will come across. So, at this very moment we are not there. So, we should not say, but we have already shown that, if the difference is low then your efficiency is high. Say, another one if T_H is equal to say 200 degree centigrade and T_L is equal to say, 40 degree centigrade, right.

Now, the difference, we have taken moderate one, right. So, yeeta thermal we can write as equal to $200 - 40$ divided by 200. So, $200 - 40$ means, 160 divided by 200. So, it is 0.8. So, 16 means 4 and this is 5 right.

So, that means, we have got $\frac{4}{5}$ that is 0.8. That means, 80 percent is the efficiency right. So, we are going high right. Again, we come back to one more because, this is giving us practice, also that if T_H if T_H is equal to say 60 degree right, and T_L equal to, it is not possible theoretically, saying say, 0 degree then we got $\frac{60 - 0}{60}$.

That means, $\frac{60}{60}$ that means, 1 that means, 100 percent, which is not yeah, it is possible, if it is reversible Carnot engine right, but because it is becoming 100 right. Another problem if we take, T_H to be equal to say 300 degree and T_L to be say 30 degree then yeeta thermal, that becomes equal to $\frac{300 - 30}{300}$ that means, 270 divided by 300 and that becomes, so, it can be divided by 3. So, 90 and it can be divided by 3, 30.

So, $\frac{90}{100}$. So, again 0.9. So, again 90 percent. So, depending on your temperatures you can get the efficiencies, right.

This we have done. Now, the last one if we do is that, this is a problem, say let us analyze an ideal gas undergoing a Carnot cycle between two temperatures T_H and T_L right. So, 1 to 2 is isothermal expansion, that is U_1 to 2 is 0, that is isenthalpic and Q_H is equal to Q_{1-2} that is, W_{1-2} which is, integral of $P Dv$, is equal to $EMR T_H \ln$ of V_2 by V_1 . So, T_L over T_H is V_2 by V_3 to the power k minus 1. So, 3 to 4 is isothermal compression, that is ΔU_{3-4} is 0. So, Q_L is equal to Q_{3-4} is W_{3-4} is minus $EMR T_L \ln$ of V_4 over V_3 .

Therefore, the other one 4 to 1 is adiabatic compression, that is Q_{4-1} is 0. Therefore, we can write T_L over T_H is equal to V_1 minus, V_1 over V_4 to the power k minus 1 right. So, from equation 1 and 2, that is this and that, we can write, V_2 over V_3 is equal to V_1 over V_4 . Therefore, V_2 over V_1 is V_3 over V_4 . Therefore, yeeta thermal is 1 minus Q_L over Q_H and that is equal to $1 - T_L$ over T_H , since $\ln V_2$ over V_1 is equal to $\ln V_4$ over V_3 .

It has been proven that eta thermal is $1 - \frac{Q_L}{Q_H}$ that is, $1 - \frac{T_L}{T_H}$ for all Carnot engines, since the Carnot efficiency is independent of the working substance right. So, with this, let us conclude, our Carnot cycles. Now, we will obviously go to, this was for Carnot engine, right, will may be going to the Carnot refrigeration, or many others ok. So, our time is up today.

Thank you for your listening. Thank you.